



2<sup>nd</sup> INTERNATIONAL CONFERENCE  
ON ANALYSIS AND ITS APPLICATIONS

July 12-15, 2016 Kirşehir / TURKEY



# Abstract Book

Editors

Vatan KARAKAYA - Mohammad MURSALEEN  
Qamrul Hasan ANSARI

Abstract  
Book



ICAA-2016  
Website



# 2<sup>nd</sup> INTERNATIONAL CONFERENCE ON ANALYSIS AND ITS APPLICATIONS

JULY, 12-15, 2016, KIRSEHIR / TURKEY

## Abstract Book

### Editors:

[Prof.Dr. Vatan KARAKAYA](#)  
Rector of Ahi Evran University  
Kırşehir, TURKEY

[Prof.Dr. Mohammad MURSALEEN](#)  
Aligarh Muslim University  
Aligarh, INDIA

[Prof.Dr. Qamrul Hasan ANSARI](#)  
Aligarh Muslim University  
Aligarh, INDIA

ISBN: 978-605-85712-3-5  
Ahi Evran University, Kırşehir / TURKEY - 2016



## FOREWORDS

Dear Conference Participants,

Welcome to the 2<sup>nd</sup> International Conference on Analysis and Its Applications (ICAA-2016).

The purpose of the 2<sup>nd</sup> International Conference on Analysis and Its Applications (ICAA-2016) is to bring together experts and young analysts from all over the world working in analysis and its applications to present their researches, exchange new ideas, discuss challenging issues, foster future collaborations and interact with each other.

The main objective of the workshop is to discuss recent results in nonlinear and variational analysis and their applications, particularly the fixed point theory, optimization and applications to medicine.

We expect the participation of many prominent experts from different countries who will present the state-of-the-art in summability theory, sequence spaces, approximation theory, nonlinear analysis, variational analysis, optimization, and their applications.

The conference brings together about 400 participants from 22 countries (Ajaria, Algeria, Azerbaijan, Bulgaria, China, England, France, India, Indonesia, Iran, Iraq, Morocco, Pakistan, Romania, Saudi Arabia, Senegal, Serbia, South Africa, Taiwan, Tunisia, Turkey, United States of America), out of which 331 are contributing to the meeting with oral and 35 with poster presentations, including nine plenary talks. Also, there are non-presenting 27 participants from India, Kuwait, Oman, Saudi Arabia, Tunisia, Turkey, and Turkmenistan.

It is also a goal of the conference to promote collaborative and networking opportunities among senior scholars and graduate students in order to advance new perspectives. Additional emphasis at ICAA-2016 is put on applications in related areas, as well as other science, such as natural science, economics, computer science and various engineering sciences. The papers presented in this conference will be considered in the journals listed on the conference websites and below:

- Advances in Difference Equations (SCI-Exp),
- Carpathian Journal of Mathematics (SCI-Exp),
- Journal of Nonlinear and Convex Analysis (SCI-Exp),
- Journal of Inequalities and Applications (SCI-Exp.),
- Creative Mathematics and Informatics,
- Istanbul Commerce University Journal of Science.

This booklet contains the titles and abstracts of almost all invited and contributed talks at the 2<sup>nd</sup> **International Conference on Analysis and Its Applications**. Only some abstracts were not available at the time of printing the booklet. They will be made available on the conference website <http://icaa2016.ahievran.edu.tr> when the organizers receive them. All talks will take place in Faculty of Arts and Sciences in Ahi Evran University, Bağbaşı Campus, Kırşehir/Turkey.

We wish everyone a fruitful conference and pleasant memories in Kırşehir, Turkey.

**Prof. Vatan KARAKAYA**  
On Behalf of Organizing Committee  
Chairman  
(Rector of Ahi Evran University)

It was a great moment of excitement when Prof. (Dr.) Vatan Karakaya, Rector, Ahi Evran University, discussed with me the matter of organizing the “International Conference on Analysis and Its Applications (ICAA-2016)” at Ahi Evran University, Kırşehir. Now it is a matter of great pleasure that the matter of holding this conference is finally materialized. This conference is in the sequel of the first one which was held during December 19-21, 2015 (ICAA-2015) in Aligarh Muslim University, India. Being one of the Co-Chairmen of the conference, I feel privileged and delighted to welcome all delegates, eminent mathematicians, speakers and young researchers in this international event. It is expected that the delegates and the participants will be benefitted by the experience of this conference and the legacy of knowledge dissemination will be continued.

I wish all of you to have a nice and enjoyable participation in the conference.

**Prof. Mohammad MURSALEEN**

---

Analysis is one of the most important topics in mathematics and has been a focus of attention of all great mathematicians. There are many areas comes under this topic. However, this conference mainly devoted to some selected topics from analysis, mainly, Theory of Summability and Approximation, Fixed Point Theory, Fourier Analysis, Wavelet and Harmonic Analysis, Variational Analysis, Convex Analysis and Optimization, Geometry of Banach Spaces, Sequence Spaces and Matrix Transformations. During the last half century, nonlinear and variational analysis have been developed very rapidly because of their numerous applications to optimization, control theory, economics, engineering, management, medical sciences and other disciplines. On the other hand, the modern summability theory plays a very important role in linking theory of sequence spaces and matrix transformations with measures of noncompactness. Measures of noncompactness are widely used tools in fixed point theory, differential equations, functional equations, integral and integro-differential equations, optimization, etc. In the recent years, measures of noncompactness have also been used in defining geometric properties of Banach spaces as well as in characterizing compact operators between sequence spaces. We expect the participation of many prominent experts from different countries who will present their current research work and will also mention some hot topics for further research.

**Prof. Qamrul Hasan ANSARI**

## Scientific Committee

- A. Ioan RUS (Romania)  
 Abdul Rahim KHAN (Saudi Arabia)  
 Adrian PETRUŞEL (Romania)  
 Akhtam DZHALILOV (Uzbekistan)  
 Aldona DUTKIEWICZ (Poland)  
 Ayhan ŞERBETÇİ (Turkey)  
 Bilal ALTAY (Turkey)  
 Billy E. RHOADES (USA)  
 Brailey SIMS (Australia)  
 Bünyamin AYDIN (Turkey)  
 Calogero VETRO (Italy)  
 Cemil TUNÇ (Turkey)  
 Davide LA TORRE (UAE, Italy)  
 Daya Ram SAHU (India)  
 Doğan KAYA (Turkey)  
 Duran TÜRKÖĞLU (Turkey)  
 Eberhard MALKOWSKY (Turkey)  
 Ekrem SAVAŞ (Turkey)  
 Emrah Evren KARA (Turkey)  
 Erdal KARAPINAR (Turkey)  
 Fahreddin ABDULLAYEV (Turkey)  
 Fatih NURAY (Turkey)  
 Feyzi BAŞAR (Turkey)  
 Franco GIANNESSE (Italy)  
 Gradimir V. MILOVANOVIC (Serbia)  
 Hamdullah ŞEVLİ (Turkey)  
 Hanlar REŞİDOĞLU (Turkey)  
 Harun POLAT (Turkey)  
 Hasan AKIN (Turkey)  
 Henryk HUDZIK (Poland)  
 Heybetkulu S MUSTAFAYEV (Turkey)  
 Hong-Kun XU (China)  
 Hüseyin ÇAKALLI (Turkey)  
 İlham ALİYEV (Turkey)  
 İlhan İÇEN (Turkey)  
 İsmail EKİNCİOĞLU (Turkey)  
 İsmail KÖMBE (Turkey)  
 İsmail KÜÇÜK (Turkey)  
 Jen-Chih YAO (Taiwan)  
 Jesús Garcia-FALSET (Spain)  
 Johannes J. A. EKSTEEN (South Africa)  
 Johnson O. OLALERU (Nigeria)  
 Józef BANAS (Poland)  
 Kaleem Raza KAZMI (India)  
 Kazimierz GOEBEL (Poland)  
 Manaf MANAFLI (Turkey)  
 Mehmet Ali SARIGÖL (Turkey)  
 Mehmet Emin ÖZDEMİR (Turkey)  
 Metin BAŞARIR (Turkey)  
 Mikail ET (Turkey)  
 Mohamed Amine KHAMSI (USA)  
 Mohammad MURSALEEN (India)  
 Mohammad IMDAD (India)  
 Murat KİRİŞÇİ (Turkey)  
 Murat ÖZDEMİR (Turkey)  
 Murat SARI (Turkey)  
 Narin PETROT (Thailand)  
 Nazim B. KERİMOV (Turkey)  
 Necdet BATIR (Turkey)  
 P. VEERAMANI (India)  
 Poom KUMAM (Thailand)  
 Pratulananda DAS (India)  
 QamrulHasan ANSARI (India)  
 Rais AHMAD (India)  
 Ravi P. AGARWAL (USA)  
 Rifat ÇOLAK (Turkey)  
 Richard F. PATTERSON (USA)  
 Sebahattin BALCI (Kırgızistan)  
 Sebaheddin ŞEVGIN (Turkey)  
 Seyit TEMİR (Turkey)  
 Sezgin AKBULUT (Turkey)  
 Suheil A. KHOURY (UAE)  
 Ştefan MARUŞTER (Romania)  
 Themistocles M. RASSIAS (Greece)  
 Tomás Domínguez BENAVIDES (Spain)  
 Vagif GULİYEV (Azerbaijan)  
 Vasile BERINDE (Romania)  
 Viktor I. BURENKOV (England)  
 Vishnu Narayan MISHRA (India)  
 W.C. WONG (Taiwan)  
 William Art KIRK (USA)  
 Yılmaz ALTUN (Turkey)  
 Wataru TAKAHASHI (Japan)  
 Yusuf ZEREN (Turkey)  
 Zuhair NASHED (USA)

## Organizing Committee

Vatan KARAKAYA (Chairman)(Turkey)  
Mohammad MURSALEEN (co-Chair) (India)  
Qamrul Hasan ANSARI (co-Chair) (India)  
Billy E. RHOADES (co-Chair) (USA)  
Necip ŞİMŞEK (coord.) (Turkey)  
Ali AKBULUT(coord.) (Turkey)  
Faik GÜRSOY (coord.) (Turkey)  
Kadri DOĞAN (coord.) (Turkey)  
Yunus ATALAN (coord.) (Turkey)  
Javid ALI (India)  
Arife Aysun KARAASLAN (Turkey)  
Aysun SOYSAL (Turkey)  
Derya SEKMAN (Turkey)  
Emirhan HACIOĞLU (Turkey)  
Ezgi ERDOĞAN (Turkey)  
M. Abdussamed MALDAR (Turkey)  
Melih DİKMEN (Turkey)  
Müzeyyen ERTÜRK (Turkey)  
Nour El Houda BOUZARA (Turkey)

## Local Organizing Committee

### *Department of Mathematics Ahi Evran University*

Levent KULA (Turkey)  
Vagıf GULİYEV (Turkey-Azerbaijan)  
Ali AKBULUT (Turkey)  
Abdullah KOÇ (Turkey)  
Ayşegül ÇETİNKAYA (Turkey)  
Benen AKINCI (Turkey)  
Bülent ALTUNKAYA (Turkey)  
Cem OĞUZ (Turkey)  
Emine ÖNAL (Turkey)  
Emrah AYDEMİR (Turkey)  
Emre TAŞ (Turkey)  
Fatih DERİNGÖZ (Turkey)  
Ferdağ KAHRAMAN AKSOY (Turkey)  
Handan KÖSE (Turkey)  
Hasan ALTINBAŞ (Turkey)  
Hasan ÜNAL (Turkey)  
Hatice ÖZCAN (Turkey)  
Hüseyin BULUT (Turkey)  
İlkay BİLGİN (Turkey)  
İsmail Onur KIYMAZ (Turkey)  
KasımEmre AKSOY (Turkey)  
Kemal ARIKAN (Turkey)  
Kemal KURT (Turkey)  
Kıvanç KARAKAŞ (Turkey)  
Mahmut MAK (Turkey)  
Mesut ALTINOK (Turkey)  
Nagehan KILINÇ GEÇER (Turkey)  
Nesrin GÜLLÜOĞLU (Turkey)  
Nil MANSUROĞLU (Turkey)  
Ömer UÇAR (Turkey)  
Şebnem YILDIZ (Turkey)  
Sezin AYKURT SEPET (Turkey)  
Süleyman ÇELİK (Turkey)  
Turhan KARAMAN (Turkey)  
Yasin KARAKAYA (Turkey)  
Zehra GÜZEL ERGÜL (Turkey)

# Contents

<b>FOREWORDS .....</b>	<b>3</b>
<b>SCIENTIFIC COMMITTEE .....</b>	<b>5</b>
<b>ORGANIZING COMMITTEE.....</b>	<b>6</b>
<b>LOCAL ORGANIZING COMMITTEE.....</b>	<b>6</b>
<b>PLENARY TALKS .....</b>	<b>25</b>
UPPER AND LOWER SOLUTION METHOD FOR $N^{\text{TH}}$ ORDER BVPs ON AN INFINITE INTERVAL.....	25
<i>Ravi P. AGARWAL</i>	
MEASURES OF NONCOMPACTNESS AND THEIR SEVERAL APPLICATIONS.....	25
<i>Mohammad MURSALEEN</i>	
THE CHALLENGE AND MAGIC OF INVERSE PROBLEMS AND THE MATHEMATICS OF SIGNAL PROCESSING .....	26
<i>Zuhair NASHED</i>	
FIXED POINT ALGORITHMS FOR OPTIMIZATION .....	26
<i>Hong-Kun XU</i>	
QUADRATURE METHODS FOR COMPUTING HIGHLY OSCILLATORY INTEGRALS WITH BESSEL FUNCTIONS.....	27
<i>Gradimir V. MILOVANOVIĆ</i>	
A GLANCE INTO THE WORLD OF ITERATIVE SCHEMES: STABILITY AND RATE OF CONVERGENCE .....	28
<i>Vasile BERINDE</i>	
COUPLED FIXED POINTS AND DIAGONAL OPERATORS.....	28
<i>Adrian PETRUŞEL</i>	
WEAK SHARP SOLUTIONS AND MINIMUM AND MAXIMUM PRINCIPLE SUFFICIENCY PROPERTIES FOR NONSMOOTH VARIATIONAL INEQUALITIES .....	29
<i>Qamrul Hasan ANSARI</i>	
<b>INVITED TALKS .....</b>	<b>30</b>
AN ALGORITHM OF ASYMPTOTICALLY NONEXPANSIVE MAPPINGS WITHOUT FAST RATE CONVERGENCE CONDITION IN HYPERBOLIC SPACES .....	30
<i>Abdul Rahim KHAN, Hafiz FUKHAR-UD-DIN</i>	
CHEBYSHEV CENTERS, FIXED POINT THEOREMS AND BEST PROXIMITY POINT THEOREMS.....	31
<i>P. VEERAMANI</i>	
OPTIMALITY CONDITIONS FOR GENERALIZED VECTOR EQUILIBRIUM PROBLEMS .....	31
<i>Ali FARAJZADEH</i>	
GENERALIZED MORREY REGULARITY FOR PARABOLIC EQUATIONS WITH DISCONTINUOUS DATA.....	32
<i>Vagif. S. GULIYEV</i>	
COMPARATIVE EVALUATION OF A NEW ITERATIVE LEARNING CONTROL ALGORITHM BY NUMERICAL EXAMPLES.....	33
<i>Jan EKSTEEN, Stephan HEYNS</i>	
<b>CONTRIBUTED TALKS.....</b>	<b>34</b>
GENERALIZED BOUNDARY PROBLEM GOVERNED BY THE LAPLACIAN OPERATOR .....	34
<i>A. BOULAOUAD, B. MEROUANI</i>	
ON ORDER OF APPROXIMATION FUNCTION BY GENERALIZED BERNSTEIN-CHLODOVSKI POLYNOMIALS .....	35
<i>A.E. ABDULLAYEVA</i>	
STRONG UNIFORM CONSISTENCY RATES OF CONDITIONAL QUANTILES FOR FUNCTIONAL DATA IN THE FUNCTIONAL SINGLE-INDEX MODEL .....	36
<i>Abbes RABHI</i>	

A NOTE ON THE VALUES OF THE TWISTED BARNES ZETA FUNCTIONS AND THEIR APPLICATIONS.....	37
<i>Abdelmejid BAYAD, Yilmaz SIMSEK</i>	
GENERALIZATIONS OF KAPLANSKY'S THEOREM INVOLVING UNBOUNDED LINEAR OPERATORS.....	38
<i>Abdelkader BENALI</i>	
THE BOUNDEDNESS OF MAXIMAL AND CALDERON-ZYGMUND OPERATORS ON LOCAL MORREY-LORENTZ SPACES.....	39
<i>Abdulhamit KUCUKASLAN</i>	
DISCRETIZATION SCHEME TO FRACTIONAL DIFFUSION EQUATION WITH MEMORY TERM.....	39
<i>Abderrazek CHAOUI</i>	
TWO-PARAMETER REGULARIZATION METHOD FOR AN ILL-POSED CAUCHY PROBLEM FOR ELLIPTIC EQUATIONS.....	40
<i>A. BENRABAH, N. BOUSSETILA, F. REBBANI</i>	
ON THE EXISTENCE OF POSITIVE SOLUTIONS FOR NONLINEAR THREE-POINT BOUNDARY VALUE PROBLEM ...	41
<i>Abdulkadir DOGAN</i>	
POSITIVE SOLUTIONS OF A THREE-POINT BOUNDARY VALUE PROBLEM FOR $p$ -LAPLACIAN DYNAMIC EQUATION ON TIME SCALES.....	42
<i>Abdulkadir DOGAN</i>	
$\Delta_p^m$ -STATISTICAL CONVERGENCE.....	43
<i>Abdulkadir KARAKAŞ, Yavuz ALTIN</i>	
STURMIAN THEORY FOR SECOND-ORDER DIFFERENTIAL EQUATIONS WITH MIXED NONLINEARITIES.....	44
<i>Abdullah ÖZBEKLER</i>	
A UNIFIED APPROACH TO WEIGHTED $L_p$ HARDY-TYPE INEQUALITIES ON RIEMANNIAN MANIFOLDS.....	45
<i>Abdullah YENER</i>	
RELATION-THEORETIC CONTRACTION PRINCIPLE.....	46
<i>Aftab ALAM, Mohammad IMDAD</i>	
DYNAMICS OF A PRE-STRESSED AND IMPERFECTLY BONDED SANDWICH PLATE-STRIP CONSISTING OF ELASTIC LAYERS AND PIEZOELECTRIC CORE.....	47
<i>Ahmet DAŞDEMİR</i>	
TWO WEIGHTED INEQUALITIES FOR FRACTIONAL INTEGRALS ASSOCIATED WITH THE LAPLACE-BESSEL DIFFERENTIAL OPERATOR.....	48
<i>A. EROGLU, M. G. HAJIBAYOV</i>	
INTEGRAL INEQUALITIES OF HERMITE-HADAMARD TYPE FOR FUNCTIONS WHOSE THIRD DERIVATIVE ABSOLUTE VALUES ARE PREINVEX.....	48
<i>Akhilad IQBAL</i>	
TRIGONOMETRIC APPROXIMATION IN WEIGHTED LORENTZ SPACES USING LOWER TRIANGULAR MATRICES.....	49
<i>Ahmet Hamdi AVSAR, Yunus Emre YILDIRIR</i>	
CONFORMABLE FRACTIONAL INTEGRALS AND RELATED GRÜSS TYPE INTEGRAL INEQUALITIES.....	50
<i>Ahmet OcaK AKDEMİR, Alper EKİNCİ, Erhan SET</i>	
NEW INTEGRAL INEQUALITIES FOR GEOMETRICALLY CONVEX FUNCTIONS VIA CONFORMABLE FRACTIONAL INTEGRALS.....	51
<i>Ahmet OcaK AKDEMİR, Merve AVCI-ARDIÇ, Abdullatif YALÇIN</i>	
NEW RESULT IN STABILITY ANALYSIS OF SINGULAR PROBLEM.....	52
<i>Ahu ERCAN, Etibar S. PANAKHOV</i>	
ANALYSIS OF EFFECT OF FLEXIBLE WING ON LIFT AND DRAG COEFFICIENT.....	53
<i>Akshaya DEVI</i>	
ROUGH FRACTIONAL MULTILINEAR INTEGRAL OPERATORS ON GENERALIZED WEIGHTED MORREY SPACES..	53
<i>Ali KEBULUT</i>	



HYPERBOLIC SMOOTHING METHOD FOR DC PROBLEMS OBTAINED FROM CLUSTERING PROBLEMS.....	54
<i>Ali Hakan TOR</i>	
SOME APPROXIMATION PROPERTIES OF TWO DIMENSIONAL CHLODOVSKY-BERNSTEIN OPERATORS BASED ON (P, Q) INTEGER .....	55
<i>Ali KARAİSA</i>	
GAMMA TYPE GENERALIZATION SZASZ-CHARLIER OPERATORS.....	56
<i>Ali KARAİSA, Bilal ÇAVDAR</i>	
MULTIPLY SOLITARY WAVE SOLUTIONS OF THE HIGHER KDV EQUATIONS IN A STRATIFIED SHEAR FLUID FLOW WITH A FREE SURFACE .....	57
<i>Aly R. SEADAWY</i>	
EXTENDED TAN-COT METHOD FOR THE SOLUTIONS TO EVOLUTION EQUATIONS .....	58
<i>Anwar Ja'afar Mohamad JAWAD</i>	
STUDY OF A FOURTH-ORDER PARABOLIC EQUATION IN TIME-DEPENDENT DOMAINS.....	59
<i>Arezki KHELOUFI, Boubaker-Khaled SADALLAH</i>	
CONVERGENCE THEOREMS OF FIXED POINTS FOR HEMICONTRACTIVE MAPPINGS IN S-PROBABILISTIC NORMED SPACES .....	60
<i>Arife Aysun KARAASLAN, Vatan KARAKAYA</i>	
COLLOCATION METHOD USING RADIAL BASIS FUNCTION FOR SOLUTION OF FRACTIONAL KDV EQUATION .	61
<i>Asif YOKUŞ, Sema Gülbahar</i>	
HILBERT TRANSFORM ON LOCAL MORREY-LORENTZ SPACES.....	62
<i>Ayhan ŞERBETÇİ</i>	
SOME IDENTITIES ASSOCIATED WITH HURWITZ-LERCH ZETA FUNCTION .....	63
<i>Aykut Ahmet AYGÜNEŞ</i>	
APPROXIMATION BY TWO DIMENSIONAL GENERALIZED SZASZ OPERATORS .....	64
<i>Aynur N. MAMMADOVA</i>	
SOME PROPERTIES OF DOUBLE SEQUENCES AND THE P-CONVERGENCE OF A DOUBLY-SEQUENCE ITERATION WITH ERROR TERMS IN CAT(0) SPACES.....	65
<i>Aynur ŞAHİN, Metin BAŞARIR, Richard F. PATTERSON</i>	
MEASURE OF NONCOMPACTNESS AND FRACTIONAL DIFFERENTIAL EQUATIONS IN BANACH SPACE .....	66
<i>Aysun SOYSAL, Vatan KARAKAYA</i>	
A RELIABLE COMPUTATIONAL METHOD FOR SINGULAR PROBLEMS .....	67
<i>Ayşe Betül KOÇ</i>	
EKELAND'S VARIATIONAL PRINCIPLE AND ITS APPLICATION TO EQUILIBRIUM PROBLEMS .....	68
<i>Azadeh HOSSEINPOUR, Somyot PLUBTIENG, Ali FARAJZADEH</i>	
DYNAMIC EVOLUTION OF DAMAGE AND FRICTION IN PIEZOELECTRIC MATERIALS .....	69
<i>Abdelaziz AZEB AHMED, Tedjani HADJ AMMAR</i>	
BACKWARD DOUBLY SDES AND SPDES WITH SUPERLINEAR GROWTH GENERATORS .....	70
<i>Badreddine MANSOURI</i>	
SUBORBITAL GRAPHS FOR THE RESIDUE CLASS OF $PSL(2, Z_N)$ .....	71
<i>Murat BEŞENK, Bahadır Özgür GÜLER, Tuncay KÖR</i>	
A NEW RESULT ON GENERALIZED ABSOLUTE MATRIX SUMMABILITY .....	72
<i>Hikmet Seyhan ÖZARSLAN, Bağdagül KARTAL</i>	
ON REFLEXIVITY OF THE BOCHNER SPACE $LP(\mu, E)$ FOR ARBITRARY $\mu$ .....	73
<i>Banu AYTAR GÜNTÜRK, Bahaettin CENGİZ</i>	
CERTAIN HERMITE-HADAMARD TYPE INEQUALITIES ASSOCIATED WITH CONFORMABLE FRACTIONAL INTEGRAL OPERATORS .....	74
<i>Erhan SET, Barış ÇELİK</i>	

SHOCK AND RAREFACTION WAVES FOR BURGERS MODELS ON SPACETIME GEOMETRIES COMPARISON AND ANALYSIS .....	75
<i>Baver OKUTMUŞTUR</i>	
ON FLOQUET SOLUTIONS FOR DISCRETE STURM-LIOUVILLE PROBLEM WITH PERIODIC GENERALIZED FUNCTION POTENTIALS .....	76
<i>Manaf MANAFOV, Bayram BALA, Abdullah KABLAN</i>	
A NONLINEAR HYPERBOLIC PROBLEM FOR VISCOELASTIC EQUATIONS .....	77
<i>Benabderrahmane BENYATTOU, Rahmoune ABITA</i>	
PROJECTED TIKHONOV REGULARIZATION METHOD FOR FREDHOLM INTEGRAL EQNS OF THE FIRST KIND .....	77
<i>Boussetila NADJIB</i>	
ON SOME INTEGRAL INEQUALITIES ON TIME SCALES AND APPLICATIONS .....	78
<i>Boukerrioua KHALED</i>	
SINGULAR QUASILINEAR ELLIPTIC SYSTEMS WITH (SUB-, SUPER-) HOMOGENEOUS CONDITION .....	78
<i>Brahim KHODJA, Hana DIDI, Abdelkrim MOUSSAOUI</i>	
A NOTE APOSTOL TYPE (P,Q)-FROBENIUS-EULER POLYNOMIALS .....	79
<i>Burak KURT</i>	
ANALYSIS OF A SECOND ORDER AND UNCONDITIONALLY STABLE BDF2-AB2 METHOD FOR THE NAVIER-STOKES EQUATIONS .....	80
<i>Osman Raşit IŞIK, Bülent DEMİR</i>	
STRONGLY SUMMABLE AND STATISTICALLY CONVERGENT BIVARIATE FUNCTIONS .....	81
<i>Bünyamin AYDIN</i>	
ASYMPTOTICALLY $l_2$ -CESÀRO EQUIVALENCE OF DOUBLE SEQUENCES OF SETS .....	82
<i>Uğur ULUSU, Erdiç DÜNDAR, Bünyamin AYDIN</i>	
A NEW GENERALIZATION OF THE FIBONACCI $p$ -FUNCTIONS WITH PERIOD $k$ .....	83
<i>Yasin YAZLIK, Cahit KÖME</i>	
ASSOCIATE SPACES OF GENERALIZED WEIGHTED WEAK-LORENTZ SPACES .....	84
<i>Canay AYKOL YÜCE</i>	
SOME REFINEMENTS OF CERTAIN GAMIDOV INTEGRAL INEQUALITIES ON TIME SCALES AND APPLICATIONS .....	85
<i>Chiheb TARIK</i>	
THE RIESZ CAPACITY IN VARIABLE EXPONENT LEBESGUE SPACES .....	85
<i>Cihan ÜNAL, İsmail AYDIN</i>	
ON EXISTING OF FIXED POINT FOR MULTIVALUED MAPPING VIA MEASURE OF NONCOMPACTNESS .....	86
<i>Derya SEKMAN, Vatan KARAKAYA, Nour El Houda BOUZARA</i>	
DEFECT-DEFERRED CORRECTION METHOD FOR THE TWO-DOMAIN CONVECTION-DOMINATED CONVECTION-DIFFUSION PROBLEM .....	87
<i>Dilek ERKMEN, Alexander E. LABOVSKY</i>	
NONLINEAR WAVELETS AND THEIR STATISTICAL APPLICATIONS .....	88
<i>Djabrane YAHIA</i>	
SOLUTION OF FRACTIONAL HARRY DYM EQUATION WITH COLLOCATION USING RADIAL BASIS FUNCTION ...	89
<i>Doğan KAYA, Asif YOKUŞ</i>	
CHARACTERIZATION AND REVERSIBILITY OF 2D CELLULAR AUTOMATA WITH REFLECTIVE BOUNDARY .....	90
<i>Ecem ACAR, Selman UĞUZ, Rahime KOÇ</i>	
ANALYSIS OF TRAINING PERFORMANCES OF INTERPOLATION METHODS FOR MODELLING HUMAN BODY MOTION .....	91
<i>Egemen HALICI, Erkan BOSTANCI</i>	
A FRACTIONAL ORDER MODEL FOR OBESITY EPIDEMIC .....	92
<i>Elif DEMİRÇİ</i>	

EXISTENCE AND CONVERGENCE THEOREMS FOR MULTIVALUED GENERALIZED HYBRID MAPPINGS IN CAT( $\kappa$ ) SPACES.....	93
<i>Emirhan HACIOGLU, Vatan KARAKAYA</i>	
IDEAL CAUCHY CONDITION FOR INFINITE PRODUCTS.....	94
<i>Emrah Evren KARA, Metin BAŞARIR, Merve İLKHAN</i>	
SOME INEQUALITIES FOR $q$ -GAMMA FUNCTION .....	95
<i>İnci EGE, Emrah YILDIRIM</i>	
SOLVING INVERSE NODAL PROBLEM WITH JUMP CONDITIONS BY USING CHEBYSHEV POLYNOMIALS AND SOME RESULTS ON STABILITY .....	96
<i>Emrah YILMAZ, Hikmet KOYUNBAKA, N. Shahrbanoo KBARPOOR</i>	
SPECTRAL THEORY OF DIRAC SYSTEM ON TIME SCALES.....	97
<i>Tuba GULSEN, Emrah YILMAZ</i>	
SUMMABILITY OF DOUBLE SEQUENCES OF 0'S AND 1'S .....	98
<i>Emre TAŞ</i>	
UNBOUNDED UPPER AND LOWER SOLUTION METHOD FOR FOURTH-ORDER DELAY DIFFERENTIAL EQUATIONS ON THE HALF-LINE .....	99
<i>Erbil ÇETİN, Ravi P. AGARWAL</i>	
STABILITY AND SQUARE INTEGRABILITY OF SOLUTIONS OF NONLINEAR FOURTH ORDER DIFFERENTIAL EQUATIONS WITH DELAY .....	100
<i>Erdal KORKMAZ, Cemil TUNC</i>	
JENSEN'S INEQUALITY WITH OPERATOR $s$ -CONVEXITY (OR BRECKNER $s$ -CONVEXITY) IN HILBERT SPACE AND SOME ITS APPLICATIONS .....	101
<i>Erdal UNLUYOL</i>	
WIJSMAN STATISTICAL CONVERGENCE OF DOUBLE SEQUENCES OF SETS .....	102
<i>Fatih NURAY, Uğur ULUSU, Erdinç DÜNDAR</i>	
ROTATIONAL HYPERSURFACE IN 4-SPACE.....	102
<i>Erhan GÜLER, Martin MAGID, Yusuf YAYLI</i>	
ENNEPER TYPE SURFACES IN 4-SPACE.....	103
<i>Erhan GÜLER, Ömer KİŞİ, Semra SARAÇOĞLU ÇELİK</i>	
ASYMPTOTICALLY $I_\sigma$ -EQUIVALENCE OF SEQUENCES OF SETS .....	103
<i>Uğur ULUSU, Esra GÜLLE</i>	
GENERALIZED WEIGHTED STATISTICAL CONVERGENCE IN INTUITIONISTIC FUZZY NORMED LINEAR SPACES	104
<i>Selma ALTUNDAĞ, Esra KAMBER</i>	
OPERATOR IDEAL OF $S$ -TYPE OPERATORS USING WEIGHTED MEAN SEQUENCE SPACE .....	105
<i>Ezgi ERDOĞAN, Vatan KARAKAYA</i>	
ON EIGENVALUES AND EIGENFUNCTIONS OF A BOUNDARY VALUE PROBLEM WITH RETARDED ARGUMENT	106
<i>Khanlar R. MAMEDOV, F. Ayça ÇETİNKAYA</i>	
SOME MATRIX CHARACTERIZATIONS ON THE SERIES SPACE $Np\theta\mu$ AND APPLICATIONS.....	107
<i>Fadime GÖKÇE, Mehmet Ali SARIGÖL</i>	
ON THE ONE SUFFICIENT CONDITION FOR SHARP ESTIMATION OF ORTHONORMAL POLYNOMIALS OVER A CONTOUR OF THE COMPLEX PLANE .....	108
<i>Fahreddin ABDULLAYEV, Gülnare ABDULLAYEV</i>	
WEAK $w_2$ –STABILITY AND DATA DEPENDENCY OF MANN ITERATIVE SCHEME OF STRONGLY DEMICONTRACTIVE OPERATORS.....	109
<i>Faik GÜRSOY</i>	
APPROX. FIXED POINTS OF ALMOST CONTRACTIONS BY A SIMPLER AND FASTER ITERATIVE SCHEME .....	110
<i>Faik GÜRSOY, Vatan KARAKAYA, Kadri DOĞAN</i>	

A GENERALIZATION OF SOME MIXED NORM SPACES .....	111
<i>Faruk ÖZGER, Eberhard MALKOWSKY</i>	
MATRICIALLY DERIVED SOLID BANACH SEQUENCE SPACES .....	112
<i>Faruk POLAT</i>	
BOUNDEDNESS OF FRACTIONAL MAXIMAL OPERATOR ON GENERALIZED ORLICZ-MORREY SPACES .....	112
<i>Fatih DERİNGÖZ</i>	
ON ONE KIND OF POSITIVE OPERATORSIN LEBESGUE SPACE OF HARMONIC FUNCTIONS .....	113
<i>Fatih SIRIN, Yusuf ZEREN</i>	
NUMERICAL RECKONING COINCIDENCE POINTS OF NONSELF MAPPINGS VIA A JUNGK-MODIFIED SP ITERATIVE METHOD .....	114
<i>Fatma ÖZTÜRK ÇELİKER</i>	
COMMON FIXED POINT THEOREMS FOR WEAKLY COMPATIBLE MAPPINGS, EMPLOYING AN IMPLICIT RELATION WITH COMPLEX COEFFICIENTSON COMPLEX VALUED METRIC SPACE .....	115
<i>Fayyaz ROUZKARD</i>	
RESTORATION OF DEGRADED FACE IMAGE USING NON LINEAR DIFFERENTIAL EQUATION FOR .....	116
<i>Fella BERRIMI, Khier BENMAHAMMED</i>	
CHARACTERIZATION OF THREE DIMENSIONAL CELLULAR AUTOMATA WITH PERIODIC BOUNDARY .....	117
<i>Ferhat ŞAH, Hasan AKIN Fatih TAŞÇI</i>	
NUMERICAL APPROACH TO SOLVE SINGULAR INTEGRO-DIFFERENTIAL EQUATIONS USING TAYLOR SERIES EXPANSION .....	118
<i>FernaneKHAIREDDINE, EllaggouneFATEH</i>	
EXTRAGRADIENT METHODFOR SOLVING EQUILIBRIUM PROBLEM IN BANACHSPACES .....	119
<i>Zeynab JOUYMANDI, Fridoun MORADLOU</i>	
NUMERICAL INTEGRATION VIA SPARSE GRIDQUASI-INTERPOLATION WITH GAUSSIANS .....	120
<i>Fuat USTA, Jeremy LEVESLEY</i>	
USING KERNEL BASED METHODS FOR NEW TYPE CONFORMABLE ODE PROBLEMS .....	121
<i>Fuat USTA</i>	
AN EXISTENCE THEOREM OF MULTIPLE POSITIVE SOLUTIONS TO SEMIPOSITONE BOUNDARY VALUE PROBLEMS .....	122
<i>Fulya YÖRÜK DEREN, Nüket AYKUT HAMAL, Tuğba ŞENLİK ÇERDİK</i>	
GENERALIZED ABSOLUTE CESÀRO SUMMABILITY SPACES AND MATRIX OPERATORS .....	123
<i>G. CananHAZAR, M. Alisarigöl</i>	
A NEW ITERATIVE ALGORITHM FOR QUASI BREGMAN NOEXPANSINE MAPPINGS .....	124
<i>G. ZAMANI ESKANDANIAND M. RAEISI</i>	
APPROXIMATE SOLUTIONS OF DELAY PSEUDO-PARABOLIC EQUATIONS .....	125
<i>Gabil M. AMIRALIYEV, İlham AMIRALI</i>	
SOME IDENTITIES OF THE HUMBERT AND GENERALIZED CHEBYSHEV POLYNOMIALS .....	126
<i>Gulsah OZDEMIR, Yılmaz SIMSEK</i>	
A NEW SMOOTHING METHOD VIA BEZIER CURVE FOR NON-SMOOTH FUNCTIONS .....	127
<i>Ahmet ŞAHİNER, Gülden KAPUSUZ, Nurullah YILMAZ</i>	
VIABILITY PROBLEM FOR SECOND ORDER DIFFERENTIAL INCLUSIONS .....	128
<i>Gülseren ÇİÇEK, Elimhan MAHMUDOV</i>	
IDENTITIES ON THE $\varepsilon A_n$ , 1-INTEGRAL TRANSFORM .....	129
<i>A. Neşe DERNEK, Gülşen MENSİMLİ</i>	
ON THE PARANORMED TAYLOR SEQUENCE SPACES .....	130
<i>SerkanDEMİRİZ, Hacer Bilgin ELLİDOKUZOĞLU</i>	

ON THE TAYLOR SEQUENCESPACES OF NON-ABSOLUTE TYPE WHICH INCLUDE THE SPACES $\ell_p$ AND $\ell_\infty$ : ( $1 \leq p < \infty$ ).....	131
<i>Hacer Bilgin ELLİDOKUZOĞLU, Serkan DEMİRİZ</i>	
LACUNARY STATISTICAL CONVERGENCE OF ORDER $\alpha, \beta$ AND STRONG $N\alpha\beta\theta, p$ –SUMMABILITY .....	132
<i>Hacer ŞENGÜL</i>	
LACUNARY STATISTICAL CONVERGENCE OF ORDER $\alpha, \beta$ IN TOPOLOGICAL GROUPS.....	133
<i>HacerŞENGÜL, Mikail ET</i>	
$A^I$ –STATISTICAL CONVERGENCE OF ORDER $\alpha$ ( $0 < \alpha < 1$ ).....	134
<i>Hafize GÜMÜŞ</i>	
A NUMERICAL ANALYSIS FOR SOLUTION OF DIFFERENTIAL EQUATIONS USING THE COMPLEMENTARY FUNCTIONS METHOD .....	135
<i>Hakan PEKEL</i>	
PERFORMANCE ANALYSIS OF STOCHASTIC BEAM AND VARIABLE NEIGHBORHOOD SEARCH UNDER PARTIALLY SHADED PHOTOVOLTAIC SYSTEMS.....	136
<i>Zehan KESILMIŞ, Halil EROL , Mahmut UÇMAN</i>	
A STUDY ON ABSOLUTE ALMOST CONVERGENCE .....	137
<i>Hamdullah ŞEVLİ, Büşra BALKAŞ</i>	
COMPOSITION OPERATORS ON WEIGHTED BESOV SPACES .....	138
<i>Hamid VAEZI, Ebrahim ZAMANI</i>	
IMPROVING THE CONVERGENCE ORDER OF THE REGULARIZATION METHOD FOR FREDHOLM INTEGRAL EQUATIONS OF THE SECOND KIND .....	139
<i>Hamza GUEBBAL, Sami SEGNI</i>	
EULER SUMMABILITY KIND VARIOUS CONVERGENCE OF SETS.....	140
<i>Harun POLAT</i>	
GIBBS MEASURES FOR THE POTTS-SOS MODEL WITH FOUR STATES ON CAYLEY TREE OF ORDER ARBITRARY.....	141
<i>Halit SAYGILI, Hasan AKIN</i>	
BOUNDEDNESS OF THE CALDERON-ZYGMUND SINGULAR INTEGRAL OPERATOR AND ITS COMMUTATORS ON MODIFIED MORREY SPACES .....	142
<i>HaticeARMUTCU, Yusuf ZEREN, Vagif S. GULIYEV</i>	
ON WEIGHTED IYENGAR TYPE INEQUALITIES FOR CONFORMABLE FRACTIONAL INTEGRALS .....	143
<i>M. Zeki SARIKAYA, Hatice YALDIZ</i>	
ON TRIGONOMETRIC APPROXIMATION BY DEFERRED-NÖRLUND ( $D.N_p$ ) MEANS IN LIP CLASS.....	144
<i>Hilal BAYINDIR, UğurDEĞER</i>	
EXPONENT OF CONVERGENCE OF SOLUTIONS OF CERTAIN LINEAR DIFFERENTIAL EQUATIONS IN THE DISC..	145
<i>Houari FETTOUCH</i>	
COUPLED COINCIDENCE POINT THEOREMS FOR A GENERALIZED COMPATIBLE IN PARTIALLY M. S.....	146
<i>Hukmi KIZILTUNC, Esra YOLACAN</i>	
A VARIATION ON HALF CAUCHY SEQUENCES.....	147
<i>Huseyin ÇAKALLI</i>	
A VARIATION ON LACUNARY STATISTICAL QUASI CAUCHY SEQUENCES.....	148
<i>Huseyin ÇAKALLI, Huseyin KAPLAN</i>	
ON COMPUTING THE AVERAGE LOWER DOMINATION NUMBERS OF SOME TREES .....	149
<i>Hüseyin AKSAN, Tufan TURACI</i>	
THE AVERAGED MODULUS OF SMOOTHNESS AND ONE SIDED APPROXIMATION IN ORLICZ SPACES .....	150
<i>Hüseyin KOÇ</i>	
ON THE PARAMETERIZED SINGULARLY PERTURBED BOUNDARY VALUE PROBLEMS .....	151
<i>İlhame AMIRALI, Gabil M. AMIRALIYEV</i>	

OPERATIONS ON $B^{\wedge}(-1)$ -CONVEX SETS AND $B^{\wedge}(-1)$ -CONVEX FUNCTIONS .....	152
<i>Gabil ADILOV, İlknur YESILCE</i>	
SOME SPECIAL NUMBERS AND POLYNOMIALS RELATED TO K-ARY LYNDON WORDS .....	153
<i>Irem KUCUKOGLU, Yilmaz SIMSEK</i>	
A NEW ITERATION SCHEME FOR A HYBRID PAIR OF NONEXPANSIVE MAPPINGS .....	154
<i>Izhar UDDIN</i>	
TAUBERIAN THEOREMS FOR WEIGHTED MEANS OF DOUBLE SEQUENCES OF FUZZY NUMBERS .....	155
<i>Ümit TOTUR, İbrahim ÇANAK</i>	
SPECTRAL SINGULARITIES OF THE IMPULSIVE STURM LIOUVILLE OPERATORS ON THE SEMI AXIS .....	156
<i>İbrahim ERDAL, Şeyhmus YARDIMCI</i>	
NORM INEQUALITIES FOR A PARTICULAR CLASS OF MATRICES .....	157
<i>İbrahim Halil GÜMÜŞ, Omar HİRZALLAH, Fuad KİTTANEH</i>	
ZWEIER SUPER BANACH SPACES .....	158
<i>İbrahim ŞANLIBABA</i>	
AN OPTIMAL MULTIPLE SWITCHING PROBLEM UNDER WEAK ASSUMPTIONS .....	159
<i>İmen HASSAIRI</i>	
ROBIN BOUNDARY VALUE PROBLEM FOR THE BELTRAMI EQUATION .....	160
<i>İlker GENÇTÜRK, Kerim KOCA</i>	
A SIMPLE APPROACH TO THE SOLUTION OF SPECIAL STRUCTURED NONHOMOGENEOUS HIGHER ORDER LINEAR DIFFERENTIAL EQUATIONS WITH CONSTANT COEFFICIENTS .....	161
<i>İnayet DERİN, Yakup HAMEŞ</i>	
ON SOME PROPERTIES OF VECTOR-VALUED WEIGHTED VARIABLE EXPONENT SOBOLEV SPACES .....	162
<i>İsmail AYDIN</i>	
EDGE OPERATIONS IN GRAPHS AND ZAGREB INDICES .....	163
<i>İsmail Naci CANGUL, Aysun YURTTAS, Muge TOGAN, Ahmet Sinan CEVIK</i>	
INITIAL TIME DIFFERENCE GENERALIZED MONOTONE ITERATIVE TECHNIQUE UNIFIED BY THE UPPER AND LOWER SOLUTIONS .....	164
<i>İsmet ARSLAN, Coşkun YAKAR, Muhammed ÇİÇEK</i>	
ON NONLINEAR BOUNDARY VALUE PROBLEM .....	165
<i>Janpou NEE</i>	
UNIFIED RELATION-THEORETIC METRICAL FIXED POINT THEOREMS UNDER AN IMPLICIT CONTRACTIVE CONDITION WITH AN APPLICATION .....	166
<i>Md. AHMADULLAH, Javid ALI, M. IMDAD</i>	
PARAMETRIC ORDERED GENERALIZED VARIATIONAL INCLUSIONS INVOLVING NODSM MAPPINGS .....	167
<i>Javid IQBAL, Rais AHMAD</i>	
ON SOMERESULTOF NEW THREE-STEP ITERATION PROCESS ON THE CONVEX METRIC SPACES .....	167
<i>Kadri DOĞAN, Yilmaz ALTUN</i>	
ON THE CONVERGENGE RESULTOF NEW THREE-STEP ITERATION PROCESS ON THE GENERALIZED BANACH SPACES .....	168
<i>Kadri DOĞAN, Vatan KARAKAYA, Faik GÜRSOY</i>	
BACKWARD SOBOLEV TYPE FRACTIONAL STOCHASTIC EVOLUTION EQUATIONS IN HILBERT SPACES .....	168
<i>Kerboua MOURAD</i>	
Q- GREEN'S FORMULA ON THE COMPLEX PLANE IN THE SENSE OF HARMAN .....	169
<i>Kerim KOCA, İlker GENÇTÜRK, Mustafa AYDIN</i>	
BERNOULLI MATRIX-COLLOCATION METHOD FOR SOLVING GENERAL FUNCTIONAL INTEGRO-DIFFERENTIAL EQUATIONS WITH HYBRID DELAYS .....	170
<i>Kübra ERDEM BİÇER, Mehmet SEZER</i>	

A NEW UNIDIMENSIONAL BISECTION METHOD FOR GLOBAL OPTIMIZATION .....	171
<i>Lakhdar CHITER, Abdelmalek KOUADRI</i>	
COMPACTNESS OF MAXIMAL OPERATOR IN WEIGHTED LEBESGUE SPACES WITH VARIABLE EXPONENT .....	172
<i>Lutfi AKIN, Yusuf ZEREN</i>	
FIXED POINT THEOREMS FOR INTEGRAL TYPE MAPPINGS IN BANACH SPACE .....	173
<i>M. Abdussamed MALDAR, Vatan KARAKAYA</i>	
STATISTICALLY CONVERGENCE OF SEQUENCES OF FUZZY NUMBERS BY A MODULUS FUNCTION .....	174
<i>Mahmut IŞIK</i>	
ON SOME INVARIANT SEQUENCE SPACES.....	175
<i>Mahmut KARAKUŞ</i>	
ON SOLIDNESS OF SEQUENCE SPACES .....	176
<i>Mahmut KARAKUŞ</i>	
THREE-STEP ITERATIVE SCHEME FOR APPROXIMATING FIXEDPOINTS OF MULTIVALUED NONEXPANSIVE MAPPINGS .....	177
<i>Makbule KAPLAN</i>	
INVERSE SPECTRAL AND INVERSE NODAL PROBLEMS FOR STRUM-LIOUVILLE EQUATIONS WITH POINT $\delta'$ -INTERACTION.....	178
<i>Manaf MANAFOV</i>	
LOG-CONVEXITY OF WEIGHTED AREA INTEGRAL MEANS OF MONOMIALS ON THE UNIT DISK .....	179
<i>Martin At. STANEV</i>	
POROSITY LIMIT AND CLUSTER POINTS OF REAL VALUED SEQUENCES.....	180
<i>Maya ALTINOK, Mehmet KÜÇÜKASLAN</i>	
RELATION-THEORETIC METRICAL FIXED POINT THEOREMS UNDER NONLINEAR CONTRACTIONS.....	181
<i>Md AHMADULLAH, Mohammad IMDAD, Rqeeb GUBRAN</i>	
STEADY-STATE SKELETON OF THE 3D POINT CLOUDS VIA QUANTUM GRAPHS .....	182
<i>Mehmet Ali BALCI, Ömer AKGÜLLER</i>	
NUMERICAL SOLUTION OF A SINGULARLY PERTURBED PROBLEM BY USING HYBRIDIZABLE DISCONTINUOUS GALERKIN METHOD .....	183
<i>Mehmet Fatih KARAASLAN</i>	
THE DYNAMICS OF POSITIVE SOLUTIONS OF A HIGHER ORDER DIFFERENCE EQUATION WITH ARBITRARY POWERS AND DELAYS .....	184
<i>Mehmet GÜMÜŞ, Yüksel SOYKAN</i>	
NUMERICAL SOLUTION OF NONLINEAR FRACTIONAL-INTEGRO DIFFERENTIAL EQUATIONS AND SYSTEMS..	185
<i>Mehmet ŞENOL</i>	
FIXED POINTS FOR SOME MULTIVALUED MAPPING IN $G_p$ – METRIC SPACES.....	186
<i>Melek Kübra AYHAN, Cafer AYDIN</i>	
FIXED POINT THEOREMS FOR EXPANSIVE MAPPINGS IN $G_p$ -METRIC SPACES.....	187
<i>Meltem KAYA, Hasan FURKAN</i>	
SOME PROPERTIES OF GENERALIZED METRIC SPACES.....	188
<i>Merve İLKHAN, Emrah Evren KARA</i>	
ON RIESZ SECTIONS IN SEQUENCE SPACES.....	189
<i>Merve TEMİZER ERSOY, Hasan FURKAN, Bilal ALTAY</i>	
STABILITY AND CONVERGENCE ANALYSIS OF THE FINITE ELEMENT DISCRETIZATION OF THE NAVIER-STOKES-TIME-FILTERING REGULARIZATION .....	190
<i>Osman Raşit IŞIK, Meryem ÖZBUNAR</i>	
INVERSE NODAL PROBLEM FOR P-LAPLACIAN BESSEL EQUATION .....	191
<i>Mesut COŞKUN, Hikmet KEMALOĞLU</i>	

ON WIJSMAN ASYMPTOTICALLY DEFERRED STATISTICAL EQUIVALENT OF SEQUENCES .....	192
<i>Mikail ET</i>	
NECESSARY CONDITIONS AND SUFFICIENT CONDITIONS FOR NONEXISTENCE RESULTS TO CERTAIN EVOLUTION EQUATION .....	193
<i>Mohamed BERBICHE</i>	
ANALYTICAL SOLUTION OF A CLASS OF NONLINEAR VOLTERRA INTEGRAL EQUATIONS USING VARIATIONAL ITERATION METHOD .....	194
<i>Mohammed S. MECHEE, RaadM. KADUM</i>	
A NOTE ON PROPERTIES THAT IMPLY THE FIXED POINT PROPERTY .....	195
<i>Mohammad KNEFATI, Vatan KARAKAYA</i>	
INTEGRAL TYPE ALMOST CONTRACTION MAPPINGS IN METRIC SPACES.....	196
<i>M. Abdussamed MALDAR, Vatan KARAKAYA</i>	
MAXIMUM NORM ANALYSIS OF SCHWARZ METHOD FOR ELLIPTIC QUASI-VARIATIONAL EQUALITIES .....	197
<i>Mohammed BEGGAS, Mohamed HAIOUR</i>	
VARIATION DIMINISHING INTEGRAL OPERATORS OF THE CONVOLUTIONS TYPE ASSOCIATED WITH THE DUNKL OPERATOR ON $\mathbb{R}$ .....	198
<i>Moncef DZIRI</i>	
PERTURBED PARTIAL FRACTIONAL ORDER FUNCTIONAL DIFFERENTIAL EQUATIONS WITH INFINITE DELAY IN FRECHET SPACES.....	198
<i>Mouffak BENCHOHA, Mohamed HELLAL</i>	
ON SHERMAN'S INEQUALITY.....	199
<i>Muhammad Adil KHAN</i>	
ON GENERALIZED DIFFERENCE SEQUENCES OF FUNCTIONS .....	199
<i>Muhammed ÇINAR, Mikail ET</i>	
INVERSE SOURCE PROBLEM FOR TIME-FRACTIONAL HEAT EQUATION WITH A GENERALIZED IMPEDANCE BOUNDARY CONDITION.....	200
<i>Muhammed ÇİÇEK, Mansur İSGENDEROĞLU (ISMAILOV)</i>	
A HYBRIDIZABLE DISCONTINUOUS GALERKIN METHOD FOR A CLASS OF FRACTIONAL BOUNDARY VALUE PROBLEM.....	201
<i>Mehmet Fatih KARAASLAN, Muhammet KURULAY</i>	
OSTROWSKI TYPE INEQUALITIES FOR GENERALIZED $s$ -CONVEX FUNCTIONS IN THE SECOND SENSE .....	202
<i>Muharrem TOMAR, Erhan SET</i>	
ON $I$ -CONVERGENCE OF SEQUENCES OF FUNCTIONS IN 2-NORMED SPACES .....	203
<i>Mukaddes ARSLAN, Erdinç DÜNDAR</i>	
DEFECT-DEFERRED CORRECTION METHOD FOR A FLUID FLOW AT HIGH REYNOLDS NUMBERS .....	203
<i>Mustafa AGGUL</i>	
ALMOST CONVERGENCE METHOD WITH FRACTIONAL ORDER OPERATOR.....	204
<i>Murat KİRİŞÇİ</i>	
ON SOME FIXED POINT THEOREMS WITH GENERALIZED CONTRACTIONS IN COMPLETE CONE METRIC SPACE ENDOWED WITH A PARTIAL ORDER AND INVOLVING A GRAPH .....	205
<i>Murat CANCAN</i>	
DISCUSSION ON ADVECTION-DIFFUSION EQUATION THROUGH FINITE DIFFERENCE SCHEMES .....	206
<i>Murat SARI, Lamia J.M. Al-MASHHADANI, Arshed A. AHMAD</i>	
THE GENERATING FUNCTIONS FOR THE FAMILY OF THE GENERALIZED BERNOULLI POLYNOMIALS .....	207
<i>Mustafa ALKAN</i>	
TWO NEW PROOFS OF GENERALIZED BIPERIODIC FIBONACCI IDENTITY IN TERMS OF THE DETERMINANTS OF TRIDIAGONAL MATRIX.....	207
<i>Yasin YAZLIK, Musa BAŞBÜK</i>	



SOME NOTES ON THE SEQUENCE SPACES $l_{p\lambda} G_m$ AND $l_{\infty\lambda} G_m$ .....	208
<i>Mustafa Cemil Bişgin, Abdulcabbar SÖNMEZ</i>	
A PARAMETERIZED SINGULARLY PERTURBED BOUNDARY VALUE PROBLEM .....	209
<i>Mustafa KUDU, Gabil M. AMIRALIYEV</i>	
P-ADIC GIBBS MEASURES FOR THEISING-VANNIMENUS MODEL ON CAYLEY TREE OF ORDER THREE.....	210
<i>Mutlay DOĞAN, Hasan AKIN</i>	
AN EXISTENCE THEOREM FOR ANALYTIC SOLUTION OF A FRACTIONAL DIFFERENTIAL EQUATION WITH CAPUTO DERIVATIVE .....	211
<i>Müfit ŞAN</i>	
SOME CONVERGENCE AND DATA DEPENDENCE RESULTS IN A GENERAL CLASS OF CONTRACTIVE TYPE OPERATORS .....	212
<i>Müzeyyen ERTÜRK, Vatan KARAKAYA</i>	
INTEGRABLE SOLUTIONS OF A NONLINEAR INTEGRAL EQUATION VIA SCHAEFER-KRASNOSELSKII FIXED POINT THEOREM .....	212
<i>N.ABADA, L. AITKAKI</i>	
A FIXED POINT PROOF OF THE CONVERGENCE OF A NEWTON-LIKE METHOD OBTAINED BY THE NORMAL S- ITERATION PROCESS .....	213
<i>Nazli KARACA, İsa YILDIRIM</i>	
A REARRANGEMENT ESTIMATE FOR THE GENERALIZED MULTILINEAR ANISOTROPIC FRACTIONAL INTEG. ..	213
<i>Nezrin GADIROVA</i>	
CALSESSES OF I-CONVERGENTDOUBLE SEQUENCES OVER N-NORMED SPACES .....	214
<i>Nazneen KHAN</i>	
ON SOME GEOMETRICAL PROPERTIES.....	215
<i>Necip ŞİMŞEK, Zhamile ASKEROVA</i>	
AVERAGE VECTOR FIELD METHOD AND CAPUTO FRACTIONAL DERIVATIVE DEFINITION FOR LINEAR FRACTIONAL SCHRÖDINGER EQUATION.....	216
<i>Neslihan Fatma Er, Canan Akkoyunlu, Hikmet Çağlar</i>	
SOME CONTRACTIONS AND FIXED POINT THEOREMS IN MODULAR METRIC SPACES .....	217
<i>Duran TÜRKÖĞLU, Nesrin MANAV</i>	
ALGORITHM FOR ZEROS OF MAXIMAL MONOTONE MAPPINGS IN CLASSICAL BANACH SPACES .....	218
<i>A. H. ADOUM, O. DIOP, M. SENE, N. DJITTE</i>	
SPECTRAL ANALYSIS OF MATRIX STURM-LIOUVILLE OPERATORS.....	219
<i>Nihal YOKUS, Nimet COSKUN</i>	
NEW RESULTS ON GRAPH PRODUCT OF SPECIAL SEMIGROUPS .....	220
<i>Nihat AKGÜNEŞ</i>	
PRINCIPAL FUNCTIONS OF DISCRETE STURM-LIOUVILLE EQUATIONS WITH HYPERBOLIC EIGENPARAMETER	221
<i>Nihal YOKUS, Nimet COSKUN</i>	
WIJSMAN I-INVARIANT CONVERGENCE OF SEQUENCES OF SETS .....	222
<i>Nimet PANCAROĞLU AKIN, Erdinç DÜNDAR, Fatih NURAY</i>	
ON NEW FIXED POINTS THEOREMS FOR SET CONTRACTION MULTIVALUED MAPPINGS AND APPLICATIONS TO DIFFERENTIAL INCLUSIONS.....	222
<i>Nour El Houda BOUZARA, Vatan KARAKAYA</i>	
APPLYING POWELL'S SYMMETRICAL TECHNIQUE TO CONJUGATE GRADIENT METHODS WITH THE GENERALIZED CONJUGACY CONDITION .....	223
<i>Noureddine BENRABIA</i>	
CONVERGENCE OF SPLIT-STEP FOURIER COLLOCATION METHOD FOR BENJAMIN-BONA-MAHONY TYPE EQUATIONS .....	224
<i>Nurcan GÜCÜYENEN</i>	

HERMIT-HADAMARD TYPE INEQUALITIES FOR CO-ORDINATES LOG-CONVEX STOCHASTIC PROCESSES.....	225
<i>Nurgül OKUR BEKAR</i>	
A NEW SMOOTHING APPROXIMATION TO PIECEWISE SMOOTH FUNCTIONS AND APPLICATIONS.....	226
<i>Nurullah YILMAZ, Ahmet ŞAHİNER</i>	
ON THE A FAMILY SAVING MODEL .....	227
<i>Olgun CABRİ, Khanlar R. MAMEDOV</i>	
CONVERGENCE ANALYSIS OF DIFFERENCE METHOD FOR VOLTERRA DELAY-INTEGRO-DIFFERENTIAL EQUATION .....	228
<i>Gabil M. AMIRALIYEV, Ömer YAPMAN</i>	
A GENERALIZATION OF THE EXP. AND LINDLEY DISTRIBUTIONS VIA THE KUMARASWAMY-G FAMILY .....	229
<i>Orhan Mazlum YAZAR, Mustafa Ç. KORKMAZ</i>	
CONVERGENCE THEOREMS FOR A FAMILY OF MULTIVALUED NONEXPANSIVE MAPPINGS IN HYPERBOLIC SPACES.....	230
<i>Osman ALAGÖZ, Birol GÜNDÜZ, Sezgin AKBULUT</i>	
COMPLETE ABSTRACT DIFFERENTIAL EQUATIONS OF ELLIPTIC TYPE WITH ROBIN'S CONDITION IN A NON-COMMUTATIVE FRAMEWORK.....	231
<i>Ould Melha KHELLAF, Mustapha CHEGGAG, Stéphane MAINGOT, Rabah LABBAS</i>	
EXTREMAL FUNCTIONS FOR STARLIKE FUNCTIONS AND CONVEX FUNCTIONS .....	232
<i>İsmet YILDIZ, Neslihan ZORLU, Oya MERT</i>	
DYNAMIC SEMI-DISCRETE SURFACES OF REVOLUTION .....	233
<i>Sibel PAŞALI ATMACA, Ömer AKGÜLLER, Emel KARACA</i>	
ON SOME PROPERTIES OF POISSON AND CAUCHY TYPE INTEGRALS IN WEIGHTED MORREY TYPE SPACES ...	234
<i>Şeyma ÇETİN, Yusuf ZEREN</i>	
ON $I_2$ -ASYMPTOTICALLY $\lambda^2$ -STATISTICAL EQUIVALENT DOUBLE SET SEQUENCES.....	235
<i>Ömer KİŞİ, Semra SARAÇOĞLU ÇELİK, Erhan GÜLER</i>	
ON THE ALMOST EVERYWHERE STATISTICAL CONVERGENCE OF SEQUENCES OF FUZZY NUMBERS .....	235
<i>Özer TALO</i>	
DYNAMICS OF A DISCRETE-TIME HOST PARASITOID .....	236
<i>Özlem AK GÜMÜŞ</i>	
STABILITY BEHAVIOR OF A MODIFIED NICHOLSON-BAILEY MODEL.....	237
<i>Özlem AK GÜMÜŞ</i>	
ON P-ADIC GAMMA FUNCTION .....	238
<i>Özge ÇOLAKOĞLU HAVARE, Hamza MENKEN</i>	
APPROXIMATION PROPERTIES OF KING TYPE (p,q)-BERNSTEIN OPERATORS .....	239
<i>Özge DALMANOĞLU, Mediha ÖRKÜ</i>	
ON THE NUMERICAL SOLUTION OF THE KLEIN-GORDON EQUATION BY EXPONENTIAL B-SPLINE COLLOCATION METHOD .....	240
<i>Özlem ERSOY HEPSON, Alper KORKMAZ, İdris DAĞ</i>	
SOLVING LINEAR FRACTIONAL EQUATIONS WITH CONSTANT COEFFICIENTS USING LAPLACE TRANSFORM METHOD UNDER CTIT TRANSFORMATION .....	241
<i>Özlem ÖZTÜRK MIZRAK</i>	
THE SPACE $W(Lp(.), Q(.), L\Omega r)$ AND BOUNDEDNESS OF THE HARDY-LITTLEWOOD MAXIMAL FUNCTION ON $W(Lp(.), Q(.), L\Omega r)$ .....	242
<i>Öznur KULAK, A. Turan GÜRKANLI</i>	
ON THE GROWTH RATE OF ALGEBRAIC POLYNOMIALS THROUGH THEIR NORM IN BERGMAN SPACE .....	243
<i>Pelin ÖZKARTEPE, Fahreddin ABDULLAYEV</i>	
DELAY DIFFERENTIAL OPERATORS AND SOME SOLVABLE MODELS IN LIFE SCIENCES .....	244
<i>Pembe İPEK, Bülent YILMAZ</i>	

STATISTICALLY RELATIVELY A-SUMMABILITY OF CONVERGENCE OF DOUBLE SEQUENCES OF POSITIVE LINEAR OPERATORS .....	245
<i>Pınar OKÇU, Fadime DIRİK</i>	
SOME SPECTRAL PROPERTIES OF LINEAR OPERATORS ON EXOTIC BANACH SPACES.....	246
<i>Rabah DEBBAR</i>	
SUPPORT VECTOR MACHINES SVM.....	247
<i>Rachid BELGACEM, Abdessamad AMIR</i>	
CHARACTERIZATION OF MIXED MODULUS OF SMOOTHNESS IN WEIGHTED $L_p$ SPACES .....	248
<i>Ramazan AKGÜN</i>	
SOME DIRECT APPROXIMATION THEOREMS IN WEIGHTED ORLICZ SPACES.....	249
<i>Ramazan ÇETİNTAŞ</i>	
UNCONDITIONALLY CAUCHY SERIES AND ZEWIER MATRIX METHOD.....	250
<i>Ramazan KAMA, Bilal ALTAY</i>	
TAUBERIAN CONDITIONS FOR DOUBLE SEQUENCES WHICH ARE STATISTICALLY SUMMABLE $(C,1,1)$ IN FUZZY NUMBER SPACE .....	251
<i>Reha YAPALI, Ozer TALO</i>	
THE REALIZATION OF THE FEEDBACK AMPLIFIER DESIGN WITH USING ARTIFICIAL NEURAL NETWORK.....	252
<i>Remzi TUNTAS</i>	
PREDICTION OF HARDNESS VALUES OF COLD WORKED $Al/SiC_p$ COMPOSITE AT DIFFERENT REDUCTION RATIO BY ADAPTIVE NEURO-FUZZY INFERENCE SYSTEM.....	253
<i>Remzi TUNTAS, Burak DİKİCİ</i>	
DIFFERENCE SEQUENCE SPACES AND MATRIX TRANSFORMATIONS OF SOME BILATERAL SEQUENCES .....	254
<i>Rıdvan Cem DEMİRKOL, Harun POLAT</i>	
TWO-WEIGHTED INEQUALITIES FOR MULTIDIMENSIONAL HARDY OPERATOR IN VARIABLE WEIGHTED LEBESGUE SPACES WITH MIXED NORM.....	255
<i>R. A. BANDALIYEV, S. G. HASANOV</i>	
GROWTH OF SOLUTIONS OF LINEAR DIFFERENTIAL EQUATIONS AROUND AN ISOLATED ESSENTIAL SINGULARITY .....	256
<i>Saada HAMOUDA</i>	
ALGEBRAIC PROPERTIES OF JOIN AND CORONA PRODUCT OF GRAPHS .....	257
<i>Sadık DELEN, İsmail Naci CANGUL</i>	
COMMON FIXED POINT THEOREMS FOR WEAKLY SUBSEQUENTIALLY CONTINUOUS MAPS IN MODIFIED INTUITIONISTIC METRIC SPACES .....	258
<i>Said BELOUL</i>	
EXPONENTIAL STABILITY OF SOME NEURAL NETWORK SYSTEMS OF COHEN-GROSSBERG TYPE .....	259
<i>Said MAZOUZI</i>	
EXACT SOLUTIONS AND CONSERVATION LAWS OF 3+1 DIMENSIONAL YTSF EQUATION .....	260
<i>Sait SAN</i>	
GENERALIZED RESULT OF GLOBAL SOLUTIONS TO A CLASS OF A REACTION-DIFFUSION SYSTEM .....	261
<i>Salah BADRAOUI</i>	
A MODIFIED REGULARIZATION METHOD FOR A NON- LINEAR ABSTRACT PARABOLIC EQUATION .....	262
<i>Salah DJEZZAR, Roumaissa BENMARAİ</i>	
ASYMPTOTIC BEHAVIOR OF WEAKLY COUPLED THERMOELASTIC WAVE MODEL .....	263
<i>Salem NAFİRİ</i>	
ON THE CONVERGENCE FOR A SEQUENCE OF INTERVALS OF FUZZY NUMBERS .....	263
<i>Salih AYTAR</i>	
SOME INEQUALITIES FOR DOUBLE INTEGRALS AND APPLICATIONS FOR CUBATURE FORMULA .....	264
<i>Samet ERDEN, M. Zeki SARIKAYA</i>	

SOME PERTURBED INEQUALITIES OF OSTROWSKI TYPE FOR TWICE DIFFERENTIABLE FUNCTIONS .....	265
<i>Samet ERDEN, Hüseyin BUDAK, M. Zeki SARIKAYA</i>	
ON THE PALINDROMICS CONTINUED FRACTIONS IN THE FIELD $F_q((X^{-1}))$ .....	266
<i>Sana DRISS</i>	
CONVERGENCE THEOREMS FOR EQUILIBRIUM PROBLEMS AND GENERALIZED HYBRID MAPPINGS .....	266
<i>Sattar ALIZADEH, Fridoun MORADLOU</i>	
HYERS-ULAM-RASSIAS STABILITY OF A VOLTERRA INTEGRO-DIFFERENTIAL EQUATION .....	267
<i>Sebaheddin ŞEVGİN</i>	
APPROXIMATION PROPERTIES OF ANALYTIC FUNCTIONS BY THE SEQUENCES OF $\kappa$ -POSITIVE LINEAR OPERATORS IN SOME SUBSPACE OF ANALYTIC FUNCTIONS.....	268
<i>Tülin COŞKUN, Seda KARATEKE</i>	
HERMITE-HADAMARD AND SIMPSON-LIKE TYPE INEQUALITIES FOR DIFFERENTIABLE $p$ -QUASI-CONVEX FUNCTIONS.....	269
<i>İmdat İŞCAN, Sercan TURHAN, Selahattin MADEN</i>	
ON SOME EQUALITIES OF ORDINARY LEAST SQUARES AND BEST LINEAR UNBIASED ESTIMATORS UNDER A GENERAL PARTITIONED LINEAR MODEL.....	270
<i>Selahattin MADEN</i>	
SOME RESULTS ON THE GENERALIZED MELLIN TRANSFORMS AND APPLICATIONS .....	271
<i>Selcan KOCABAŞ, Ezgi ERDOĞAN, A. Neşe DERNEK</i>	
APPROXIMATE SOLUTION FOR SOLVING THE SINE-GORDON EQUATION BY REDUCED DIFFERENTIAL TRANSFORM METHOD WITH FIXED GRID SIZE.....	272
<i>Sema SERVÍ, Yıldıray KESKİN, Galip OTURANC</i>	
EULER SPIRALS .....	273
<i>Semra SARAÇOĞLU ÇELİK, Erhan GÜLER, Ömer KİŞİ</i>	
SIMPLE EQUATION METHOD FOR TRAVELING WAVESOLUTIONS OF SOME NONLINEAR PARTIAL DIFFERENTIAL EQUATIONS .....	273
<i>Serbay DURAN, Ibrahim E. INAN, Yavuz UĞURLU</i>	
ENTROPY CONVERGENCE FOR SEQUENCES OF FUZZY NUMBERS.....	274
<i>Sevda ATPINAR, Mehmet ŞENGÖNÜL</i>	
ENTROPY VALUE OF QRS COMPLEX IN THE ELECTROCARDIOGRAPHY .....	275
<i>Sevda ATPINAR, Mehmet ŞENOL</i>	
OPTIMIZATION OF HIGHER ORDER POLYHEDRAL DISCRETE AND DIFFERENTIAL INCLUSIONS.....	276
<i>Sevilay DEMİR, Elimhan MAHMUDOV</i>	
WEIGHTED APPROXIMATION BY NONLINEAR DOUBLE SINGULAR INTEGRAL OPERATORS .....	277
<i>Gumrah UYSAL, Sevilay KIRCI SERENBAY, Ertan İBIKLİ</i>	
ON STATISTICAL CONVERGENCE OF SEQUENCES OF FUNCTIONS IN 2-NORMED SPACES .....	278
<i>Sevim YEGÜL, Erdinç DÜNDAR</i>	
SOME DOUBLE SEQUENCE SPACES OF INTERVAL NUMBERS .....	279
<i>Sibel YASEMİN GÖLBOL, Uğur DEĞER, Ayhan ESİ</i>	
APPROXIMATING SOLUTIONS OF NONLINEAR ABSTRACT MEASURE DIFFERENTIAL EQUATIONS.....	280
<i>Sidheshwar BELLALE, Bapurao DHAGE</i>	
ON $\lambda$ -CONVERGENCE OF SECOND ORDER AND NEW BANACH SPACES.....	281
<i>Sinan ERCAN, Çiğdem A. BEKTAŞ</i>	
COMPARISON OF SOME SET OPEN AND UNIFORM TOPOLOGIES ON $C(X, Y)$ .....	282
<i>Smail KELAIAIA, Lamia HARKAT</i>	
SOLUTION OF A LINEAR MULTIOBJECTIVE PROBLEM BY THE ADAPTIVE METHOD .....	283
<i>Zohra Sabrina DELHOUM, Sonia RADJEF, Fatima BOUDAUD</i>	

GROUPS WHOSE PROPER SUBGROUPS ARE HYPERCENTRAL.....	284
<i>Souad AZRA, Nadir TRABELSI</i>	
SOLUTION OF FRACTIONAL ORDER ORDINARY DIFFERENTIAL EQUATION: A NUMERICAL APPROACH .....	284
<i>Soumen SHAW</i>	
ERROR ANALYSIS FOR EXTENDED DISCONTINUOUS GALERKIN(XDG) METHODS.....	285
<i>Suayip TOPRAKSEVEN</i>	
ON A $C^*$ - MODULE NORMED SPACE AND ITS TOPOLOGICAL PROPERTIES .....	286
<i>SUPAMA, Atok ZULIJANTO, Imam SOLEKHUDDIN, SUMARDI</i>	
NUMERICAL SOLUTIONS OF SINGULARLY PERTURBED TURNING POINT PROBLEMS EXHIBITING AN INTERIOR LAYER VIA MAGNUS SERIES EXPANSION METHOD .....	287
<i>Sure KÖME, Aytekin ERYILMAZ</i>	
ON GENERALIZATION ABSOLUTE RIESZ SUMMABILITY FACTORS OF FOURIER SERIES.....	288
<i>Hikmet Seyhan ÖZARSLAN, Şebnem YILDIZ</i>	
SPECTRAL SINGULARITIES OF IMPULSIVE DISCRETE DIRAC OPERATORS .....	289
<i>Şerifenur CEBESÖY, Elgiz BAIRAMOV, Şeyda SOLMAZ</i>	
FIXED POINT RESULTS FOR BERINDE-TYPE ALMOST CONTRACTIONS ON $G_p$ -METRIC SPACES.....	290
<i>Şeyma ÇEVİK, Hasan FURKAN</i>	
WIJSMAN $I_2$ -INVARIANT CONVERGENCE OF DOUBLE SEQUENCE OF SETS.....	291
<i>Şükrü TORTOP, Erdinç DÜNDAR</i>	
A PRIORI ESTIMATES OF SOLUTIONS BOUNDARY VALUE PROBLEMS FOR THE HIGHER ORDER ELLIPTIC EQUATIONS IN GENERALIZED MORREY SPACES.....	291
<i>Tahir GADJIEV, Shahla GALANDAROVA</i>	
TWO PARAMETRIC (P; Q)-STANCU-BETA OPERATORS AND THEIR APPROXIMATION PROPERTIES.....	292
<i>Taqseer KHAN</i>	
A COMPARISON OF FINITE-DIFFERENCE METHOD BY FIRST ORDER AND SECOND ORDER CENTRAL DIFFERENTIATION FORMULAS FOR LINEAR ODES UP TO FOURTH DEGREE AND A GENERALIZED CODE .....	293
<i>Tefaruk HAKTANIR, Hatice CITAKOGLU, Murat COBANER</i>	
MATHEMATICAL ANALYSIS OF LENGYEL-EPSTEIN MODEL BY FRACTIONAL-ORDER DIFFERENTIAL EQUATIONS SYSTEMS .....	294
<i>Teslima DAŞBAŞI, Bahatdin DAŞBAŞI</i>	
GLOBAL EXISTENCE AND BOUNDEDNESS OF SOLUTIONS FOR A TYPE OF NONLINEAR INTEGRO DIFFERENTIAL EQUATIONS OF THIRD ORDER .....	295
<i>Timur AYHAN</i>	
A NEW RESULT ON THE CONTINUABILITY AND BOUNDEDNESS OF SOLUTIONS TO A CLASS OF VECTOR DIFFERENTIAL EQUATIONS OF THIRD ORDER WITH DELAY.....	296
<i>Timur AYHAN</i>	
AN INVERSE NODAL PROBLEM TO CONSTRUCT COULOMB POTENTIAL FOR $p$ -LAPLACIAN STURM-LIOUVILLE EQUATION WITH POLYNOMIALLY BOUNDARY CONDITIONS.....	297
<i>Tuba GULSEN</i>	
SOME GENERAL RESULTS FOR THE AVERAGE LOWER 2-DOMINATION NUMBER OF GRAPHS.....	298
<i>Tufan TURACI</i>	
A NEW EFFECTIVE METHOD TO SOLVE NONLINEAR PARTIAL DIFFERENTIAL EQN.: THE UNIFIED METHOD....	299
<i>Şamil AKÇAĞIL, Tuğba AYDEMİR And Ömer Faruk GÖZÜKIZIL</i>	
THE MULTIDIMENSIONAL REVERSE HARDY-TYPE INEQUALITIES FOR SUPREMACIAL OPERATOR.....	300
<i>Rza MUSTAFAYEV, Tuğçe ÜNVER</i>	
ON STATISTICAL CONVERGENCE WITH RESPECT TO THE GEOMETRIC MEAN AND ITS APPLICATIONS TO APPROXIMATION THEOREMS.....	301
<i>Uğur KADAK, Feyzi BAŞAR</i>	

NECESSARY AND SUFFICIENT CONDITIONS FOR FIRSTORDER DIFFERENTIAL OPERATORS TO BE ASSOCIATED WITH A GENERALIZED CAUCHY-RIEMANN OPERATOR IN CLIFFORD ANALYSIS .....	302
<i>Uğur YÜKSEL</i>	
INVERSE NUMERICAL RADIUS INEQUALITY FOR REPRODUCING KERNEL HILBERT SPACE OPERATORS .....	303
<i>Ulaş YAMANCI, Mehmet GÜRDAL</i>	
SECOND-ORDER BOUNDARY VALUE PROBLEM ON A HALF-LINE .....	304
<i>Ummahan AKCAN, Erbil ÇETİN</i>	
PARABOLIC OBLIQUE DERIVATIVE PROBLEM WITH DISCONTINUOUS COEFFICIENTS IN GENERALIZED WEIGHTED MORREY SPACES .....	305
<i>V. S. GULIYEV, M. N. OMAROVA</i>	
FIXED POINT THEOREMS FOR MAPPINGS (E.A)-PROPERTY IN PARTIAL METRIC SPACE .....	306
<i>Vildan ÖZTÜRK, Duran TÜRKÖĞLU</i>	
RIESZ POTENTIAL IN GENERALIZED MORREY SPACES ON THE HEISENBERG GROUP .....	306
<i>Y.PELİN MAMMADO, V A. EROGLU</i>	
ON EXISTENCE AND CONVERGENCE THEOREMS FOR A NEW GENERAL NONLINEAR MAPPING ON CAT(0) SPACES.....	307
<i>Vatan KARAKAYA, Emirhan HACIOGLU, Yunus ATALAN</i>	
SOME THEOREMS ABOUT STATISTICAL CONVERGENCE ON TIME SCALES.....	308
<i>Yavuz ALTIN</i>	
AUTO-BÄCKLUND TRANSFORMATION FOR SOME NONLINEAR PARTIAL DIFFERENTIAL EQUATION .....	309
<i>Ibrahim E. INAN, Yavuz UĞURLU, Hasan BULUT</i>	
A NEW APPROACH TO FRACTIONAL $q$ -DIFFERENCE EQUATIONS AND THE $q$ -LAPLACE TRANSFORM .....	310
<i>Yavuz YAZICI, Umut Mutlu ÖZKAN</i>	
ON THE CONSTRUCTION OF GENERAL SOLUTION OF THE EQUATION $\partial w(z)\partial\phi(z) - 12\phi(z) - 1\lambda wz=0$ ...	311
<i>Yeşim SAĞLAM ÖZKAN, Sezayi HIZLIYEL</i>	
CENTRAL FACTORIAL TYPE NUMBERS ASSOCIATED WITH AVERAGING OPERATOR .....	312
<i>Yılmaz ŞİMŞEK</i>	
STABILITY OF NONLINEARVOLTERRA-FREDHOLM INTEGRO DIFFERENTIAL EQUATION:A FIXED POINT APPROACH.....	313
<i>Yunus ATALAN, Vatan KARAKAYA</i>	
ON STATISTICAL E-CONVERGENCE OF DOUBLE SEQUENCES .....	314
<i>Yurdal SEVER, Özer TALO</i>	
THE VARIATIONAL FORMULATION OF AN INVERSE PROBLEM FOR A PARABOLIC EQUATION .....	315
<i>Yusuf KOÇAK</i>	
COMPACTNESS OF FRACTIONAL MAXIMAL OPERATOR IN WEIGHTED $L^p(x)$ (0,l) SPACE .....	316
<i>Yusuf ZEREN, Lutfi AKIN</i>	
NEW SOLUTIONS OF THE SPACE-TIME FRACTIONAL SHARMA-TASSO-OLVER EQUATION WITH CONFORMABLE DERIVATIVE.....	317
<i>Yücel ÇENESİZ, Orkun TAŞBOZAN, Ali KURT, Olaniyi Samuel IYIOLA</i>	
NONCOMMUTATIVE SPACE AND 2D SCHRÖDINGER EQUATION WITH CENTRAL POTENTIAL .....	318
<i>Slimane ZAIM, Hakim GUELMAMENE</i>	
DETERMINING THE CENTER OF GRAVITY AND SIMILARITY MEASURES OF SEQUENCE SPACES OF TRIANGULAR FUZZY NUMBERS .....	319
<i>Zarife ZARARSIZ</i>	
OBTAINING MATHEMATICAL MODELS OF THE PIEZOELECTRIC SYNTHETIC JET .....	320
<i>Zeynep EKİCİOĞLU KÜZECİ, Celal Sami TÜFEKÇİ</i>	
LACUNARY $I\sigma$ -CONVERGENCE .....	321
<i>Uğur ULUSU, Fatih NURAY</i>	

EXISTENCE AND NONEXISTENCE FOR NONLINEAR PROBLEM.....	321
<i>B. ABDELLAOUI, K. BIROUD<sup>1</sup>, J. DAVILA, AND F. MAHMOUDI</i>	
MAXIMUM PRINCIPLE FOR OPTIMAL CONTROL PROBLEM OF FORWARD BACKWARD WITH A JUMP IN THE MEAN-FIELD MODEL.....	322
<i>N. CHAOUCHKHOUANE, B. LABED, L. TAMER</i>	
ON A SOLUTIONS IN $PC(0,B;X)$ OF SOME INTEGRAL EQUATION WITH APPLICATION TO AN IMPLULSIVE SEMILINEAR DIFFERENTIAL EQUATION .....	322
<i>Leila AITKAKI, Nadjat ABADA</i>	
PERSISTENCE AND GLOBAL STABILITY IN A BEDDINGTON-DEANGELIS TYPE THREE SPECIES FOOD CHAIN.....	323
<i>W. KHELLAF</i>	
<b>POSTER SESSION .....</b>	<b>323</b>
ON THE PARABOLIC EQUATION WITH NONLOCAL CONDITIONS.....	323
<i>Abdelhak Berkane, Abdelkrim Zekri</i>	
A NONLOCAL SPECTRAL PROBLEM .....	324
<i>Abdelkrim Zekri, Abdelhak Berkane</i>	
FIXED POINT THEOREM AND EM ALGORITHM .....	324
<i>Ahsene LANANI, Rahima BENCHABI</i>	
A NEW MODIFIED SCHEME FOR LINEAR SHALLOW-WATER EQUATIONS.....	326
<i>Aicha BOUSSAHA</i>	
ELECTRO-VISCOELASTIC ANTIPLAN CONTACT PROBLEM WITH POWER FRICTION LAW .....	327
<i>Allaoua BOUDJEDOUR, Mohamed DALAH</i>	
HIGH ORDER BOUNDARY VALUE PROBLEMS AT RESONANCE ON AN UNBOUNDED INTERVAL.....	327
<i>Assia FRIQUI</i>	
THE FRACTIONAL-ORDER MATHEMATICAL MODELING OF BACTERIAL RESISTANCE AGAINST MULTIPLE ANTIBIOTICS IN CASE OF LOCAL BACTERIAL INFECTION .....	328
<i>Bahatdin DAŞBAŞI, Emre Hayri BARAZ</i>	
CHELYSHKOV COLLOCATION APPROACH FOR MODEL DESCRIBING BIOLOGICAL SPECIES LIVING TOGETHER	329
<i>Cem OĞUZ, Mehmet SEZER</i>	
EXISTENCE OF SOLUTIONS FOR $P(X)$ -SOLITONS TYPE EQUATIONS IN SEVERAL SPACE DIMENSIONS.....	330
<i>Dellal ABDELKADER, Henderson JOHNNY, Ouahab ABDELGHANI</i>	
THE EXISTENCE OF SOLUTIONS FOR A FRACTIONAL-ORDER BOUNDARY VALUE PROBLEM.....	331
<i>Dondu OZ, Ilkay KARACA</i>	
PROPERTIES OF MINIMIZING CURVES FOR GEOMETRIC OPTIMAL CONTROL PROBLEMS .....	332
<i>Driai Nedjoud</i>	
A NEW APPROACH OF THE CUTTING PLANE ALGORITHM USING INTERIOR POINT METHOD .....	333
<i>El Amir DJEFFAL</i>	
ON THE GENERALIZATION OF THE GRAPH-DIRECTED ITERATED FUNCTION SYSTEMS .....	334
<i>Yunus ÖZDEMİR, Fatma Diğdem YILDIRIM</i>	
APPROXIMATION OF THE UNILATERAL CONTACT PROBLEM BY THE FINITE ELEMENT METHOD.....	335
<i>Frekh TAALLAH</i>	
SOME SPECIAL CURVES AND MANNHEIM CURVES IN THREE DIMENSIONAL EUCLIDEAN SPACE.....	336
<i>Funda KAYMAZ, Ferdağ KAHRAMAN AKSOYAK</i>	
LAMB SHIFT IN HYDROGEN LIKE ATOM INDUCED FROM NON COMMUTATIVE QUANTUM SPACE TIME .....	337
<i>Hakim GUELMAMENE</i>	
MODELING AND CONTROL FOR NONLINEAR SYSTEM.....	338
<i>Hachemi GLAOUI</i>	

EXISTENCE OF POSITIVE SOLUTIONS FOR SOME SYSTEMS OF SINGULAR SECOND-ORDER DIFFERENTIAL EQUATIONS .....	339
<i>Karima MEBARKI, Smail DJEBALI</i>	
ON INVARIANT WIDE BAND NOISE FILTER .....	340
<i>Kanda ABUASSBA</i>	
ANALYSE AND STUDY OF ANTIPLANE ELECTRO-VISCOELASTIC CONTACT PROBLEM .....	341
<i>Hacene Chaouche SOUMEYA , Mohamed DALAH, Allaoua BOUDJEDOUR</i>	
ON FINITE ELEMENT APPROXIMATION IN THE $L^{\infty}$ -NORM OF SYSTEM OF PARABOLIC QUASI-VARIATIONAL INEQUALITIES RELATED TO STOCHASTIC CONTROL PROBLEMS .....	342
<i>Mohamed El Amine BENCHEIK LE HOCINE</i>	
THE EFFECT OF ALLEE FACTOR ON STABILITY IN A NONLINEAR DISCRETE-TIME POPULATION MODEL INVOLVING DELAY .....	343
<i>Özlem AK GÜMÜŞ</i>	
OPTIMAL CLAIM BEHAVIOUR FOR VEHICLE DAMAGE INSURANCES .....	344
<i>S.SEGNI</i>	
VOLTERRA INTEGRO-DIFFERENTIAL EQUATIONS OF CONVOLUTION TYPE.....	344
<i>Sami SEGNI</i>	
THE WEAK SOLUTION OF ANTIPLANE ELECTRO-VISCOELASTIC CONTACT PROBLEM WITH REGULARIZED FRICTION LAW .....	345
<i>Hacene Chaouche SOUMEYA , Mohamed DALAH</i>	
NEW EXACT SOLUTIONS OF NONLINEAR PARTIAL DIFFERENTIAL EQUATIONS USING TRIAL EQUATION METHOD.....	346
<i>Riadh HEDLI, Abdelouahab KADEM</i>	
A STUDY OF THE APPLICATION OF CHAOS TO THE GLOBAL OPTIMIZATION.....	347
<i>Tayeb HAMAIZIA</i>	
DETERMINATION OF SOME NON LINEAR GROWTH CURVES WITH THE SUM OF SQUARE REDUCTION TEST FOR TURKEYS REARING IN FREE RANGE SYSTEM .....	348
<i>Ufuk KARADAVUT, Atilla TAŞKIN, Mehmet Emin YAZICI</i>	
LOCAL CONDITIONS FOR THE EXISTENCE OF CYCLES .....	349
<i>Zineb BENMEZIANE</i>	
MAPPINGS BETWEEN $C^*$ - ALGEBRAS THAT PRESERVE THE SPECTRUM .....	350
<i>Hakan AVCI, Nilay SAGER</i>	
EXISTENCE OF MINIMAL AND MAXIMAL SOLUTIONS FOR A SECOND ORDER QUASILINEAR DYNAMIC EQUATION WITH INTEGRAL BOUNDARY CONDITIONS .....	351
<i>Mohammed DERHAB, Mohamed NEHARI</i>	
<b>INDEX.....</b>	<b>352</b>



# PLENARY TALKS

## UPPER AND LOWER SOLUTION METHOD FOR $n^{\text{th}}$ ORDER BVPs ON AN INFINITE INTERVAL

Ravi P. AGARWAL

Texas A&M University-Kingsville, USA

[Ravi.Agarwal@tamuk.edu](mailto:Ravi.Agarwal@tamuk.edu)

**Abstract:** This work is devoted to study  $n^{\text{th}}$  order ordinary differential equation on a half-line with Sturm-Liouville boundary conditions. The existence results of a solution and triple solutions are established by employing a generalized version of the upper and lower solution method, Schäuder fixed point theorem, and topological degree theory. In our problem the nonlinearity depends on derivatives, and we allow solutions to be unbounded, which is an extra interesting feature. To demonstrate the usefulness of our results we illustrate two examples.

**Keywords:**  $n^{\text{th}}$  order ODE, Schäuder fixed point theorem, topological degree theory.

## MEASURES OF NONCOMPACTNESS AND THEIR SEVERAL APPLICATIONS

Mohammad MURSALEEN

*Department of Mathematics, Aligarh Muslim University, Aligarh/INDIA*

[mursaleenm@gmail.com](mailto:mursaleenm@gmail.com)

**Abstract:** In this talk, we present technique of measures of noncompactness to characterize compact operators between some sequence spaces. We also present some applications of measures of noncompactness to the theory of infinite system of differential equations in some sequence spaces. Further, we present some new results on applications to integral equations.

**Keywords:** Measures of noncompactness, differential equations, sequence spaces.

### References:

- [1] M. Mursaleen. "Differential equations in classical sequence spaces." *Revista de la Real Academia de Ciencias Exactas, Físicas y Naturales. Serie A. Matemáticas* (2016): 1-26.
- [2] M. Mursaleen. "Application of measure of noncompactness to infinite system of differential equations." *Canadian Math. Bull.* 56 (2), 2013 pp. 388–394.
- [3] M. Mursaleen, S. A. Mohiuddine. "Applications of measures of noncompactness to the infinite system of differential equations in  $l_p$  spaces". *Nonlinear Anal.* 75, 2111–2115 (2012).

## THE CHALLENGE AND MAGIC OF INVERSE PROBLEMS AND THE MATHEMATICS OF SIGNAL PROCESSING

Zuhair NASHED

Department of Mathematics  
University of Central Florida  
Orlando, Florida, USA

**Abstract:** Inverse Problems deal with determining for a given input-output system an input that produces an observed output, or determining an input that produces an output that is as close as possible to a desired output, often in the presence of noise. Most inverse problems are ill-posed, so their resolution requires some methods of regularization.

Signal Analysis/Processing deals with digital representations of signals and their analog reconstructions from digital representation. Sampling expansions, filters, reproducing kernel Hilbert spaces, various function spaces, and techniques of functional analysis, computational and applied harmonic analysis play pivotal role in this area.

This talk will highlight some land marks in these two areas and discuss some common threads between them. We will show that function spaces, in particular reproducing kernel Hilbert spaces, play a magical role in both ill-posed inverse problems and sampling expansion theorems.

The year 2016 marks the 110th birthday of the great Russian mathematician Andrey Nikoayevich Tikhonov (October 30, 1906 - October 7, 1993) and the 100th birthday of the great American mathematician Claude Elwood Shannon (April 30, 1916 - February 24, 2001). We celebrate their memory and seminal contributions to regularization theory of ill-posed problems, and sampling expansions and communication theory, respectively.

## FIXED POINT ALGORITHMS FOR OPTIMIZATION

Hong-Kun XU

*Department of Mathematics  
Hangzhou Dianzi University  
Hangzhou 310018, China  
xuhk@hdu.edu.cn*

**Abstract:** We will report fixed point algorithms and their applications in convex and nonconvex optimization problems.

**Keywords:** Fixed point algorithms, optimization problems.

## QUADRATURE METHODS FOR COMPUTING HIGHLY OSCILLATORY INTEGRALS WITH BESSEL FUNCTIONS

Gradimir V. MILOVANOVIĆ

*Mathematical Institute, Serbian Academy of Sciences and Arts,  
Belgrade/SERBIA  
[gvm@mi.sanu.ac.rs](mailto:gvm@mi.sanu.ac.rs)*

**Abstract:** In this lecture, we deal with integration of rapidly oscillating functions, which appear in the theory of special functions, as well as in applied and computational sciences and engineering. Using suitable integral representations of special functions, we show how existing or specially developed quadrature formulas can be successfully applied to effectively calculation of such highly oscillatory integrals of Fourier type with Hankel kernel, oscillatory Bessel transformation, Bessel-Hilbert transformation, etc. Theoretical results and numerical examples illustrate the efficiency and accuracy of the proposed methods.

**Keywords:** Gaussian quadrature rule, oscillatory Bessel transform, Hankel function, Whittaker W function, error analysis.

### References:

- [1] G.V. Milovanović, "Numerical calculation of integrals involving oscillatory and singular kernels and some applications of quadratures", *Comput. Math. Appl.* 36 (1998), 19-39.
- [2] Z. Xu, G.V. Milovanović, S. Xiang, "Efficient computation of highly oscillatory integrals with Hankel kernel", *Appl. Math. Comput.* 261 (2015), 312-322.
- [3] Z. Xu, G.V. Milovanović, "Efficient method for the computation of oscillatory Bessel transform and Bessel Hilbert transform", *J. Comput. Appl. Math.* 308 (2016), 117-137.
- [4] Z. Xu, S. Xiang, "On the evaluation of highly oscillatory finite Hankel transform using special functions", *Numer. Algor.* 72 (2016), 37-56.
- [5] G.V. Milovanović, "Generalized Gaussian quadratures for integrals with logarithmic singularity", *FILOMAT*, 30 (2016), 1111-1126.

## A GLANCE INTO THE WORLD OF ITERATIVE SCHEMES: STABILITY AND RATE OF CONVERGENCE

V.BERINDE

*Technical University of Cluj-Napoca  
North University Center at Baia Mare  
Baia Mare/ Romania  
[vasile.berinde@gmail.com](mailto:vasile.berinde@gmail.com)*

**Abstract:** Iterative schemes are ubiquitous among the constructive methods in nonlinear analysis. Some of their most important accessories are:

1. Computability; 2. Stability; 3. Rate of convergence (error estimate). Starting from the various numerical demands coming from concrete problems in pure and applied mathematics, the main aim of this talk is to present some recent approaches to study of *stability* and *rate of convergence* of one step and multi-step iterative schemes.

Numerical tests and experiments to illustrate the main ideas of the lecture will also be presented.

**Keywords:** Iterative schemes, stability, rate of convergence.

## COUPLED FIXED POINTS AND DIAGONAL OPERATORS

Adrian PETRUȘEL

*Department of Mathematics, Babeș-Bolyai University Cluj-Napoca, Romania  
[petrusel@math.ubbcluj.ro](mailto:petrusel@math.ubbcluj.ro)*

**Abstract:** In this talk, we will study coupled fixed point problems for single-valued and multi-valued operators. The notion of diagonal operator and its historical roots will be also presented. Our approach is based on the weakly Picard operator technique. Some applications and research directions are also suggested.

### References:

- [1] V. Berinde, Generalized coupled fixed point theorems for mixed monotone mappings in partially ordered metric spaces, *Nonlinear Anal.*, 74 (2011) 7347-7355.
- [2] T. GnanaBhaskar, V. Lakshmikantham, Fixed point theorems in partially ordered metric spaces and applications, *Nonlinear Anal.*, 65 (2006), 1379-1393.
- [3] D. Guo, V. Lakshmikantham, Coupled fixed points of nonlinear operators with applications, *Nonlinear Anal.*, 11 (1987), 623-632.
- [4] M.A. Krasnoselskii and P.P. Zabreiko, *Geometrical Methods of Nonlinear Analysis*, Springer, 1984.
- [5] A. Petrușel, G. Petrușel, B. Samet, J.-C. Yao, Coupled fixed point theorems for symmetric contractions in b-metric spaces with applications to operator equation systems, *Fixed Point Theory*, 17 (2016), no.2, 457-476.

## WEAK SHARP SOLUTIONS AND MINIMUM AND MAXIMUM PRINCIPLE SUFFICIENCY PROPERTIES FOR NONSMOOTH VARIATIONAL INEQUALITIES

Qamrul Hasan ANSARI

*<sup>1</sup>Department of Mathematics, Aligarh Muslim University, Aligarh, India*

**Abstract:** In this talk, we present a brief introduction of nonsmooth variational inequalities defined by of generalized directional derivatives. We first introduce gap functions, and then by using such gap functions we study the minimum and maximum principle sufficiency properties for nonsmooth variational inequalities. We provide several characterizations of these two sufficiency properties. We also study the weak sharp solutions for nonsmooth variational inequalities and give a characterization in terms of error bound. Some characterizations of the solution sets of nonsmooth variational inequalities will be presented. Under certain conditions, we prove that the sequence generated by an algorithm for finding a solution of nonsmooth variational inequalities terminates after a finite number of iterates provided that the solutions set of the nonsmooth variational inequality is weakly sharp. We also study the finite termination property of the gradient projection method for solving nonsmooth variational inequalities under weak sharpness of the solution set.

**Keywords:** Three step iteration, strong convergence, rate of convergence, data dependence integral equation.

### References:

- [1] F.Gursoy, V. Karakaya, "A Picard-S hybrid type iteration method for solving a differential equation with retarded argument", arXiv preprint arXiv:1403.2546 (2014).
- [2] M.Abbas, T. Nazir, "A new faster iteration process applied to constrained minimization and feasibility problems", *Matematicki Vesnik*, 66(2014), 223.
- [3] R.Chugh, V. Kumar, S. Kumar, "Strong Convergence of a New Three Step Iterative Scheme in Banach Spaces", *American Journal of Computational Mathematics*, 2(2012), 345-357.
- [4] V. Berinde, "On the approximation of fixed points of weak contractive mappings", *Carpathian J. Math*, 19(2003), 7-22.

## INVITED TALKS

### AN ALGORITHM OF ASYMPTOTICALLY NONEXPANSIVE MAPPINGS WITHOUT FAST RATE CONVERGENCE CONDITION IN HYPERBOLIC SPACES

Abdul Rahim KHAN<sup>1</sup>, Hafiz FUKHAR-UD-DIN<sup>1,2</sup>

<sup>1</sup>*Department of Mathematics and Statistics, King Fahd University of Petroleum and Minerals, Dhahran 31261, Saudi Arabia*

[arahim@kfupm.edu.sa](mailto:arahim@kfupm.edu.sa)

<sup>2</sup>*Department of Mathematics, The Islamia University of Bahawalpur, Bahawalpur 63100, Pakistan*

[hfdin@kfupm.edu.sa](mailto:hfdin@kfupm.edu.sa)

**Abstract:** In the context of a hyperbolic space, we introduce and study convergence of implicit iterates of a finite family of asymptotically (quasi-) nonexpansive mappings with and without the fast rate convergence condition associated with the family of mappings. The results presented in this paper substantially improve and extend several recent well-known results in uniformly convex Banach spaces.

**Keywords:** Hyperbolic space, asymptotically (quasi-)nonexpansive mapping, common fixed point, implicit iteration process, semi-compactness,  $\Delta$  –convergence, strong convergence.

#### References:

- [1] W. Guo and Y. J. Cho, On the strong convergence of the implicit iterative processes with errors for a finite family of asymptotically nonexpansive mappings, *Appl. Math. Lett.*, 21(2008), 1046-1052.
- [2] A. R. Khan, A. A. Domlo and H. Fukhar-ud-din, Common fixed points Noor iteration for a finite family of asymptotically quasi-nonexpansive mappings in Banach spaces, *J. Math. Anal. Appl.*, 341(2008), 1-11.
- [3] Z. H. Sun, Strong convergence of an implicit iteration process for a finite family of asymptotically quasi-nonexpansive mappings *J. Math. Anal. Appl.*, 286 (2003), 351-358.
- [4] E. Yolacan and H. Kiziltunc, A new hybrid iteration method for I-symptotically nonexpansive mappings, *Numer. Funct. Anal. Optimiz.* DOI:10.1080/01630563.2016.1179203.

## Chebyshev Centers, Fixed Point Theorems and Best Proximity Point Theorems

P.VEERAMANI

*Department of Mathematics, Indian Institute of Technology Madras, Chennai-600036, India*

[pvmani@iitm.ac.in](mailto:pamani@iitm.ac.in)

**Abstract:** In this talk, it is aimed to discuss the relation between normal structure and the invariance of the set of Chebyshev centers of a non-expansive (isometry) map defined on a weakly compact convex subset of a Banach space. We also indicate some problems involving Chebyshev centers, normal structure and fixed points of non-expansive (isometry) maps.

**Keywords:** Nonexpansive maps, Chebyshev centers, best proximity.

## Optimality Conditions for Generalized Vector Equilibrium Problems

Ali FARAJZADEH

*Department of Mathematics, Razi University, Kermanshah, 67149, Iran.*

[farajzadehali@gmail.com](mailto:farajzadehali@gmail.com)

**Abstract:** In this presentation, existence of a nonempty pointed convex cone with empty topological interior and nonempty algebraic interior for an arbitrary infinite dimensional linear topological space is proved. A multivalued version of Farakas's lemma in the setting of ordered linear spaces is established. By using it, an equivalence relation between the solution set of some generalized vector equilibrium problems and the corresponding minimization problems are provided. The techniques are used in this note different from the KKM theory and fixed point theory. Some examples in order to support the main results are given.

**Keywords:** Pointed convex cone, KKM, Farakas's lemma, generalized vector equilibrium problems, minimization problems, infinite dimensional linear topological space.

## GENERALIZED MORREY REGULARITY FOR PARABOLIC EQUATIONS WITH DISCONTINUOUS DATA

Vagif S. GULIYEV<sup>1,2</sup>

<sup>1</sup>*Department of Mathematics, Ahi Evran University,  
Kirsehir/TURKEY*

<sup>2</sup>*Institute of Mathematics and Mechanics,  
Baku/AZERBAIJAN  
[vagif@guliyev.com](mailto:vagif@guliyev.com)*

**Abstract:** We obtain two types of results:

- Boundedness of sublinear operators generated by singular and nonsingular integrals in generalized Morrey spaces  $M^{p,\varphi}$ . Continuity in  $M^{p,\varphi}$  of some classical integral operators as the Calderon-Zygmund one.
- Global  $M^{p,\varphi}$ -regularity of the solutions of boundary value problems for linear uniformly elliptic/parabolic equations with discontinuous coefficients.

The results presented here are published in [1,2,3,4,5].

The research of V. Guliyev was partially supported by the grant of Presidium of Azerbaijan National Academy of Science 2015.

### References:

- [1] V. S. Guliyev, S. S. Aliyev, T. Karaman, P. Shukurov, Boundedness of sublinear operators and commutators on generalized Morrey spaces, *Integral Equations Operator Theory* 71 (3) (2011), 327-355.
- [2] A. Akbulut, V.S. Guliyev and R. Mustafayev, On the boundedness of the maximal operator and singular integral operators in generalized Morrey spaces, *Math. Bohem.* 137 (1) (2012), 27-43.
- [3] V. S. Guliyev, L. Softova, Global regularity in generalized Morrey spaces of solutions to nondivergence elliptic equations with VMO coefficients, *Potential Anal.* 38 (4) (2013), 843-862.
- [4] L. Softova, Parabolic oblique derivative problem with discontinuous coefficients in generalized Morrey spaces, *Ric. Mat.* 62 (2) (2013), 265-278.



## COMPARATIVE EVALUATION OF A NEW ITERATIVE LEARNING CONTROL ALGORITHM BY NUMERICAL EXAMPLES

Jan EKSTEEN<sup>1</sup>, Stephan HEYNS<sup>1</sup>

<sup>1</sup>*Department of Mechanical and Aeronautical Engineering, University of Pretoria, Pretoria/SOUTH AFRICA*

[jan.eksteen@up.ac.za](mailto:jan.eksteen@up.ac.za)

[stephan.heyns@up.ac.za](mailto:stephan.heyns@up.ac.za)

**Abstract:** Model-based iterative learning control (ILC) [1] of nonlinear dynamical systems is an off-line control algorithm that is routinely used in structural integrity testing of mechanical systems in the laboratory. In a recent paper [2] the connections between the ILC algorithm and Mann iteration was explored and an alternative model-based ILC algorithm was developed, however without a comparative evaluation of the new method in terms of numerical examples. This paper presents a comparative evaluation of the new method in terms of numerical examples similar to those in [2], proving that the new method is competitive with the conventional algorithm.

**Keywords:** Iterative learning control, nonlinear dynamical systems, Mann iteration.

### References:

- [1] H.-S. Ahn, Y. Chen, K.L. Moore, "Iterative learning control: brief survey and categorization" *IEEE Transactions On Systems, Man, And Cybernetics*, 37(2007):1099-1121.
- [2] J.J.A. Eksteen, P.S. Heyns, "An alternative update formula for non-linear model-based iterative learning control", *Inverse Problems in Science and Engineering*, 24(2016), 860-888.

## CONTRIBUTED TALKS

### GENERALIZED BOUNDARY PROBLEM GOVERNED BY THE BILAPLACIEN OPERATOR

A. BOULAOUAD, B. MEROUANI

*Univ. F. ABBAS-Sétif 1, Algeria.*

[a\\_boulaouad@yahoo.fr](mailto:a_boulaouad@yahoo.fr),

*Univ. F. ABBAS-Sétif 1, Algeria*

[mermathsb@hotmail.fr](mailto:mermathsb@hotmail.fr).

**Abstract:** In this work, we study the existence and the uniqueness of a mathematical model solution of a thin plate with a polygonal rectilinear frontier under generalized boundary conditions such as those of Fourier. Concerning, the particular cases of Laplace's operators and Lamé's elasticity had been respectively studied by Mghazli in [8] and by Merouani in [7].

**Keywords:** Boundary Problem, Bilaplacien operator, Existence, Uniqueness.

#### References:

- [1] A. Alvino, P. L. Lions, Trombetti, Comparison results for elliptic and parabolic equations via Schwarz symmetrization, *Ann. H. Poincaré Anal. Nonlinéaire* 7 (1990) 37-65.
- [2] R. Dautray-J. L. Lions, *Analyse mathématique et calcul numérique*, Tome1, Masson 1988
- [3] P. Grisvard, *Singularities in boundary value problems*. Springer-verlag, Masson (Paris), 1992:
- [4] S. Gunther, Boris N. Khoromskij, Boundary integral equations for the biharmonic dirichlet problem on nonsmooth domains, *Journal of Integral Equations and Application* Volume 11, Number 2, Summer 1999.
- [5] Lions-Magenes, *Problèmes aux limites non homogène et applications*, volume1. Dunod Paris, 1968:
- [6] B. Merouani, Solution singulières du système de l'élasticité dans un polygone pour différentes conditions aux limites, *Maghreb Maths. Rev*, Vol. 5, Nos 1 & 2, (1996) ; pp.95 - 112:

## ON ORDER OF APPROXIMATION FUNCTION BY GENERALIZED BERNSTEIN-CHLODOVSKI POLYNOMIALS

A.E. ABDULLAYEVA

*Institute of Mathematics and Mechanics of National Academy of Sciences of  
Azerbaijan*

**Abstract:** The generalized Bernstein-Chlodovsky polynomials order  $(n, r)$  defined as a

$$B_{(n,r)}(f; x) = \sum_{k=0}^n \sum_{i=0}^r \frac{f(\frac{kb_n}{n})}{i!} (x - \frac{kb_n}{n})^i C_n^k(\frac{x}{b_n})^k (1 - \frac{x}{b_n})^{n-k}, 0 \leq x \leq b_n \quad (1)$$

Here  $\lim_{n \rightarrow \infty} b_n = \infty, \lim_{n \rightarrow \infty} \frac{b_n}{n} = 0$ .

In particular, if, then (1) coincides with the classical Bernstein-Chlodovsky polynomials

$$B_{(n,r)}(f; x) = \sum_{k=0}^n \sum_{i=0}^r f(\frac{kb_n}{n}) C_n^k(\frac{x}{b_n})^k (1 - \frac{x}{b_n})^{n-k}, 0 \leq x \leq b_n,$$

Let the  $C^r[0, \infty)$  class  $r$ -times continuously differentiable function on the  $[0, \infty)$ .

**Theorem.** Let the  $C^r[0, \infty)$  and  $B_{(n,r)}(f; x)$  is a generalized Bernstein-Chlodovsky polynomials. Then for any fixed  $A > 0$  asymptotic equality

$$\|f(\cdot) - B_{(n,r)}(f; \cdot)\|_{C[0,A]} = O\left(\frac{b_n^{r+2}}{n^{r/2}} \Omega(f^{(r)}; \frac{b_n}{\sqrt{n}})\right).$$

### References:

- [1] A. D. Gadjiev, N. Ispir, "On a sequence of linear positive operators in weighted spaces", *Proc. Inst. Math. Mech. Natl. Acad. Sci. Azerb.*, 11 (1999), 45-55.

## STRONG UNIFORM CONSISTENCY RATES OF CONDITIONAL QUANTILES FOR FUNCTIONAL DATA IN THE FUNCTIONAL SINGLE-INDEX MODEL

Abbes RABHI

*Department of Mathematics, University of Sidi Bel Abbès,  
Sidi Bel Abbès/ALGERIA  
[rabhi\\_abbes@yahoo.fr](mailto:rabhi_abbes@yahoo.fr)*

**Abstract:** This presentation, deals with a scalar response conditioned by a functional random variable. The main goal is to estimate nonparametrically the quantiles of such a conditional distribution when the sample is considered as an i.i.d sequence. Firstly, a kernel type estimator for the conditional cumulative distribution function (**cond-cdf**) is introduced. Afterwards, we derive an estimation of the quantiles by inverting this estimated **cond-cdf** and asymptotic properties are stated when the observations are linked with a single-index structure. We establish the pointwise almost complete convergence and the uniform almost complete convergence (with the rate) of the kernel estimate of this model. The functional conditional quantile approach can be used both to forecast and to build confidence prediction bands.

**Keywords:** Conditional distribution, conditional quantile, functional data, functional single-index process, small ball probability.

### References:

- [1] A. A. Bouchentouf, T. Djebbouri, A. Rabhi and K. Sabri, "Str uniform consistency rates of the conditional distribution estimator in the single functional index model", *Applicaciones Mathematicae (warsaw)*, 41(3-4)(2014), 301-322.
- [2] F. Ferraty, A. Laksaci, A. Tadj, P. Vieu, "Rate of uniform consistency for nonparametric estimates with functional variables", *J. Statist. Plann. And Inf.*, 140(2010), 335-352.
- [3] F. Ferraty, A. Peuch, P. Vieu, "Modèle à indice fonctionnel simple", *CR Mathématiques, Paris*, 336(2003), 1025-1028

## A NOTE ON THE VALUES OF THE TWISTED BARNES ZETA FUNCTIONS AND THEIR APPLICATIONS

Abdelmejid BAYAD<sup>1</sup>, Yılmaz SIMSEK<sup>2</sup>

<sup>1</sup>*Department of Mathematics, d'Évry Val d'Essonne University,  
Paris/France*

[abayad@maths.univ-evry.fr](mailto:abayad@maths.univ-evry.fr)

<sup>2</sup>*Department of Mathematics, Akdeniz University, Antalya/TURKEY*

[ysimsek@akdeniz.edu.tr](mailto:ysimsek@akdeniz.edu.tr)

**Abstract:** The aim of this paper is to study and investigate some properties of the twisted zeta function related to the complex parameters with positive real parts such as  $a_1; \dots; a_N$ . We give many interesting properties of these functions with their functional equations. We also give relationships between these functions and other well-known zeta families such as the Barnes zeta functions the Hurwitz zeta functions and the Riemann zeta functions. Finally we give some applications of these functions by the analytic continuation.

**Keywords:** Riemann Zeta function, Hurwitz zeta function, Barnes zeta functions, Bernoulli numbers.

### References:

- [1] W. Barnes, On the Theory of the Multiple Gamma Function, Trans. Cambridge. Philos. Soc. 19, 374-425 (1904).
- [2] A. Bayad, Arithmetical Properties of Elliptic Bernoulli and Euler Numbers, Int. J. of Algebra 4 (8), 353–372 (2010).
- [3] T. Kim, A New Approach to q-Zeta Function, Adv. Stud. Contemp. Math. 11 (2), 157-162 (2005).
- [4] S. N. M. Ruijsenaars, On Barnes' Multiple Zeta and Gamma Functions, Adv. Math. 156, 107-132.
- [5] W. H. Schikhof, Ultrametric Calculus: An Introduction to p-Adic Analysis (Cambridge Univ Press, 1984).
- [6] Y. Simsek, Twisted (h,q)-Bernoulli Numbers and Polynomials Related to Twisted (h,q)-Zeta Function and L-Function, J. Math. Anal. Appl. 324 (2), 790-804 (2006).

## GENERALIZATIONS OF KAPLANSKY'S THEOREM INVOLVING UNBOUNDED LINEAR OPERATORS

Abdelkader BENALI

*Department of Mathematics, Faculty of science, University of Hassiba Benbouali Chlef 02000, Algeria*  
[benali4848@gmail.com](mailto:benali4848@gmail.com)

**Abstract:** The purpose of this paper is to generalize a very famous result on products of normal operators, due to I. Kaplansky. The context of generalization is that of bounded hyponormal and unbounded normal operators on complex separable Hilbert spaces. Some examples "spice up" the paper. enough so that even monographs have been devoted to them. See for instance [3] and [10].

In this paper we are mainly interested in generalizing the following result to unbounded normal and bounded hyponormal operators.

**Keywords:** Products of operators, Bounded and unbounded, Normal Hypo normal subnormal operators, data Kaplansky Theorem, Fuglede Putnam Theorem.

### References:

- [1] .J. B. Conway, A Course in functional Analysis, Springer, 1990 (2nd edition).
- [2] .J. B. Conway, A Course in Operator Theory, GSM 21, American Mathematical Soci-ety, Providence, RI, 2000..
- [3] A. Devinatz, A. E. Nussbaum, On the Permutability of Normal operators, Ann. Of Math. (2), 65 (1957) 144-152..
- [4] B. Fuglede, A Commutativity Theorem for Normal Operators, Proc. Nati. Acad. Sci.,36 (1950) 35-40
- [5] Akhiezer et Glazman : Theory of Linear Operators in Hilbert spaces. Frederick Ungar Publishing Company, New York, 1961. (Tomes 1 et 2).
- [6] Math. (2), 65 (1957) 144-152..
- [7] Weidman J. : Linear operators in Hilbert spaces, Springer-Verlag, New York, 1980.
- [8] J. Charles, M. Mbekhta et H. Queffélec : Analyse fonctionnelle et théorie des opérateurs, Dunod, Paris, 2010.
- [9] Walter Rudin Analyse fonctionnelle Springer, New York, 1989.

## THE BOUNDEDNESS OF MAXIMAL AND CALDERON-ZYGMUND OPERATORS ON LOCAL MORREY-LORENTZ SPACES

Abdulhamit KUCUKASLAN

*Ministry of Health, Central Organization*

*Ankara/TURKEY*

[abdulhamitk@hotmail.com](mailto:abdulhamitk@hotmail.com)

**Abstract:** In this talk the boundedness, including the limiting cases, of the Hardy-Littlewood maximal operator  $M$ , the Calderon-Zygmund operators  $T$  and the maximal Calderon-Zygmund operators  $T$  on the local Morrey-Lorentz spaces  $M_{p,q,\lambda}^{loc}(R^n)$  will be proved. Further some applications of obtained results will be given.

**Keywords:** Local Morrey-Lorentz spaces, Maximal operator, Calderon-Zygmund operators, maximal Calderon-Zygmund operators.

### References:

- [1] K.F. Andersen and B. Muckenhoupt, Weighted weak type Hardy inequalities with applications to Hilbert transforms and maximal functions, *Studia Math.*, 72 (1982), 9–26.
- [2] C. Bennett, De Vore R and Sharpley R. Maximal singular integrals on  $L_\infty$ , *Colloq. Math. Soc. Janos Bolyai*, no. 35, Functions, Series, Operators, Budapest, North-Holland, Amsterdam, (1980) 233-235.
- [3] C. Aykol, V.S. Guliyev and A. Serbetci, Boundedness of the maximal operator in the local Morrey-Lorentz spaces, *Jour. Inequal. Appl.*, 2013, 2013:346.
- [4] C. Aykol, V.S. Guliyev, A. Kucukaslan and A. Serbetci, The boundedness of Hilbert transform in the local Morrey-Lorentz spaces, *Integral Transform. Spec. Funct.*, (<http://dx.doi.org/10.1080/10652469.2015.1121483>).
- [5] C. Bennett and R. Sharpley, *Interpolation of Operators*, Academic Press, Boston, 1988.
- [6] G.G. Lorentz, Some new function spaces, *Annals of Mathematics*, 51 (1950), 37--55.

## DISCRETIZATION SCHEME TO FRACTIONAL DIFFUSION EQUATION WITH MEMORY TERM

Abderrazek CHAOUI

**Abstract:** In this work we use the method of Rohe to approximate the solution of fractional diffusion equation with second-order differential Volterra operator and fractional integral condition. Existence and uniqueness of weak solution in an appropriate sense as well as some regularity results are obtained .

## TWO-PARAMETER REGULARIZATION METHOD FOR AN ILL-POSED CAUCHY PROBLEM FOR ELLIPTIC EQUATIONS

A. BENRABAH<sup>1</sup>, N. BOUSSETILA<sup>2</sup> and F. REBBANI<sup>3</sup>

<sup>1,2</sup>*Department of Mathematics, 8 May 1945 University,  
Guelma/ALGERIA*

babderafik@yahoo.fr, naboussetila@yahoo.fr

<sup>3</sup>*Department of Mathematics, Badji Mokhtar University, Annaba/ALGERIA*  
faouzia.rebbani@univ-annaba.org

**Abstract:** The paper is devoted to investigating a Cauchy problem for homogeneous elliptic PDEs in the abstract Hilbert space given by  $u''(t) - Au(t) = 0$ ,  $0 < t < T$ ,  $u(0) = \varphi$ ,  $u'(0) = 0$  where  $A$  is positive self-adjoint and unbounded linear operator. The problem is severely ill-posed in the sense of Hadamard(1), we shall give a new regularization method for this problem when the operator  $A$  is replaced by  $A_\alpha = A(I + \alpha A)^{-1}$  and  $u(0) = \varphi$  is replaced by a nonlocal condition. We show the convergence of this method and we construct a family of regularizing operators for the considered problem. Convergence estimates are established under a priori regularity assumptions on the problem data. Some numerical results are given to show the effectiveness of the proposed method.

**Keywords:** Three step iteration, strong convergence, rate of convergence, data dependence integral equation.

### References:

- [1] J. Hadamard, "Lecture note on Cauchy's problem in linear partial differential equations" Yale Uni press, New Haven, (1923).
- [2] D.N.Hào, N.V Duc and D. Lesnic "A non-local boundary value problem method for the Cauchy problem for elliptic equations", *Inverse problems*, 25: 055002, 27p, (2009).
- [3] F. Zouyed and F. Rebbani, "A modified quasi-boundary value method for an ultraparabolic ill-posed problem", *J. Inverse Ill-Posed Probl.* Volume 22, Issue 4, (2014), 449-466.
- [4] N. Boussetila and F. Rebbani, "Optimal regularization method for ill-posed Cauchy problems", *Electronic Journal of Differential Equations*, Vol. 2006(2006), No. 147, pp. 1-15



## ON THE EXISTENCE OF POSITIVE SOLUTIONS FOR NONLINEAR THREE-POINT BOUNDARY VALUE PROBLEM

Abdulkadir DOGAN

*Department of Applied Mathematics, Faculty of Computer Sciences, Abdullah Gul  
University,  
Kayseri/TURKEY  
[abdulkadir.dogan@agu.edu.tr](mailto:abdulkadir.dogan@agu.edu.tr)*

**Abstract:** We study the existence of a nonlinear three-point boundary value problem

$$\begin{aligned}u''(t) + a(t)f(u(t)) &= 0, & 0 < t < 1, \\ \beta u(0) - \gamma u'(0) &= 0, & \alpha u(\eta) = u(1),\end{aligned}$$

where  $0 < \eta < 1$ ,  $0 < \alpha < 1/\eta$ ,  $\beta, \gamma \geq 0$ ,  $\beta + \gamma > 0$ , and  
 $d = \beta(1 - \alpha\eta) + \gamma(1 - \alpha) > 0$ .

By applying the fixed point theorem in cones, we prove the existence of at least one positive solutions if  $f$  is either superlinear or sublinear.

**Keywords:** Boundary value problems, positive solutions, superlinear and sublinear, operators on a cone

### References:

- [1] A. Dogan, "On the existence of positive solutions for the second-order boundary value problem", *Appl. Math. Lett.* 49 (2015) 107-112.
- [2] R. Ma, "Positive solutions of a nonlinear three-point boundary value problem" *J. Differ. Equat. Appl.* 34 (1998) 1-8.
- [3] J. R. Graef, L. Kong "Positive solutions for third order semipositone boundary value problems", *Appl. Math. Lett.* 22 (2009) 1154-1160.
- [4] Z. Chengbo, "Positive solutions for semi-positone three-point boundary value problems," *J. Comput. Appl. Math.* 228 (2009) 279-286.

## POSITIVE SOLUTIONS OF A THREE-POINT BOUNDARY VALUE PROBLEM FOR $p$ -LAPLACIAN DYNAMIC EQUATION ON TIME SCALES

Abdulkadir DOGAN

*Department of Applied Mathematics, Faculty of Computer Sciences, Abdullah Gul University,  
Kayseri/TURKEY  
[abdulkadir.dogan@agu.edu.tr](mailto:abdulkadir.dogan@agu.edu.tr)*

**Abstract:** We study a three-point boundary value problem for  $p$ -Laplacian dynamic equation on time scales. By using the Avery and Peterson fixed point theorem, we prove the existence at least three positive solutions of the boundary value problem. The interesting point is that the non-linear term  $f$  involves a first-order derivative explicitly. As an application, an example is given to illustrate the result.

**Keywords:** Time scales, boundary value problem,  $p$ -Laplacian, positive solution, fixed point theorem.

### References:

- [1] A. Dogan, "On the existence of positive solutions for the one-dimensional  $p$ -Laplacian boundary value problems on time scales", *Dynamic Systems and Applications* 24 (2015) 295-304.
- [2] Z. He, X. Jiang, "Triple positive solutions of boundary value problems for  $p$ -Laplacian dynamic equations on time scales" *Journal of Mathematical analysis and applications* 321 (2006) 911-920.
- [3] H.R. Sun, W.T. Li, "Positive solutions for nonlinear three-point boundary value problems on time scales", *J. Math. Anal. Appl.* 299 (2004) 508-524.
- [4] D.R. Anderson, "Solutions to second-order three-point problems on time scales" *J. Differ. Equat. Appl.* 8 (2002) 673-688.

## $\Delta_p^m$ -STATISTICAL CONVERGENCE

Abdulkadir KARAKAŞ<sup>1</sup>, Yavuz ALTIN<sup>2</sup>

<sup>1</sup>*Department of Mathematics, Siirt University,  
Siirt /TURKEY*

<sup>2</sup>*Department of Mathematics, Firat University,  
Elazığ/TURKEY*

[kadirkarakas21@hotmail.com](mailto:kadirkarakas21@hotmail.com), [yaltin23@yahoo.com](mailto:yaltin23@yahoo.com)

**Abstract:** In this work, we introduce  $\Delta_p^m$ -statistical convergence and give inclusion relation between  $\Delta_p^m(W_q)$ -convergence and  $\Delta_p^m$ -statistical convergence.

**Keywords:** Statistical Convergence, Difference sequence spaces.

### References:

- [1] Karakaş,A., Altın,Y, Et, M. On some topological properties of a new type difference sequence spaces. In:ADVANCEMENTS IN MATHEMATICAL SCIENCES: Proceedings of the International Conference on Advancements in Mathematical Sciences. AIP Publishing, (2015). p. 020090.
- [2] Et,M., Çolak,R. On some generalized difference sequence spaces, "SoochowJ. Math., 21 (1995), no. 4, 377-386.
- [3] Kızmaz, H. On certain sequence spaces. Canad. Math. Bull. 24 (1981), no. 2, 169-176.
- [4] Et M., Nuray, F.  $\Delta^m$ -statistical convergence. Indian J. Pure Appl. Math. 32 (2001), no. 6, 961--969
- [5] Connor, J.S.The statistical and strong p-Cesàro convergence of sequences.Analysis8(1988), no. 1-2, 47-63.
- [6] Salat,T. On statistically Convergent Sequence of real Numbers, Math. Slovaca 30 (1980), no. 2, 139-150.

## STURMIAN THEORY FOR SECOND-ORDER DIFFERENTIAL EQUATIONS WITH MIXED NONLINEARITIES

Abdullah ÖZBEKLER<sup>1</sup>

<sup>1</sup>*Department of Mathematics, Atılım University,  
Ankara/TURKEY  
[aobekler@gmail.com](mailto:aobekler@gmail.com)*

**Abstract:** In the presentation, Sturmian comparison theory is developed for the pair of second-order differential equations; first of which is the nonlinear differential equations

$$(m(t)y')' + s(t)y' + \sum_{i=1}^n q_i(t)|y|^{\alpha_i-1}y = 0, \quad (\mathbf{A})$$

with mixed nonlinearities  $\alpha_1 > \dots > \alpha_m > 1 > \alpha_{m+1} > \dots > \alpha_n$ , and the second is the nonselfadjoint differential equations

$$(k(t)x')' + r(t)x' + p(t)x = 0. \quad (\mathbf{B})$$

Under the assumption that the solution of Eq. (B) has two consecutive zeros, we obtain Sturm-Picone type and Leighton type comparison theorems for Eq. (A) by employing the new nonlinear version of Picone's formula that we derive. Wirtinger type inequalities and several oscillation criteria are also attained for Eq. (A). Examples are given to illustrate the relevance of the results.

**Keywords:** Comparison, Leighton, Mixed nonlinear, Nonselfadjoint, Sturm-Picone, Wirtinger.

### References:

- [1] Y.G. Sun, James S.W. Wong, "Oscillation criteria for second order forced ordinary differential equations with mixed nonlinearities", *J. Math. Anal. Appl.* **334** (2007) 549-560.
- [2] M. Picone, "Sui valori eccezionali di un parametro da cui dipende un'equazione differenziale lineare ordinaria del secondo ordine", *Ann. Scuola. Norm. Sup.* **11** (1909) 1-41.
- [3] E. Picard, "Leçons sur quelques problèmes aux limites de la théorie des équations différentielles", Paris 1930.

## A UNIFIED APPROACH TO WEIGHTED $L^p$ HARDY-TYPE INEQUALITIES ON RIEMANNIAN MANIFOLDS

Abdullah YENER<sup>1</sup>

<sup>1</sup>*Department of Mathematics, Istanbul Commerce University,  
Istanbul/TURKEY  
ayener@ticaret.edu.tr*

**Abstract:** In this work, we provide an approach that recovers and improves most of the Hardy-type inequalities appeared on Riemannian manifolds  $M$  to date regarding. More precisely, let  $M$  be a complete noncompact Riemannian manifold endowed with a metric  $g$  and  $dV, \nabla, \text{div}$  and  $\Delta$  denote respectively the Riemannian volume element, the Riemannian gradient, the Riemannian divergent and the Laplace Beltrami operator on  $M$ . We proved that if  $a$  and  $b$  are nonnegative weight functions and  $w$  is a positive function such that

$$-\text{div}(a(x)|\nabla w|^{p-2}\nabla w) \geq b(x)w^{p-1}$$

almost everywhere in  $M$ , then the following  $L^p$  Hardy-type inequality

$$\int_M a(x)|\nabla \phi(x)|^p dV \geq \int_M b(x)|\phi(x)|^p dV$$

is valid for all  $\phi \in C_0^\infty(M)$  and  $p \geq 1$ . It is worth emphasizing here that, one can readily obtain as many weighted Hardy-type inequalities as one can construct the functions  $a$  and  $w$  satisfying the above hypothesis.

**Keywords:** Riemannian manifolds, Hardy inequality.

### References:

- [1] G. Carron, Inégalités de Hardy sur les variétés riemanniennes non-compactes, J. Math. Pures Appl. 76(1997), 883-891.
- [2] L. D'Ambrosio and S. Dipierro, Hardy inequalities on Riemannian manifolds and applications, Ann. I. H. Poincaré 31(2014), 449-475.
- [3] I. Kombe and M. Özaydın, Improved Hardy and Rellich inequalities on Riemannian manifolds, Trans. Amer. Math. Soc. 361(2009), 6191-6203.
- [4] I. Kombe and A. Yener, Weighted Hardy and Rellich type inequalities on Riemannian manifolds, Math. Nachr. 289(2016) 1-11.

## RELATION-THEORETIC CONTRACTION PRINCIPLE

Aftab ALAM<sup>1</sup>, Mohammad IMDAD<sup>2</sup>

<sup>1</sup>*Department of Mathematics, Aligarh Muslim University,  
Aligarh/INDIA*

[aafu.amu@gmail.com](mailto:aafu.amu@gmail.com)

<sup>2</sup>*Department of Mathematics, Aligarh Muslim University,  
Aligarh/INDIA*

[mhimdad@gmail.com](mailto:mhimdad@gmail.com)

**Abstract:** In this presentation, we present yet another new and novel variant of classical Banach contraction principle on a complete metric space endowed with a binary relation which under universal relation reduces to Banach contraction principle. In process, we observe that various kinds of binary relations such as: partial order, preorder, transitive relation, tolerance, strict order, symmetric closure etc. utilized by earlier authors in several well-known metrical fixed point theorems can be weakened to the extent of an arbitrary binary relation.

**Keywords:** Complete metric spaces; binary relations; contraction mappings.

### References:

- [1] B. Samet, M. Turinici, "Fixed point theorems on a metric space endowed with an arbitrary binary relation and applications", *Commun. Math. Anal.* 13 (2) (2012) 82-97.
- [2] A. Stouti, A. Maaden, "Fixed points and common fixed points theorems in pseudo-ordered sets", *Proyecciones* 32 (4) (2013) 409-418.

## DYNAMICS OF A PRE-STRESSED AND IMPERFECTLY BONDED SANDWICH PLATE-STRIP CONSISTING OF ELASTIC LAYERS AND PIEZOELECTRIC CORE

Ahmet DAŞDEMİR

*Department of Mathematics, Kastamonu University,  
Kastamonu/TURKEY  
[ahmetdasdemir37@gmail.com](mailto:ahmetdasdemir37@gmail.com)*

**Abstract:** In this presentation, the dynamics of a sandwich plate-strip consisting of a piezoelectric core and elastic layers with initial stress under the action of a time-harmonic force resting on a rigid foundation is considered within the scope of the piecewise homogeneous body model with utilizing of the three dimensional linearized theory of electro-elasticity waves in initially stressed bodies. The piezoelectric core is poled along the direction perpendicular to the rigid foundation and imperfectly bonded to the elastic layers. The mathematical model corresponding to the current situation is created, and the governing system of the partial differential equations of motion is solved by employing Finite Element Method (FEM). The numerical results illustrating the effect of the different dependencies of the problem on the distribution of the stresses and the electric displacements at the interface planes between the upper and lower elastic layers and the piezoelectric core and between the plate-strip and the rigid foundation are presented. In particular, the influence of a change in the value of the shear-spring imperfectness parameter on the behavior of the corresponding parameter, i.e. the initial stress or the dimensionless frequency, is investigated.

**Keywords:** Sandwich plate-strip, initial stress, shear-spring type imperfectness, dimensionless frequency, forced vibration.

### References:

- [1] M. S. Son, Y. J. Kang, "The effect of initial stress on the propagation behavior of SH waves in piezoelectric coupled plates", *Ultrasonics*, 51(2011), 489-495.
- [2] S. D. Akbarov, N. Ilhan, "Time-harmonic Lamb's problem for a system comprising a piezoelectric layer and piezoelectric half-plane", *Journal of Sound and Vibration*, 332(2013), 5375-5392.

## TWO WEIGHTED INEQUALITIES FOR FRACTIONAL INTEGRALS ASSOCIATED WITH THE LAPLACE-BESSEL DIFFERENTIAL OPERATOR

A. EROGLU<sup>1</sup>, M. G. HAJIBAYOV<sup>2</sup>

<sup>1</sup>*Department of Mathematics, Nigde University,  
Nigde/TURKEY*

[aeroglu@nigde.edu.tr](mailto:aeroglu@nigde.edu.tr)

<sup>2</sup>*National Academy of Aviation,  
Baku/AZERBAIJAN*

[hajibayovm@yahoo.com](mailto:hajibayovm@yahoo.com)

**Abstract:** In this report it is proved that two weighted inequalities for fractional integrals  $I_{\alpha,\gamma}f$  (B-fractional integrals) associated with the

Laplace-Bessel differential operator  $\Delta_B = \sum_{i=1}^n \frac{\partial^2}{\partial x_i^2} + \sum_{j=1}^k \frac{\gamma_j}{x_j} \frac{\partial}{\partial x_j}$  (see [1]).

This result is an analog of Heinig's result [2] for the B-fractional integral. Further, the Stein-Weiss inequality for B-fractional integrals is proved as an application of this result.

The research of M. Hajibayov was partially supported by the grant of Presidium of Azerbaijan National Academy of Science 2015.

This talk is present jointly with A. Serbetci.

### References:

- [1] A. Eroglu, M.G. Hajibayov, A. Serbetci, Two weighted inequalities for B-fractional integrals, accepted in J. Inequal. Appl. 2016, 1-12.
- [2] H.P. Heinig, Weighted norm inequalities for classes of operators, Indiana Univ. Math. J. 33 (4) (1984), 573-582.

## INTEGRAL INEQUALITIES OF HERMITE-HADAMARD TYPE FOR FUNCTIONS WHOSE THIRD DERIVATIVE ABSOLUTE VALUES ARE PREINVEX

Akhilad IQBAL

*Department of Mathematics, AMU Aligarh*

Email: akhlad6star@gmail.com, akhlad.mm@amu.ac.in

**Abstract:** In this paper, we establish some new integral inequalities of Hermite-Hadamard's type for functions whose third derivative absolute values are preinvex. Applications to some special means are also considered.

**Keywords:** Hermite-Hadamard inequality, Preinvex function, Integral inequality, arithmetic mean, logarithmic mean.



## TRIGONOMETRIC APPROXIMATION IN WEIGHTED LORENTZ SPACES USING LOWER TRIANGULAR MATRICES

Ahmet Hamdi AVSAR<sup>1</sup>, Yunus Emre YILDIRIR<sup>2</sup>

<sup>1</sup>Department of Mathematics, Necatibey Education Faculty,  
Balıkesir University, Balıkesir, TURKEY  
[ahmet.avsar@balikesir.edu.tr](mailto:ahmet.avsar@balikesir.edu.tr)

<sup>2</sup>Department of Mathematics, Necatibey Education Faculty,  
Balıkesir University, Balıkesir, TURKEY  
[yildirir@balikesir.edu.tr](mailto:yildirir@balikesir.edu.tr)

**Abstract:** We investigated the approximation to  $f$  functions in weighted Lorentz spaces by the sums  $\tau_n(f, x) = \sum_{k=0}^n a_{nk} S_k(f, x)$  where  $(a_{nk})$  will denote a lower triangular regular matrices with nonnegative entries and  $S_k(f, x)$  will denote partial sums of Fourier series of  $f$ . We obtain the degree of approximation for derivatives of functions in weighted Lorentz spaces.

**Keywords:** Weighted Lorentz space, trigonometric approximation, Fourier series, Muckenhoupt weight.

### References:

- [1] Quade, E. S., "Trigonometric approximation in the mean", *Duke Math. J.*, 529-542, (1937).
- [2] Chandra, P., Trigonometric approximation of function in  $L_p$  norm, *J. Math. Anal. Appl.*, 275, (2002), 13-26.
- [3] Mittal, M.L., Rhoades, B.E., Mishra, V.N., Singh, U.: Using infinite matrices to approximate functions of  $Lip(\alpha, p)$  class using trigonometric polynomials. *J. Math. Anal. Appl.* 326, 667-676 (2007).

## CONFORMABLE FRACTIONAL INTEGRALS AND RELATED GRÜSS TYPE INTEGRAL INEQUALITIES

Ahmet Ocak AKDEMİR<sup>1</sup>, Alper EKİNCİ<sup>2</sup>, Erhan SET<sup>3</sup>

<sup>1</sup>*Department of Mathematics, Ağrı İbrahim Çeçen University,  
Ağrı/TURKEY*

[aocakakdemir@gmail.com](mailto:aocakakdemir@gmail.com)

<sup>2</sup>*Department of Mathematics, Ağrı İbrahim Çeçen University,  
Ağrı/TURKEY*

[alperekinci@hotmail.com](mailto:alperekinci@hotmail.com)

<sup>3</sup>*Department of Mathematics, Ordu University,  
Ordu/TURKEY*

[erhanset@yahoo.com](mailto:erhanset@yahoo.com)

**Abstract:** In the present note, we have given the definition of Conformable fractional integrals and some further properties. In the second part, we have established some Grüss type integral inequalities by using the bounded functions via Conformable fractional integrals.

**Keywords:** Bounded functions, Conformable fractional integrals, Grüss Inequality.

### References:

- [1] T. Abdeljawad, On conformable fractional calculus, Journal of Computational and Applied Mathematics, 279 (2015), 57-66.
- [2] R. Khalil, M. AlHorani, A. Yousef, M. Sababheh, A new definition of fractional derivative, Journal of Computational and Applied Mathematics, 264 (2014), 65-70.
- [3] Z. Dahmani, L. Tabharit, S. Taf, New Generalization of Grüss inequality using Riemann-Liouville fractional integrals Bull. Math. Anal. Appl. 2 (3) (2010), 93-99.
- [4] E. Set, A.O. Akdemir and İ. Mumcu, Grüss type inequalities for conformable fractional integrals, (submitted).

## NEW INTEGRAL INEQUALITIES FOR GEOMETRICALLY CONVEX FUNCTIONS VIA CONFORMABLE FRACTIONAL INTEGRALS

Ahmet Ocak AKDEMİR<sup>1</sup>, Merve AVCI-ARDIÇ<sup>2</sup>, Abdullatif YALÇIN<sup>3</sup>

<sup>1</sup>*Department of Mathematics, Ağrı İbrahim Çeçen University, Ağrı/TURKEY*

[aocakakdemir@gmail.com](mailto:aocakakdemir@gmail.com)

<sup>2</sup>*Department of Mathematics, Adıyaman University, Adıyaman/TURKEY*

[mavci@adiyaman.edu.tr](mailto:mavci@adiyaman.edu.tr)

<sup>3</sup>*Department of Mathematics, Ağrı İbrahim Çeçen University, Ağrı/TURKEY*

[latif.yalcin012@gmail.com](mailto:latif.yalcin012@gmail.com)

**Abstract:** In this paper, Conformable fractional derivative and Conformable fractional integrals have been introduced. Based on these definitions, a new Hadamard type integral inequality have been proved for Geometrically convex functions. Also, we have obtain a new integral identity and by using this identity, we have established some new integral inequalities for Geometrically convex functions via Conformable fractional integrals.

**Keywords:** Geometrically convex functions, Conformable fractional integrals, Hermite-Hadamard Inequality.

### References:

- [1] T. Abdeljawad, On conformable fractional calculus, Journal of Computational and Applied Mathematics, 279 (2015), 57-66.
- [2] F. Chen, Extensions of the Hermite-Hadamard Inequality for convex functions via fractional integrals, Journal of Mathematical Inequalities, 10 (1)(2016), 75-81.
- [3] Z. Dahmani, New inequalities in fractional integrals, Int. J. Nonlinear Sci. 9 (4) (2010) 493497.
- [4] Z. Dahmani, On Minkowski and Hermite-Hadamard integral inequalities via fractional integration, Ann. Funct. Anal. 1 (1) (2010) 5158.
- [5] Z. Dahmani, L. Tabharit, S. Taf, Some fractional integral inequalities, Nonlinear. Sci. Lett. A 1 (2) (2010) 155160.

## NEW RESULT IN STABILITY ANALYSIS OF SINGULAR PROBLEM

Ahu ERCAN<sup>1</sup>, Etibar S. PANAKHOV<sup>1,2</sup>

<sup>1</sup>*Department of Mathematics, Firat University,  
Elazig/TURKEY*

[ahuduman24@gmail.com](mailto:ahuduman24@gmail.com)

<sup>2</sup>*Institute of Applied Mathematics, Baku State University,  
Baku/AZERBAIJAN*

[epenahov@hotmail.com](mailto:epenahov@hotmail.com)

**Abstract:** In this study, the meaning of the stability problem is to calculate the difference of two spectral functions, solutions and potentials when finite numbers of eigenvalues of considered problems is coincided. These type problem for regular Sturm-Liouville problems was studied [1],[2]. We dealt with this type stability problem for Dirac operators in [4]. Marchenko and Maslov dealt with similar issue in the case of the spectral function coincide on given interval [2]. As far as we know, the stability problems for singular operator have not been studied. Moreover, we give a formula for expression of norming constants respect to its two spectra.

**Keywords:** Stability, Sturm-Liouville Equation, singularity.

### References:

- [1] T.I. Ryabushko, "Stability of the reconstruction of a Sturm-Liouville operator from two spectra", II. Teor. Funkts. Anal., Prilozhen., 18 (1973), 176-85. (in Russian).
- [2] V.A. Marchenko, K.V. Maslov, "Stability of the problem of reconstruction of the Sturm-Liouville operator in terms of the spectral function", Mathematics of the USSR Sbornik, 81 (1970), 525-51. (in Russian)
- [3] R. Amirov, Y. Çakmak, S. Gulyaz, "Boundary value problem for second order differential equations with Coulomb singularity on a finite interval", Indian J. Pure Appl. Math., 37 (2006), 125-140.
- [4] A. Ercan, E.S. Panakhov, "Stability of the spectral problem for Dirac operators" AIP Conference Proceedings, 1738, (2016), 290010.

## ANALYSIS OF EFFECT OF FLEXIBLE WING ON LIFT AND DRAG COEFFICIENT

Akshaya DEVI

**Abstract:** Flexible wing is an aircraft wing which is not rigid but can deform in flight. This project is intended to carry out an analysis on flexible wing as well as a rigid wing. The expected outcome is flexible wing provides better Lift and Drag Co-efficient than a rigid wing. The disadvantages of rigid wings such as increased drag, vulnerability to high speed loads and decreased performance during crosswinds are overcome by flexible wings. Flexible wings in aircrafts possess great control over tip vortices, high roll efficiency at high speed. In addition, the induced drag can be reduced which significantly improves the take-off and landing performances. Flexible wings can also be used as an alternate arrangement to cancel the adverse effect of wing tip vortices, which in turn reduces the time between two consecutive take-offs at an airport. The potential applications include all commercial and fighter airplanes which demand high maneuverability.

## ROUGH FRACTIONAL MULTILINEAR INTEGRAL OPERATORS ON GENERALIZED WEIGHTED MORREY SPACES

Ali AKBULUT

*Department of Mathematics, AhiEvrans University,  
Kirsehir/TURKEY  
aakbulut@ahievran.edu.tr*

**Abstract:** We consider generalized weighted Morrey spaces. In these spaces, we find the sufficient conditions for the boundedness of the fractional multilinear integral operators with rough kernels from one generalized weighted Morrey space to another one.

**Keywords:** generalized weighted Morrey spaces, fractional multilinear integral operator.

This work was supported by the Ahi Evran University Scientific Research Projects Coordination Unit. Project Number: **FEF.E2.16.015**

### References:

- [1] A.Akbulut, V.H.Hamzayev, Z.V. Safarov "Boundedness of rough fractional multilinear integral operators on generalized Morrey spaces", Journal of Inequalities and Applications, JIA:751 (2015), 13 pp.
- [2] A. Akbulut, V.H. Hamzayev, Z.V. Safarov "Rough fractional multilinear integral operators on generalized weighted Morrey spaces", Azerbaijan Journal of Mathematics, 6(2) (2016), 1-24.

## HYPERBOLIC SMOOTHING METHOD FOR DC PROBLEMS OBTAINED FROM CLUSTERING PROBLEMS

Ali Hakan TOR<sup>1</sup>

<sup>1</sup>*Department of Mathematics, YüzüncüYil University, Van/TURKEY*  
[hakantor@yyu.edu.tr](mailto:hakantor@yyu.edu.tr)

**Abstract:** In this study, we focused on the non-smooth unconstrained optimization problems, particularly the differences of two convex functions (DC) problems. They can be obtained from the minimum sum of square clustering (MSSC) problems [1,2]. Clustering is an important problem in data mining. In the literature, the hyperbolic smoothing technique is applied to handle nonsmoothness of optimization problems. A new hyperbolic smoothing method proposed to solve them, which made the possible to use smooth optimization algorithms for this type of non-smooth problems.

**Keywords:** Hyperbolic smoothing method, DC problem, clustering problem.

### References:

- [1] A. M. Bagirov, A. Al Nuaimat, and N. Sultanova, "Hyperbolic smoothing function method for minimax problems", *Optimization*, 62 (6): 759-782, 2013.
- [2] A. M. Bagirov, A. M. Rubinov, N. V. Soukhoroukova, and J. Yearwood, "Unsupervised and supervised data classification via nonsmooth and global optimization", *Top*, 11(1):1-93 (2003).
- [3] A. M. Bagirov and John Yearwood, "A new non-smooth optimization algorithm for minimum sum-of-squares clustering problems", *European J. Oper. Res.*, 170(2), 578-596, 2006.

## SOME APPROXIMATION PROPERTIES OF TWO DIMENSIONAL CHLODOVSKY-BERNSTEIN OPERATORS BASED ON (P, Q) INTEGER

Ali KARAIŞA<sup>1</sup>

<sup>1</sup>*Department of Mathematics- Computer Sciences, Necmettin Erbakan  
University,  
Konya/TURKEY  
[alikaisha@hotmail.com](mailto:alikaisha@hotmail.com)*

**Abstract:** In the present study, we introduce the two dimensional Chlodovskytype Bernstein operators based on  $(p, q)$ -integer. We examine approximation properties of our new operator by the help of Korovkin-type theorem. Further, we present the local approximation properties and establish the rates of convergence by means of the modulus of continuity and the Lipschitz type maximal function. Also, we give a Voronovskaja type theorem for this operator. And, we investigate weighted approximation properties of these operators and estimate rate of convergence in the same space. Finally, with the help of Maple, illustrative graphics show the rate of convergence of these operators to certain functions.

**Keywords:**  $(p, q)$ -integer, strong convergence, rate of convergence, Voronovskaja type theorem

### References:

- [1] A. Karaisa, D. T. Tolu, Y. Asar, Stancu type generalization of  $(p, q)$ -Favard-Szasz operators. *Appl. Math. Comput.* 2015, 264: 249-257.
- [2] İ. Büyükyazıcı, On the approximation properties of two-dimensional  $q$ -Bernstein-Chlodowsky polynomials. *Math. Commun.* 2009, 14, 255-269.
- [3] A. Karaisa, F. Karakoc Stancu type generalization of Dunkl analogue of Szász operators. *Adv Appl* DOI:10.1007/s00006-016-0643-41.
- [4] M. Mursaleen, Md Nasruzzaman, A. Nurgali Some approximation results on Bernstein-Schurer operators defined by  $(p, q)$ -integers. *Jour. Ineq. Appl.* 2015, 249, 1-15.
- [5] A. Karaisa Approximation by Durrmeyer type Jakimoski-Leviatan operators. *Math. Methods Appl. Sci* 2015; DOI 10.1002/mma.3650, 12.

## GAMMA TYPE GENERALIZATION SZASZ-CHARLIER OPERATORS

Ali KARAİSA, Bilal ÇAVDAR

<sup>1</sup>*Department of Mathematics- Computer Sciences, Necmettin Erbakan University,  
Konya/TURKEY*

[alikaaisa@hotmail.com](mailto:alikaaisa@hotmail.com), [bilalcavdar71@gmail.com](mailto:bilalcavdar71@gmail.com)

**Abstract:** In this paper, we define Gamma type generalization Szasz operators which involving Charlier polynomial. We also study the convergence of these operators in a weighted space of functions.

Further, we establish the local approximation properties and establish the rates of convergence by means of the modulus of continuity and the Lipschitz type maximal function. Finally, with the help of Maple, illustrative graphics show the rate of convergence of these operators to certain functions.

**Keywords:** Gamma type generalization Szasz operators, Charlier polynomial.

### References:

- [1] A. Karaisa, D. T. Töllu, Y. Asar, Stancu type generalization of Favard-Szasz operators. *Appl. Math. Comput.* 2015, 264: 249-257.
- [2] N. Ispir, Ç. Atakut, Approximation by modified Szasz-Mirakjan operators on weighted spaces, *Proc. Indian Acad. Sci. Math. Sci.* 112(4) (2002) 571-578.
- [3] A. Karaisa, F. Karakoc Stancu type generalization of Dunkl analogue of Szász operators. *Adv Appl* DOI:10.1007/s00006-016-0643-41.
- [4] Z. Walczak, On approximation by modified Szasz-Mirakjan operators, *Glas. Mat. Ser. III* 37(57) 2 (2002) 303-319.
- [5] A. Karaisa Approximation by Durrmeyer type Jakimoski-Leviatan operators. *Math. Methods Appl. Sci* 2015; DOI 10.1002/mma.3650, 12.



## MULTIPLY SOLITARY WAVE SOLUTIONS OF THE HIGHER KdV EQUATIONS IN A STRATIFIED SHEAR FLUID FLOW WITH A FREE SURFACE

Aly R. SEADAWY

*Mathematics Department, Faculty of science, Taibah University, Al-Ula, Saudi Arabia*  
[Aly7420012@yahoo.com](mailto:Aly7420012@yahoo.com)

**Abstract:** Solitary waves solutions are generated by deriving the nonlinear higher order of extended KdV equations for the free surface displacement. The problem formulations of models for internal solitary waves in a stratified shear flow with a free surface are presented. All coefficients of the nonlinear higher order extended KdV equation are expressed in terms of integrals of the modal function for the linear long-wave theory. The electric field potential and the fluid pressure in form traveling wave solutions of the extended KdV equation are obtained. The stability of the obtained solutions and the movement role of the waves by making the graphs of the exact solutions are discussed and analyzed.

**Keywords:** Internal solitary waves, Higher order of extended KdV equation, wave solutions, modified direct algebraic method.

### References:

- [1] Sarma J., Solitary wave solution of higher-order Korteweg–de Vries equation, *Chaos, Solitons and Fractals*, 39, 1 (2009) 277-281.
- [2] A. R. Seadawy, New exact solutions for the KdV equation with higher order nonlinearity by using the variational method, *Comp. and Math. Appl.* 62 (2011) 3741-3755.
- [3] Seadawy, A.R., Fractional solitary wave solutions of the nonlinear higher-order extended KdV equation in a stratified shear flow: Part I, *Comp. and Math. Appl.* 70 (2015) 345–352.

## EXTENDED TAN-COT METHOD FOR THE SOLUTIONS TO EVOLUTION EQUATIONS

Anwar Ja'afar Mohamad JAWAD

*Department of Computer Engineering Al-Rafidain University College ,  
Baghdad, Iraq  
[anwar\\_jawad2001@yahoo.com](mailto:anwar_jawad2001@yahoo.com)*

**Abstract:** The proposed extended Tan-Cot method is applied to obtain new exact travelling wave solutions to evolution equation. The method is applicable to a large variety of nonlinear partial differential equations, the Fifth-order nonlinear integrable equation, the symmetric regularized long wave equation, the higher-order wave equation of Kdv type, and Benney-Luke equation. The Extended Tan-Cot method seems to be a powerful tool in dealing with nonlinear physical models.

**Keywords:** Fifth-order nonlinear integrable equation, the symmetric regularized long wave equation (SRLW), the higher-order wave equation of Kdv type, and Benney-Luke equation (B-L)

### References:

- [1] Ali AT. New generalized Jacobi elliptic function rational expansion method. *J Comput Appl Math* 2011;235:4117–27.
- [2] Wang M. Solitary wave solutions for variant Boussinesq equations. *Phys Lett A* 1995;199:169–72.
- [3] Jawad A J M, Petkovic MD, Biswas A. Modified simple equation method for nonlinear evolution equations. *Appl Math Comput* 2010;217:869–77.
- [4] Wang M, Li X, Zhang J. The (G'/G)-expansion method and travelling wave solutions of nonlinear evolution equations in mathematical physics. *Phys Lett A* 2008;372:417–23.
- [5] Zhang J, Jiang F, Zhao X. An improved (G'/G)-expansion method for solving nonlinear evolution equations. *Int J Com Math* 2010;87(8):1716–25.
- [6] Weiss J, Tabor M, Carnevale G. The Painleve property for partial differential equations. *J Math Phys* 1983;24:522.

## STUDY OF A FOURTH-ORDER PARABOLIC EQUATION IN TIME-DEPENDENT DOMAINS

Arezki KHELOUFI<sup>1</sup>, Boubaker-Khaled SADALLAH<sup>2</sup>

<sup>1</sup>*Department of Technology, Bejaia University,  
Béjaia/ALGERIA*

[arezkinet2000@yahoo.fr](mailto:arezkinet2000@yahoo.fr)

<sup>2</sup>*Department of Mathematics, Ecole Normale Supérieure, Algiers/ALGERIA*

[sadallah@ens-kouba.dz](mailto:sadallah@ens-kouba.dz)

**Abstract:** New results on the existence, uniqueness and maximal regularity of a solution are given for a two-space dimensional fourth-order parabolic equation set in conical time-dependent domains. The study is performed in the framework of anisotropic weighted Sobolev spaces. Our method is based on the technique of decomposition of domains. Some details concerning the results given here can be found in [1].

**Keywords:** Fourth-order parabolic equations, conical domains, anisotropic weighted Sobolev spaces.

### References:

- [1] A. Kheloufi, B. K. Sadallah, "Resolution of a high-order parabolic equation in conical time-dependent domains of  $\mathbb{R}^3$ ", Arab. J. Math. Sci., Article in press.
- [2] J. L. Lions, E. Magenes, "Problèmes aux limites non homogènes et applications", Vols. 1, 2, Dunod, Paris, 1968.
- [3] B. K. Sadallah, "Etude d'un problème 2m-parabolique dans des domaines plan non rectangulaires", Un. Mat. Ital. B. (6) 2, American Journal of Computational Mathematics, 2(1983), 51-112.
- [4] B. K. Sadallah, "Study of a parabolic problem in a conical domain", Math. J. Okayama Univ., 56(2014), 157-169.

## CONVERGENCE THEOREMS OF FIXED POINTS FOR HEMICONTRACTIVE MAPPINGS IN S-PROBABILISTIC NORMED SPACES

Arife AysunKARAASLAN<sup>1</sup>, Vatan KARAKAYA<sup>2</sup>

<sup>1</sup>*Department of Mathematics, Işık University,  
İstanbul/TURKEY*

<sup>2</sup>*Department of Mathematical Engineering, Yıldız Technical University,  
İstanbul/TURKEY*

[karaaslan.aysun@gmail.com](mailto:karaaslan.aysun@gmail.com)  
[vkaya@yahoo.com](mailto:vkaya@yahoo.com)

**Abstract:** In this presentation, we study fixed point problems in S-probabilistic normed spaces. We obtain the definition of probabilistic hemicontractive mapping in a probabilistic normed space. Also, probabilistic convergence theorems of fixed points for hemicontractive mappings are proved.

**Keywords:** Probabilistic normed space, hemicontractive mapping, strong convergence, fixed point.

**Acknowledgement:** The first author was supported by TÜBİTAK- The Scientific and Technological Research Council of Turkey.

### References:

- [1] Su Y., Zhang J., "Fixed Point and Best Proximity Point Theorems for Contractions in New Class of Probabilistic Metric Spaces", Fixed Point Theory and Applications, 170, 2014.
- [2] Xu Y., Guan J., Su Y., "Weak and Strong Convergence Theorems of Fixed Points for Nonexpansive Mappings and Strongly Pseudocontractive Mappings in a New Class of Probabilistic Normed Spaces", Fixed Point Theory and Applications, 2015.
- [3] Shrivastava R., Rajput A., Singh S.K., "Iteration Process for Hemicontractive Mappings on Hilbert Spaces", IMACST, 3, 2012, 199-201.

## COLLOCATION METHOD USING RADIAL BASIS FUNCTION FOR SOLUTION OF FRACTIONAL CKdV EQUATION

Asif YOKUŞ<sup>1</sup>, Sema Gülbahar<sup>2</sup>

<sup>1</sup>Department of Actuary, Firat University, Elazığ/TURKEY  
[asfyokus@yahoo.com](mailto:asfyokus@yahoo.com)

<sup>2</sup>Department of Mathematics, İstanbul Commerce University, İstanbul/TURKEY  
[semaakkus\\_mat@hotmail.com](mailto:semaakkus_mat@hotmail.com)

**Abstract:** In this paper, collocation method using radial basis functions is applied to solution of fractional compound KdV differential equation. In the solution process, we will use linearization technique for non-linear term existing in the equation.  $L_2$  and  $L_\infty$  error norms are calculated with mathematica program to compare the approximate solution with exact solution.

**Keywords:** Radial basis functions, Collocation method, Linearization technique.

### References:

- [1] W.G.Zhang, Y.Zhao, X.Y. Teng, "An approximate Damped Oscillatory Solutions for Compound KdV-Burgers Equation and Their Error", ActaMath.Appl. Sin., 28 (2012), 305-324.
- [2] B. Lie, Y.Chen, H. Zhang, "Auto-Bäcklund transformation and exact solutions for compound KdV-type and compound KdV-Burgers type equations with nonlinear terms of any order", Phys. Lett. A, 305 (2002), 372-382.
- [3] X. Zheng, T. Xia, H. Zhang, "New Exact Traveling Wave Solutions for Compound KdV-Burgers Equations in Mathematical Physics", Appl. Math. E-Notes, 2 (2002), 45-50.

## HILBERT TRANSFORM ON LOCAL MORREY-LORENTZ SPACES

Ayhan ŞERBETÇİ

*Department of Mathematics, Ankara University,  
Ankara/TURKEY  
serbetci@ankara.edu.tr*

**Abstract:** In this talk we introduce a new class of functions called local Morrey-Lorentz spaces  $M_{p,q;\lambda}^{loc}$ ,  $0 < p, q \leq \infty$  and  $0 \leq \lambda \leq 1$ . These spaces generalize Lorentz spaces such that  $M_{p,q;0}^{loc} = L_{p,q}$ . We show that in the case  $\lambda < 0$  or  $\lambda > 1$  the space  $M_{p,q;\lambda}^{loc}$  is trivial, and in the limiting case  $\lambda = 1$  the space  $M_{p,q;\lambda}^{loc}$  is the classical Lorentz space  $\Lambda_{\infty,t^{1/p-1/q}}$ .

We prove that for  $0 < q \leq p < \infty$  and  $0 < \lambda \leq q/p$ , the local Morrey-Lorentz spaces  $M_{p,q;\lambda}^{loc}$  are equal to weak Lebesgue spaces  $WL_{1/p-\lambda/q}$ . Furthermore, we obtain the boundedness of the Hilbert transform in the local Morrey-Lorentz spaces.

**Keywords:** Morrey spaces, Lorentz spaces, local Morrey-Lorentz spaces, Hilbert transform.

### References:

- [1] D.R. Adams, A note on Riesz potentials, *Duke Math. J.*, 42, (1975), 765-778.
- [2] K.F. Andersen and B. Muckenhoupt, Weighted weak type Hardy inequalities with applications to Hilbert transforms and maximal functions, *Studia Math.*, 72 (1982), 9–26.
- [3] C. Aykol, V.S. Guliyev and A. Serbetci, Boundedness of the maximal operator in the local Morrey-Lorentz spaces, *Jour. Inequal. Appl.*, 2013, 2013:346.
- [4] C. Aykol, V.S. Guliyev, A. Kucukaslan and A. Serbetci, The boundedness of Hilbert transform in the local Morrey-Lorentz spaces, *Integral Transform. Spec. Funct.*, <http://dx.doi.org/10.1080/10652469.2015.1121483>
- [5] C. Bennett and R. Sharpley, *Interpolation of Operators*, Academic Press, Boston, 1988.
- [6] G.G. Lorentz, Some new function spaces, *Annals of Mathematics*, 51 (1950), 37--55.

## SOME IDENTITIES ASSOCIATED WITH HURWITZ-LERCH ZETA FUNCTION

Aykut Ahmet AYGÜNEŞ<sup>1</sup>

<sup>1</sup>*Department of Mathematics,  
Antalya/TURKEY*

[aykutahmet1981@hotmail.com](mailto:aykutahmet1981@hotmail.com)

**Abstract:** In this paper, we firstly introduce a special integral representation associated with Hurwitz-Lerch zeta function. By using this integral representation, we obtain some functional equations for a special case of the Hurwitz-Lerch zeta function, Also we give some remarks for this identities.

**Keywords:** Hurwitz-Lerch zeta function, Hurwitz zeta function, Riemann zeta function, Leibniz derivative formula.

### References:

- [1] A. Erdélyi, Higher Transcendental Functions, vol. 1, New York: McGraw-Hill, 1955.
- [2] A. Erdélyi, W. Magnus, F. Oberhettinger, F. G. Tricomi, Higher Transcendental Functions, vol. 1, McGraw-Hill Book Company, New York, Toronto and London, 1953.
- [3] E. C. Titchmarsh, The Theory of the Riemann-zeta function, Oxford University (Clarendon) Press, Oxford and London, 1951; Second Edition (Revised by D. R. Heath-Brown), 1986.
- [4] H. M. Srivastava, J. Choi, Series Associated with the Zeta and Related Functions, Kluwer Academic Publishers, Dordrecht, Boston and London, 2001.
- [5] H. M. Srivastava, Some properties and results involving the zeta and associated functions, Functional Analysis, Approximation and Computation 7 (2), 89-133 (2015).
- [6] T. M. Apostol, Introduction to Analytic Number Theory, Springer-Verlag, New York, Heidelberg and Berlin, 1976.

## APPROXIMATION BY TWO DIMENSIONAL GENERALIZED SZASZ OPERATORS

Aynur N. MAMMADOVA

*Institute of Mathematics and Mechanics of NAS of Azerbaijan,  
Baku/AZERBAIJAN*

**Abstract:**We study approximation theorem for generalized Szasz operator in space a higher order, differentiable weighted continuous functions.

Suppose that  $C^{r+2}([0, \infty) \times [0, \infty))$  is a space of  $r$  time continuous and differentiable functions is bisemi-axis  $([0, \infty) \times [0, \infty))$  and  $f \in C^{r+2}([0, \infty) \times [0, \infty))$ . Let us consider the following Szasz operator for  $f \in C^{r+2}([0, \infty) \times [0, \infty))$

$$S_{n,m,r}(f; x, y) = e^{-nx-my} \sum_{k=0}^{\infty} \sum_{l=0}^{\infty} \sum_{i=0}^r [(x - \frac{k}{n}) \frac{\partial}{\partial x} + (y - \frac{l}{m}) \frac{\partial}{\partial y}]^i f(\frac{k}{n}, \frac{l}{m}) \frac{(nx)^k}{k!} \frac{(ml)^l}{l!}$$

**Theorem.**For  $f \in C^{r+2}([0, \infty) \times [0, \infty))$  the following equality is true

$$S_{n,m,r}(f; x, y) = f(x, y) + \frac{(-1)^r f^{(r+1)}(x, y) T_{r+1}(x, y)}{(r+1)!} + \frac{(-1)^r (r+1) f^{(r+2)}(x, y) T_{r+2}(x, y)}{(r+2)!} + \frac{\rho_{n,m,r}(x, y)}{(nm)^{r/4}},$$

where

$$\lim_{n,m \rightarrow \infty} \rho_{n,m,r}(x, y) = 0.$$

### References:

- [1] G. H. Kirov, A Generalization of the Bernstein polynomials, Math. Balkanica 6 (1992), 147-153.



## SOME PROPERTIES OF DOUBLE SEQUENCES AND THE $P$ -CONVERGENCE OF A DOUBLY-SEQUENCE ITERATION WITH ERROR TERMS IN CAT(0) SPACES

Aynur ŞAHİN<sup>1</sup>, Metin BAŞARIR<sup>1</sup>, Richard F. PATTERSON<sup>2</sup>

<sup>1</sup>*Department of Mathematics, Sakarya University,  
Sakarya, 54050, TURKEY*

[ayuce@sakarya.edu.tr](mailto:ayuce@sakarya.edu.tr), [basarir@sakarya.edu.tr](mailto:basarir@sakarya.edu.tr)

<sup>2</sup>*Department of Mathematics and Statistics, University of North Florida,  
Jacksonville, Florida, 32224, USA*

[rpatters@unf.edu](mailto:rpatters@unf.edu)

**Abstract:** In this presentation, we obtain some properties related to double sequences. Moreover, we prove the  $P$ -convergence of the Halpern-type double-sequence iteration process with error terms in a CAT(0) space and present an example to support this result. Our results extend and improve some recent results announced in the current literature.

**Keywords:** Double sequence, iteration process, fixed point, nonexpansive mapping,  $P$ -convergence, CAT(0) space.

### References:

- [1] A. Cuntavepanit, B. Panyanak, "Strong convergence of modified Halpern iterations in CAT(0) spaces", *Fixed Point Theory Appl.*, 2011, Article ID 869458, 11 pages (2011).
- [2] A. El-Sayed Ahmed, A. Kamal, "Construction of fixed points by some iterative schemes", *Fixed Point Theory Appl.*, 2009, Article ID 612491, 17 pages (2009).
- [3] A. Pringsheim, "Zur Theorie der zweifach unendlichen Zahlenfolgen", *Math. Ann.*, 53(1900), 289-321.
- [4] C. Moore, "A double-sequence iteration process for fixed points of continuous pseudocontractions", *Comput. Math. Appl.*, 43(2002), 1585-1589.
- [5] M. Bridson, A. Haefliger, "Metric spaces of non-positive curvature", Springer, Berlin (1999).
- [6] R. F. Patterson, "Analogues of some fundamental theorems of summability theory", *Int. J. Math. Math. Sci.*, 23(2000), 1-9.

## MEASURE OF NONCOMPACTNESS AND FRACTIONAL DIFFERENTIAL EQUATIONS IN BANACH SPACE

Aysun SOYSAL<sup>1</sup>, Vatan KARAKAYA<sup>2</sup>

<sup>1</sup>*Department of Mathematical Engineering, Yıldız Technical University,  
İstanbul/TURKEY*

[aysunsoysal90@gmail.com](mailto:aysunsoysal90@gmail.com)

<sup>2</sup>*Department of Mathematical Engineering, Yıldız Technical University,  
İstanbul/TURKEY*

[vkkaya@yahoo.com](mailto:vkkaya@yahoo.com)

**Abstract:** In this paper, we study the existence of solutions for a class of initial value problems for fractional differential equations involving Caputo fractional derivative in Banach space. The arguments are based upon Mönch's fixed point theorem and the technique of measures of noncompactness.

**Keywords:** Initial value problem, Caputo fractional derivative, measure of noncompactness, fixed point, Banach space.

### References:

- [1] R. P. Agarwal, M. Benchohra and S. Hamani, Boundary value problems for differential inclusion with fractional order, *Adv. Stud. Contemp. Math.* **12** (2008), 181-196.
- [2] Banas, J. and Goebel, K. (1980) *Measure of Noncompactness in Banach Spaces*. Lecture Notes in Pure and Applied Mathematics, Dekker, New York.
- [3] R. P. Agarwal, M. Meehan and D. O'Regan, *Fixed Point Theory and Applications*, Cambridge University Press, Cambridge, 2001.
- [4] R. R. Akhmerow, M. I. Kamenskii, A. S. Patapov, A. E. Rodkina and B. N. Sadovskii, *Measures of Noncompactness and Condensing Operators*, trans. from the Russian by A. Iacob, BirkhauserVerlag, Basel, 1992.

## A RELIABLE COMPUTATIONAL METHOD for SINGULAR PROBLEMS

Ayşe Betül KOÇ<sup>1</sup>

<sup>1</sup>*Department of Mathematics, Selcuk University,  
Konya/TURKEY*

[aysebetulkoc@selcuk.edu.tr](mailto:aysebetulkoc@selcuk.edu.tr)

**Abstract:** In this presentation, a new numerical algorithm is established for singular initial value problems. The solutions are constructed in the series form of the Fibonacci polynomials. The efficiency and validity of the approach are illustrated with few numerical examples.

**Keywords:** Pseudo-spectral approach, Fibonacci polynomials.

### References:

- [1] A. B. Koc, M. Cakmak, A. Kurnaz, K. Uslu, "A new Fibonacci type collocation procedure for boundary value problems", *Advances in Difference Equations*, 262: 2013 (2013).
- [2] A. B. Koc, M. Cakmak, A. Kurnaz, "A matrix method based on the Fibonacci polynomials to the generalized pantograph equations with functional arguments", *Advances in Mathematical Physics* Article ID: 694580 (2014).
- [3] A. B. Koc, A. Kurnaz, "An efficient approach for solving telegraph equation", *AIP Conf. Proc.*, 1648, 370006 (2015).

## EKELAND'S VARIATIONAL PRINCIPLE AND ITS APPLICATION TO EQUILIBRIUM PROBLEMS

Azadeh HOSSEINPOUR<sup>1</sup>, Somyot PLUBTIENG<sup>2</sup>, Ali FARAJZADEH<sup>3</sup>

<sup>1,2</sup>*Department of Mathematics, Faculty of Science, Naresuan University, Phitsanulok 65000, THAILAND.*

[azadeh.hoseinpour@hotmail.com](mailto:azadeh.hoseinpour@hotmail.com), [somyotp@nu.ac.th](mailto:somyotp@nu.ac.th)

<sup>3</sup>*Department of Mathematics, Razi University, Kermanshah, 67149, Iran.*

[farajzadehali@gmail.com](mailto:farajzadehali@gmail.com)

**Abstract:** In this study, we obtain a generalization of vectorial form of Ekeland's variational principle for set valued mapping in Banach space. We get some equivalent results to the mentioned variational principle. As an application of our work, we provide some existence results for equilibrium problems in compact and noncomplete spaces.

**Keywords:** Ekeland's variational principle, Equilibrium problems, Set valued mappings, Scalarization function, Banach space.

### References:

- [1] G.Y. Chen, X.X. Huang, "Ekeland's  $\varepsilon$ -variational principle for set-valued mapping", *Mathematical Methods of Operations Research*. 48 (1998) 181-186.
- [2] S.J. Li, X.Q. Yang, G.Y. Chen, "Vector Ekeland variational principle, in: F Giannessi (Ed.), *Vector Variational Inequalities and Vector Equilibria*", Kluwer Academic Publishers, (2000), 321-333.
- [3] J. Zeng, S.J. Li, "An Ekeland's variational principle for set-valued mappings with applications", *Journal of Computational and Applied Mathematics*, 230 (2009), 477-484.

## DYNAMIC EVOLUTION OF DAMAGE AND FRICTION IN PIEZOELECTRIC MATERIALS

Abdelaziz AZEB AHMED<sup>1</sup>, Tedjani HADJ AMMAR<sup>2</sup>

<sup>1</sup>*Department of Mathematics, University of El Oued /ALGERIA*

[aziz-azebahmed@univ-eloued.dz](mailto:aziz-azebahmed@univ-eloued.dz)

<sup>2</sup>*Department of Mathematics, University of El Oued /ALGERIA*

[hat\\_olsz@yahoo.com](mailto:hat_olsz@yahoo.com)

**Abstract:** We consider a dynamic frictional contact problem between a piezoelectric body and an obstacle. The contact is bilateral, and the friction is modeled with Tresca's friction law. The material's behavior is described by a nonlinear electro-viscoelastic constitutive law with damage. We derive a variational formulation for the model which is in the form of a system involving the displacement field, the electric potential field, and the damage field. Then we provide the existence of a unique weak solution to the model. The proofs are based on the classical result of nonlinear first order evolution inequalities, the equations with monotone operators and the fixed point arguments.

**Keywords:** Dynamic process, piezoelectric material with damage, frictional contact, existence and uniqueness, weak solution, fixed point.

### References:

- [1] A. Azeb Ahmed, S. Boutechebak, "Analysis of a dynamic electro-elastic-viscoplastic contact problem", *Wulfenia Journal Klagenfurt Austria*, Vol 20, No. 3 (2013), 43-63.
- [2] P. Bisenga, F. Lebon, F. Maceri, "The unilateral frictional contact of a piezoelectric body with a rigid support", In: Martins, J.A.C., Monteiro Marques, M.D.P. (eds.) *Contact Mechanics*,. Kluwer, Dordrecht (2002), 347-354.
- [3] A. Dorfmann, K.N.G. Fuller, R.W. Ogden, Shear, compressive and dilatational response of rubberlike solids subject to cavitation damage, *Internat. J. Solids Structures* 39 (2002) 1825-1857.
- [4] T. Hadj ammar, B. Benyattou, S. Drabla, "A dynamic contact problem between elasto-viscoplastic piezoelectric bodies", *Electron. J. Qual. Theory Difer. Equ.* No. 49. (2014), 1-21.
- [5] T. Ikeda, *Fundamentals of Piezoelectricity*, Oxford University Press, Oxford (1990).

## BACKWARD DOUBLY SDES AND SPDES WITH SUPERLINEAR GROWTH GENERATORS

Badreddine MANSOURI

*Université Mohamed Khider, BP 145, 07000 Biskra*

[mansouri.badreddine@gmail.com](mailto:mansouri.badreddine@gmail.com)

**Abstract:** We deal with multidimensional backward doubly stochastic differential equations (BDSDEs) with a superlinear growth generator and a square integrable terminal datum. We introduce new local conditions on the generator then we show that they ensure the existence and uniqueness as well as the stability of solutions. Our work goes beyond the previous results on the subject. Although we are focused on multidimensional case, the uniqueness result we establish is new in one dimensional too. As application, we establish the existence and uniqueness of probabilistic solutions to semilinear stochastic partial differential equations (SPDEs) with superlinear growth generator. By probabilistic solution, we mean a solution which is representable throughout a BDSDEs.

## SUBORBITAL GRAPHS FOR THE RESIDUE CLASS OF $PSL(2, Z_n)$

Murat BEŞENK<sup>1</sup>, Bahadır Özgür GÜLER, Tuncay KÖR<sup>1</sup>

<sup>1</sup>*Department of Mathematics, Karadeniz Technical University,  
Trabzon/TURKEY*

[mbesenk@ktu.edu.tr](mailto:mbesenk@ktu.edu.tr), [boguler@ktu.edu.tr](mailto:boguler@ktu.edu.tr), [tkor@ktu.edu.tr](mailto:tkor@ktu.edu.tr),

**Abstract:** For each integer  $n \geq 2$ , let  $Z_n$  denote the ring of integers  $\text{mod } n$ ; then the  $2 \times 2$  unimodular matrices with coefficients in  $Z_n$  form a group  $SL(2, Z_n)$  in which the matrices  $\{\pm I\}$  form a normal subgroup. The natural ring-epimorphism  $Z \rightarrow Z_n$ ,  $a \mapsto [a]$ , induces a group-homomorphism  $SL(2, Z) \rightarrow SL(2, Z_n)$  and also it is known that dividing  $SL(2, R)$  by its center  $\{\pm I\}$  we get the group  $PSL(2, R) \cong SL(2, R)/\{\pm I\}$ . Hence this in turn induces a group-homomorphism  $\phi_n$  from  $PSL(2, Z)$  to  $PSL(2, Z_n)$ . In this paper, we investigate some properties of suborbital graphs for the  $PSL(2, Z_n)$  group. We obtain edge-circuit conditions and also we find some relations between for the  $M$  dessin associated with  $\Gamma(n)$ .

**Keywords:** Suborbital graphs, orbit, circuit, dessin, imprimitive action.

### References:

- [1] M.Akbaş, "On Suborbital Graphs For The Modular Group", Bull. London Math. Soc. 33,647-652, (2001).
- [2] G.A. Jones, D. Singerman, K. Wicks "The Modular Group and Generalized Farey Graphs", London Math. Soc. 160, 316-338 (1991).
- [3] B.Ö.Güler, M.Beşenk, A.H.Değer, S.Kader "Elliptic Elements and Circuits in Suborbital Graphs", Hacettepe Journal of Mathematics and Statistics, 40(2)203-210 (2011).
- [4] B.Schoeneberg, "Elliptic Modular Functions", Springer, Berlin, (1974).
- [5] M.Beşenk, "Suborbital Graphs For a Special Subgroup of The  $SL(3, Z)$ ", Filomat, 30(3)593-602 (2016).
- [6] R. Diestel, "Graph Theory", Springer-Verlag, (2010).

## A NEW RESULT ON GENERALIZED ABSOLUTE MATRIX SUMMABILITY

Hikmet Seyhan ÖZARSLAN <sup>1</sup>, Bağdagül KARTAL <sup>2</sup>

<sup>1</sup>*Department of Mathematics, Erciyes University,  
Kayseri/TURKEY*  
[seyhan@erciyes.edu.tr](mailto:seyhan@erciyes.edu.tr)

<sup>2</sup>*Department of Mathematics, Erciyes University,  
Kayseri/TURKEY*  
[bagdaqulkartal@erciyes.edu.tr](mailto:bagdaqulkartal@erciyes.edu.tr)

**Abstract:** In this presentation, we have generalized a known result dealing with the  $\left| \bar{N}, p_n \right|_k$  summability to the  $\varphi - \left| A, p_n \right|_k$  summability by using the concepts of almost increasing and  $\delta$ -quasi-monotone sequences. We also obtain some new and known results.

**Keywords:** Almost increasing sequences, absolute matrix summability, quasi-monotone sequences, infinite series, Hölder inequality, Minkowski inequality.

### References:

- [1] G. H. Hardy, "Divergent Series", Oxford University Press, Oxford, 1949.
- [2] H. Bor, "On two summability methods", Math. Proc. Cambridge Philos. Soc., 97(1985), 147-149.
- [3] H. Bor, "On the relative strength of two absolute summability methods", Proc. Amer. Math. Soc., 113(1991), 1009-1012.
- [4] H. Bor, "On quasi-monotone sequences and their applications", Bull. Austral. Math. Soc., 43(1991), 187-192.
- [5] H. Bor, "An application of almost increasing and  $\delta$ -quasi-monotone sequences", J. Inequal. Pure Appl. Math., 1(2000), no 2, Article 18, 6 pp.



## ON REFLEXIVITY OF THE BOCHNER SPACE $L^p(\mu, E)$ FOR ARBITRARY $\mu$

Banu AY TAR GÜNTÜRK<sup>1</sup>, Bahaettin CENGİZ<sup>2</sup>

<sup>1</sup>*Faculty of Engineering, Baskent University,  
Ankara/TURKEY*

[bgunturk@baskent.edu.tr](mailto:bgunturk@baskent.edu.tr)

<sup>2</sup>*Faculty of Engineering, Baskent University,  
Ankara/TURKEY*

[bcengiz@baskent.edu.tr](mailto:bcengiz@baskent.edu.tr)

**Abstract:** Let  $\mu$  be a finite positive measure,  $E$  a Banach space, and  $1 < p < \infty$  a real number.

(a) It is known that the Bochner space  $L^p(\mu, E)$  is reflexive if and only if  $E$  is reflexive;

(b) it is also known that  $\mathcal{L}(L^1(\mu), E) \simeq L^\infty(\mu, E)$  if and only if  $E$  has the Radon-Nikodým property (RNP), (where for two Banach spaces  $E, F$ ,  $E \simeq F$  means that they are isometric, and  $\mathcal{L}(E, F)$  denotes the Banach space of all bounded operators from  $E$  to  $F$ .)

In this article we prove that both statements almost hold for any arbitrary positive measure  $\mu$  as well, more precisely, if  $\nu$  is the so-called perfect equivalent of  $\mu$ , (i.e., for each  $1 \leq p < \infty$ ,  $\nu$  is perfect and they have the same  $L^p$  spaces), we have,

(a') for  $1 < p < \infty$ ,  $L^p(\mu, E) \simeq L^p(\nu, E)$  is reflexive if and only if  $E$  is reflexive,

(b')  $\mathcal{L}(L^1(\mu), E) \simeq \mathcal{L}(L^1(\nu), E) \simeq L^\infty(\nu, E)$  if and only if  $E$  has the RNP.

**Keywords:** Reflexivity, Radon-Nikodým property, Bochner space, isometry, perfect measure.

### References:

- [1] J. Diestel and J. Jr. Uhl, Vector Measures, Mathematical Surveys and Monographs, American Mathematical Society, Providence, RI, 15(1977).
- [2] Dinculeanu, Vector Measures, Pergamon Press, New York, 1967.

## CERTAIN HERMITE-HADAMARD TYPE INEQUALITIES ASSOCIATED WITH CONFORMABLE FRACTIONAL INTEGRAL OPERATORS

Erhan SET<sup>1</sup>, Barış ÇELİK<sup>2</sup>

<sup>1</sup>*Department of Mathematics, Ordu University,  
Ordu/TURKEY*

[erhanset@yahoo.com](mailto:erhanset@yahoo.com)

<sup>2</sup>*Department of Mathematics, Ordu University,  
Ordu/TURKEY*

[bariscelik15@hotmail.com](mailto:bariscelik15@hotmail.com)

**Abstract:** The aim of this article is to obtain some new Hermite-Hadamard type inequalities for convex functions via conformable fractional integral. The results presented here would provide extensions of those given in earlier works.

**Keywords:** Convex function, Hermite-Hadamard inequality, conformable fractional integral.

### References:

- [1] S. Belarbi, Z. Dahmani, "On some new fractional integral inequalities", *J. Ineq. Pure Appl. Math.*, 10(3) (2009), Art. 86.
- [2] Z. Dahmani, "New inequalities in fractional integrals", *Int. J. Nonlinear Sci.*, 9(4) (2010), 493-497.
- [3] S. Miller, B. Ross, "An introduction to the Fractional Calculus and Fractional Differential Equations", John Wiley. Soons. USA., 1993.
- [4] M.Z. Sarıkaya, E. Set, H. Yaldiz, N. Başak, "Hermite-Hadamard's inequalities for fractional integrals and related fractional inequalities", *Math. Comput. Model.*, 57 (2013), 2403-2407.
- [5] D.-P. SHI, B.-Y. XI and F. QI, "Hermite-Hadamard type inequalities for Reimann-Liouville fractional integrals of  $(\alpha; m)$ -convex functions", *Fractional Differential Calculus*, 4(1) (2014), 31-43.
- [6] E. Set, A.O. Akdemir, İ. Mumcu, "Hadamard's inequality and its extensions for conformable fractional integrals of any order  $\alpha > 0$ ", Submitted.

## SHOCK AND RAREFACTION WAVES FOR BURGERS MODELS ON SPACETIME GEOMETRIES COMPARISON AND ANALYSIS

Baver OKUTMUŞTUR

*Department of Mathematics, Middle East Technical University (METU),  
Ankara/TURKEY*  
[baver@metu.edu.tr](mailto:baver@metu.edu.tr)

**Abstract:** The relativistic Burgers model has recently been derived on flat geometry, developed and generalized to several spacetime backgrounds such as Schwarzschild, Friedmann-Lemaitre-Robertson-Walker (FLRW), de Sitter (dS), anti-de Sitter (AdS), Schwarzschild-de Sitter (SdS) and Schwarzschild-anti de Sitter (SAdS) spacetimes. In this work we consider these spacetime geometries in order to analyze the derived Burgers models and their finite volume solutions containing shock/rarefaction waves both theoretically and numerically. To this end, we establish a second-order Godunov-type finite volume scheme to the relativistic models for approximation of discontinuous solutions and compare each model of interest by illustrating shock and rarefaction wave propagations.

**Keywords:** Spacetime, Euler equations, relativistic Burgers models, finite volume approximation, shock waves, rarefaction waves, Godunov scheme.

### References:

- [1] T. Ceylan, B. Okutmustur, "Finite Volume Method for the Relativistic Burgers Model on a (1+1)-Dimensional de Sitter Spacetime", *Math. Comput. Appl.*, 21(2016), 16.
- [2] T. Ceylan, P.G.LeFloch, B. Okutmustur, "The relativistic Burgers equation on an FLRW background and its finite volume approximation", arXiv preprint arXiv:1512.08142v1 (2015).
- [3] P.G. LeFloch, H. Makhlof, B. Okutmustur, "Relativistic Burgers equations on a curved spacetime. Derivation and finite volume approximation", *SIAM J. Num. Anal.* 2012, 50(2012). 2136-2158.
- [4] B. Okutmustur, T. Ceylan, "Relativistic Burgers equation on a de Sitter background. Derivation of the model and finite volume approximations", *Int. J. Pure Math.* 2 (2015), 21–29.

## ON FLOQUET SOLUTIONS FOR DISCRETE STURM-LIOUVILLE PROBLEM WITH PERIODIC GENERALIZED FUNCTION POTENTIALS

Manaf MANAFOV<sup>1</sup>, Bayram BALA<sup>2</sup>, Abdullah KABLAN<sup>2</sup>

<sup>1</sup>*Department of Mathematics, Adiyaman University,  
Adiyaman/TURKEY*

[mmanafov@adiyaman.edu.tr](mailto:mmanafov@adiyaman.edu.tr)

<sup>2</sup>*Department of Mathematics, Gaziantep University,  
Gaziantep/TURKEY*

[bayrambala27@gmail.com](mailto:bayrambala27@gmail.com), [kablan@gantep.edu.tr](mailto:kablan@gantep.edu.tr)

**Abstract:** Floquet theory plays a central role for Sturm-Liouville problem and difference equations with periodic potentials. This theory for Sturm-Liouville problem and with generalized function potential are studied in [2] and [3] respectively. Floquet solutions for periodic systems and for Hill difference equation have been investigated in [4] and [1]. In this study, we obtain Floquet solutions for discrete Sturm-Liouville problem with periodic generalized function potentials.

**Keywords:** Sturm-Liouville equation, difference equation, Floquet theory.

### References:

- [1] Ag. Kh. Khanmamedov, "On Floquet Solutions to Hill Difference Equation" Dokl. Nats. Akad. Nauk. Azerb., 59 (2003), no:3-4, 9-15 (in Russian).
- [2] Guseinov, G. Sh., "On a quadratic pencil Sturm-Liouville operators with periodic coefficients", Vesnik Moskov Univ.-Ser. 1 Math. Mekh., 3 (1984), 14-21.
- [3] M. Dzh. Manafov and A. Kablan, "Eigenfunction expansions of a quadratic pencil of differential operators with periodic generalized potential," Electronic Journal of Qualitative Theory of Differential Equations, 76 (2013), 1-11.
- [4] M. Toda, Theory of Nonlinear Lattices, Springer, Berlin, (1988).

## A NONLINEAR HYPERBOLIC PROBLEM FOR VISCOELASTIC EQUATIONS

\*Benabdderrahmane BENYATTOU , \*\*Rahmoune ABITA

\* Faculty of Mathematics and Computer Sciences, University of M'Sila, Algeria.

[bbenyattou@yahoo.com](mailto:bbenyattou@yahoo.com)

\*\* Laboratory of Computer Sciences and Mathematics, University Amar Telidji

Laghouat, Algeria. [rahmouneabita@yahoo.fr](mailto:rahmouneabita@yahoo.fr)

**Abstract:** In this paper, we consider a nonlinear hyperbolic problem for viscoelastic equations with a source term. By basing on Faedo-Galerkin approximations and compactness argument, this work is devoted to prove the existence, uniqueness, and also continuous dependence with respect to the initial data of solutions.

**Keywords:** Compactness method, continuous dependence, local existence, nonlinear hyperbolic equation, viscoelastic bodies.

## PROJECTED TIKHONOV REGULARIZATION METHOD FOR FREDHOLM INTEGRAL EQUATIONS OF THE FIRST KIND

Boussetila NADJIB

Department of Mathematics, U. Guelma, Algeria

[n.boussetila@gmail.com](mailto:n.boussetila@gmail.com)

**Abstract:** In this talk, we consider a variant of projected Tikhonov regularization method for solving Fredholm integral equations of the first kind. We give the theoretical analysis of this method in the Hilbert space  $L_2(a, b)$  setting, and we establish some convergence rates under certain regularity on the exact solution and the kernel  $k(.,.)$ . Some numerical results are also presented.

**Keywords:** ill-posed problems, integral equation of the first kind, projected Tikhonov regularization method.

### References:

- [1] Groetsch, CW: Tikhonov regularization for integral equations of the first kind. Pitman (1984)
- [2] Groetsch, CW, Neubauer, A: Regularization of Ill-Posed Problems: Optimal Parameter Choice in Finite Dimensions, Journal of Approximation Theory 58, 184-200 (1989)

## ON SOME INTEGRAL INEQUALITIES ON TIME SCALES AND APPLICATIONS

Boukerrioua KHALED

**Abstract:** The goal of this paper is to derive some generalizations and re-nements of certain inequalities of Pachpatte type and Bellman-Bihari type, on time scales, using elementary analytic methods. The given results unify continuous and discrete inequalities and extend some known results in the literature. To show the feasibility of the obtained inequalities, some illustrative examples are also introduced.

## SINGULAR QUASILINEAR ELLIPTIC SYSTEMS WITH (SUB-, SUPER-) HOMOGENEOUS CONDITION

Brahim KHODJA<sup>1</sup>, Hana DIDI<sup>2</sup> and Abdelkrim MOUSSAOUI<sup>3</sup>

<sup>1</sup>Mathematic Department, Badji-Mokhtar Annaba University,  
23000 Annaba Algeria  
[brahim.khodja@univ-annaba.org](mailto:brahim.khodja@univ-annaba.org)

<sup>2</sup>Mathematic Department, Badji-Mokhtar Annaba University,  
23000 Annaba Algeria  
[hana.di@hotmail.fr](mailto:hana.di@hotmail.fr)

<sup>3</sup>Biology Department, A. Mira Bejaia University,  
TargaOuzemour 06000 Bejaia, Algeria  
[abdelkrim.moussaoui@univ-bejaia](mailto:abdelkrim.moussaoui@univ-bejaia)

**Abstract:**In this talk we establish existence, nonexistence and regularity of positive solutions for a class of singular quasilinear elliptic systems subject to (sub-, super-) homogeneous condition. The approach is based on sub-supersolution methods for systems of quasilinear singular equations combined with perturbation arguments involving singular terms.

**Keywords:** Singular system; p-Laplacian; Sub-supersolution; Schauder's fixed point Theorem; regularity.

### References:

- [1] C.O. Alves & .F.J.S.A. Corrêa, On the existence of positive solution for a class of singular systems involving quasilinear operators, Appl Math Comput. 185 (2007), 727-736.
- [2] G. Astarita, G. Marrucci. Principles of non-Newtonian fluid mechanics. McGraw-Hill, 1974.
- [3] S. Carl, V. K. Le & D. Motreanu, Nonsmoothvariational problems and their inequalities. Comparaison principles and applications, Springer, New York, 2007.
- [4] P. Clément, J. Fleckinger, E. Mitidieri and F. de Thelin, Existence of Positive Solutions for a NonvariationalQuasilinear Elliptic System, J. Diff. Eqts. 166 (2000), 455-477.
- [5] A. Moussaoui, B. Khodja& S. Tas, A singular Gierer-Meinhardt system of elliptic equations in  $R^N$  Nonlinear Anal. 71 (2009), 708-716.

## A NOTE APOSTOL TYPE (P,Q)-FROBENIUS-EULER POLYNOMIALS

Burak KURT

Department of Mathematics, Akdeniz University, Antalya/TURKEY

[burakkurt@akdeniz.edu.tr](mailto:burakkurt@akdeniz.edu.tr)

**Abstract:** In this work, we define and introduce a new kind of the Apostol type Frobenius-Euler polynomials based on the  $(p,q)$ -calculus and investigate their some properties, recurrence relationships and so on. We give some identities at this polynomial. Moreover, we get  $(p,q)$ -extension of Carlitz's main result. In this work, we define and introduce a new kind of the Apostol type Frobenius-Euler polynomials based on the  $(p,q)$ -calculus and investigate their some properties, recurrence relationships and so on. We give some identities at this polynomial. Moreover, we get  $(p,q)$ -extension of Carlitz's main result.

**Keywords:** Bernoulli polynomials and numbers, Euler polynomials and numbers, Generating functions, Apostol type Frobenius-Euler polynomials,  $(p,q)$ -calculus,  $(p,q)$ -Frobenius-Euler polynomials, Generating function, .

### References:

- [1] Carlitz L., Eulerian numbers and polynomials, Math. Mag. 32(1959), 247-260.
- [2] Carlitz L.,  $q$ -Bernoulli numbers and polynomials, Duke Math. J., 15(1948), 987-1050. R.Chugh, V. Kumar, S. Kumar, "Strong Convergence of a New Three Step Iterative Scheme in Banach Spaces", American Journal of Computational Mathematics, 2(2012), 345-357.
- [3] Cenkci M., Can M. and Kurt V.,  $q$ -extensions of Genocchi numbers, J. Korean Math. Soc., 43(2006), 183-198.
- [4] Luo Q.-M., Some results for the  $q$ -Bernoulli and  $q$ -Euler polynomials, J. Math. Anal. Appl., 363 (2010), 7-18.
- [5] Duran U., Acikgoz M. and Araci S., On  $(p,q)$ -Bernoulli,  $(p,q)$ -Euler and  $(p,q)$ -Genocchi polynomials, Accepted in Journal of Computational and Theoretical Nanoscience.

## ANALYSIS OF A SECOND ORDER AND UNCONDITIONALLY STABLE BDF2-AB2 METHOD FOR THE NAVIER-STOKES EQUATIONS

Osman Raşit IŞIK<sup>1</sup>, Bülent DEMİR<sup>2</sup>

<sup>1</sup>*Department of Elementary Mathematics Education, Muğla Sıtkı Koçman University, Muğla/TURKEY*

[osmanrasit@mu.edu.tr](mailto:osmanrasit@mu.edu.tr)

<sup>2</sup>*Van Anadolu İmam Hatip Lisesi, İpekyoluKaymakamlığı, Van/TURKEY*

[bulentdemir@hotmail.com](mailto:bulentdemir@hotmail.com)

**Abstract:** In this study, we introduce a second order time stepping BDF2-AB2 method for the Navier-Stokes equations (NSE). It was proven that the method is unconditionally stable and  $O(\Delta t^2)$  accurate. We applied the method to several numeral experiments. Numerical results are overlapped with the theoretical results.

**Keywords:** NSE, Finite Element Method, BDF2-AB2 time discretization ..

**Acknowledgments:** This paper has been granted by the Mugla Sıtkı Kocman University Research Projects Coordination Office. Project Grant Number: 16/063 and title "Navier-Stokes Zaman Rahatlama Modeli ve Sonlu Elemanlar Çözümü Üzerine"

### References:

- [1] Kaya, S., Riviere, B. (2003) Analysis of a discontinuous Galerkin and eddy viscosity method for Navier Stokes equations. Technical Report, TR-MATH 03-14, University of Pittsburgh.
- [2] Connors, J. (2010), Convergence analysis and computational testing of the finite element discretization of the Navier–Stokes alpha model. Numer. Methods Partial Differential Eq., 26: 1328–1350. doi:10.1002/num.20493
- [3] William Layton, Nathaniel Mays, Monika Neda and CatalinTrenchea (2014). Numerical analysis of modular regularization methods for the BDF2 time discretization of the Navier-Stokes equations . ESAIM: Mathematical Modelling and Numerical Analysis, 48, pp 765-793. doi:10.1051/m2an/2013120.
- [4] Jiang, N., Mohebujjaman, M.,Rebholz, L., Trenchea, C. (2015) Analysis of a family of Optimally accurate regularization methods for Navier-Stokes equations. Technical Report,15-02, University of Pittsburgh.
- [5] Jiang, N., Mohebujjaman, M., Rebholz, L, G., Trenchea, C. (2015) Analysis Of A Family Of Regularization Methods For Navier-Stokes Equations. Technical Report, TR-MATH 03-14, University of Pittsburgh.



## STRONGLY SUMMABLE AND STATISTICALLY CONVERGENT BIVARIATE FUNCTIONS

Bünyamin AYDIN

Education faculty, Necmettin Erbakan University,

Konya/TURKEY

[bydin@konya.edu.tr](mailto:bydin@konya.edu.tr)

**Abstract:** We extend the definitions and basic results on strong summability, statistical convergence and almost convergence from functions of one variable to real valued bivariate functions measurable in the Lebesgue sense on the  $(1;1)_{(1;1)}$ .

### References:

- [1] S. Banach, *Theorie des operations linearies*, Warsaw, 1932.
- [2] M. Başarır, On the strong almost convergence of double sequences, *Periodica Mathematica Hungarica*, 30, 2 (1995) 99-103.
- [3] D. Borwein, Linear functionals with strong Cesaro Summability, *Journal London Math. Soc.*, 40 (1965) 628-634
- [4] H. Fast, Sur la convergence statistique, *Coll. Math.*, 2 (1951) 241-244.
- [5] A. R. Freedman, J. J. Sember and M. Raphael, Some Cesro type summability spaces, *Proc. London Math. Soc.*, 37 (1978) 508-520.
- [6] J. A. Fridy, On statistical convergence Analysis, 5 (1985) 301-313.
- [7] G. G. Lorentz, A contribution to the theory of divergent quences, *Acta. Math.*, 80 (1948) 167-190.
- [8] I. J. Maddox, A new type of convergence, *Math. Proc. Cambridge Phil. Soc.*, 83, 1 (1978) 61-64.
- [9] F. Moricz, Statistical convergence of multiple sequences, *J. Math. Anal. Appl.*, 288 (2003) 223-231.
- [10] F. Moricz and B. E. Rhoades, Almost convergence of double sequences and strongly regularity of summability, *Math. Proc. Cambridge Phil. Soc.*, 104, 2 (1988) 283-294.

## ASYMPTOTICALLY $I_2$ -CESÀRO EQUIVALENCE OF DOUBLE SEQUENCES OF SETS

Uğur ULUSU<sup>1</sup>, Erdinç DÜNDAR<sup>1</sup> and Bünyamin AYDIN<sup>2</sup>

<sup>1</sup>Department of Mathematics, AfyonKocatepe University,  
Afyonkarahisar/TURKEY

[ulusu@aku.edu.tr](mailto:ulusu@aku.edu.tr)

<sup>1</sup>Department of Mathematics, AfyonKocatepe University,  
Afyonkarahisar/TURKEY

[edundar@aku.edu.tr](mailto:edundar@aku.edu.tr)

<sup>2</sup>Education faculty, Necmettin Erbakan University,  
Konya/TURKEY

[baydin@konya.edu.tr](mailto:baydin@konya.edu.tr)

**Abstract:** In this paper, we defined concepts of asymptotically  $I_2$ -Cesàro equivalence and investigate the relationships between the concepts of asymptotically strongly  $I_2$ -Cesàro equivalence, asymptotically strongly  $I_2$ -lacunary equivalence, asymptotically  $p$ -strongly  $I_2$ -Cesàro equivalence and asymptotically  $I_2$ -statistical equivalence of double sequences of sets.

**Keywords:** Asymptotically equivalence, Cesàro summability, lacunary sequence, statistical convergence,  $I$ -convergence, double sequences of sets, Wijsman convergence.

### References:

- [1] M. Baronti, P. Papini, Convergence of sequences of sets, In: Methods of functional analysis in approximation theory, ISNM 76, Birkhauser-Verlag, Basel (1986).
- [2] G. Beer, On convergence of closed sets in a metric space and distance functions, Bull. Aust. Math. Soc. 31 (1985) 421432.
- [3] G. Beer, Wijsman convergence: A survey, Set-Valued Var. Anal. 2 (1994) 7794.
- [4] P. Das, E. Sava<sup>3</sup>, S. Kr. Ghosal, On generalized of certain summability methods using ideals, Appl. Math. Letter 36 (2011) 15091514.

## A NEW GENERALIZATION OF THE FIBONACCI $p$ –FUNCTIONS WITH PERIOD $k$

Yasin YAZLIK<sup>1</sup>, Cahit KÖME<sup>2</sup>

<sup>1</sup>Department of Mathematics, Nevşehir Hacı Bektaş Veli University,  
Nevşehir/TURKEY

[yyazlik@nevsehir.edu.tr](mailto:yyazlik@nevsehir.edu.tr), [cahitkome@gmail.com](mailto:cahitkome@gmail.com)

**Abstract:** In this presentation, we present the basic properties of the  $m$  –extension of Fibonacci  $p$  –functions with period  $k$ . Specifying  $p$  and  $m$ , we obtain the Fibonacci ( $p = 1, m = 1$ ) and Pell ( $p = 1, m = 2$ ) functions. Furthermore, we define  $m$  –extension of odd Fibonacci  $p$  –functions with period  $k$ . Moreover, we analyze some properties by using notion of  $f$  – even and  $f$  –odd functions with period  $k$ . We also demonstrate the products and quotients of these functions and provide new results in the development of Fibonacci functions with period  $k$ .

**Keywords:**  $m$  –extension of Fibonacci  $p$  –functions with period  $k$ ,  $m$  –extension of odd Fibonacci  $p$  –functions with period  $k$ ,  $f$  –even function with period  $k$ ,  $f$  –odd function with period  $k$ .

### References:

- [1] E. G. Kocer, N. Tuglu, A. Stakhov, On the  $m$  –extension of the Fibonacci and Lucas  $p$  –numbers, *Chaos, Solitons & Fractals*, 40 (4) (2009), 1890-1906.
- [2] B. Sroysang, On Fibonacci functions with period  $k$ , *Discrete Dynamics in Nature and Society* 2013, Article ID 418123, 4 pages.
- [3] Y. Yazlik, N. Taskara, A note on generalized  $k$  –Horadam sequence, *Computers & Mathematics with Applications*, 63 (1) (2012), 36-41.
- [4] A. Stakhov, B. Rozin, Theory of binet formulas for Fibonacci and Lucas  $p$  – numbers, *Chaos, Solitons & Fractals*, 27 (5) (2006), 1162-1177.

## ASSOCIATE SPACES OF GENERALIZED WEIGHTED WEAK-LORENTZ SPACES

Canay AYKOL YÜCE

*Department of Mathematics, Ankara University,  
Ankara/TURKEY*

[aykol@science.ankara.edu.tr](mailto:aykol@science.ankara.edu.tr)

**Abstract:** In this presentation, we characterize associate spaces of generalized weighted weak-Lorentz spaces.

**Keywords:** Generalized weighted weak-Lorentz spaces, reverse Hardy inequalities, associate spaces.

### References:

- [1] M. Carro, J. Soria, "Weighted Lorentz spaces and the Hardy operator", *J. Func. Anal.*, 112(1993), 480-494.
- [2] M. Carro, J. Soria, "Boundedness of some integral operators", *Canad. J. Math.*, 45(1993), 1155-1166.
- [3] A. Gogatishvili, L. Pick, "Discretization and anti-discretization of rearrangement-invariant norms", *Publ. Mat.*, 49(2003), 311-358.
- [4] A. Gogatishvili, L. Pick, "Embeddings and Duality Theorems for Weak Classical Lorentz Spaces", *Canad. Math. Bull.*, 49(2006), 82-95.

## SOME REFINEMENTS OF CERTAIN GAMIDOV INTEGRAL INEQUALITIES ON TIME SCALES AND APPLICATIONS

Chiheb TARIK

**Abstract:** The goal of this paper is to derive some generalizations and refinements of certain Gamidov type integral inequalities on time scales, which provide explicit bounds on unknown functions. To show the feasibility of the obtained inequalities, some illustrative examples are also introduced.

## THE RIESZ CAPACITY IN VARIABLE EXPONENT LEBESGUE SPACES

Cihan ÜNAL<sup>1</sup>, İsmail AYDIN<sup>2</sup>

<sup>1</sup>*Department of Mathematics, Sinop University,  
Sinop/TURKEY*

[cunal@sinop.edu.tr](mailto:cunal@sinop.edu.tr)

<sup>2</sup>*Department of Mathematics, Sinop University,  
Sinop/TURKEY*

[iaydin@sinop.edu.tr](mailto:iaydin@sinop.edu.tr)

**Abstract:** In this paper, we study a capacity theory based on a definition of a Riesz potential in the Euclidean space. Also, we define Riesz( $\alpha, p(\cdot)$ )–capacity and discuss properties of the capacity in the variable exponent Lebesgue space  $L^{p(\cdot)}(\mathbb{R}^n)$ .

**Keywords:** The Riesz potential and capacity, the variable exponent Lebesgue spaces.

### References:

- [1] D. R. Adams, L. I. Hedberg, "Function Spaces and Potential Theory", Springer-Verlag, (1996).
- [2] H. Aikawa, M. R. Essen, "Potential Theory: Selected Topics no.1633", Springer, (1996).
- [3] I. Aydın, "Weighted variable Sobolev spaces and capacity", Journal of Function Spaces and Applications, Vol. 2012, Article ID 132690, 17 pages, doi:10.1155/2012/132690, (2012).
- [4] G. Choquet, "Theory of capacities", Annales de l'institut Fourier, 5 (1954), 131-295.
- [5] N. G. Meyers, "A theory of capacities for potential of functions in Lebesgue classes", Math. Scand., 26(1970), 255-292.
- [6] J. Nuutinen, P. Silvestre, "The Riesz capacity in metric spaces", arXiv preprint, arXiv: 1501.05746, (2015).
- [7] W. P. Ziemer, "Weakly Differentiable Functions", Springer-Verlag, New York, (1989).

## ON EXISTING OF FIXED POINT FOR MULTIVALUED MAPPING VIA MEASURE OF NONCOMPACTNESS

Derya SEKMAN<sup>1</sup>, Vatan KARAKAYA<sup>2</sup>, Nour El Houda BOUZARA<sup>3</sup>

<sup>1</sup>*Department of Mathematics, Ahi Evran University,  
Kırşehir/TURKEY*

[deryasekman@gmail.com](mailto:deryasekman@gmail.com)

<sup>2</sup>*Department of Mathematical Engineering, Yildiz Technical University,  
İstanbul/TURKEY*

[vkaya@yahoo.com](mailto:vkaya@yahoo.com)

<sup>3</sup>*Department of Mathematics, Yildiz Technical University,  
İstanbul/TURKEY*

[bzr.nour@gmail.com](mailto:bzr.nour@gmail.com)

**Abstract:** In this work, using measure of noncompactness some result on the existence of coupled and tripled fixed point for multivalued set contraction mapping are investigated. As application, the existence of solution, for a system of integral inclusion is studied.

**Keywords:** Fixed point, multivalued set contraction mapping, measure of noncompactness.

### References:

- [1] B. C. Dhage, "Some generalizations of multi-valued version of Schauder's fixed point theorem with applications", CUBO A Mathematical Journal, 03,12(2010),139-151.
- [2] A. Aghajani, R. Allahyari, M. Mursaleen, "A generalization of Darbo's theorem with application to the solvability of systems of integral equations", Journal of Computational and Applied Mathematics, 260(2014), 68-77.
- [3] V. Karakaya, N.H. Bouzara, K. Doğan, Y. Atalan, " Existence of tripled fixed points for a class of condensing operators in Banach spaces", The Scientific World Journal, Volume 2014, 9 pages.

## DEFECT-DEFERRED CORRECTION METHOD FOR THE TWO-DOMAIN CONVECTION-DOMINATED CONVECTION-DIFFUSION PROBLEM

Dilek ERKMEN<sup>1</sup>, Alexander E. LABOVSKY<sup>2</sup>

<sup>1</sup> *Department of Mathematical Sciences, Michigan Technological University, USA,  
Department of Mathematical Sciences, Agri Ibrahim Cecen University,  
Agri, TURKEY .*

<sup>2</sup> *Department of Mathematical Sciences, Michigan Technological University, USA.*

**Abstract:** We present a method for solving a fluid-fluid interaction problem (two convection-dominated convection-diffusion problems adjoined by an interface), which is a simplified version of the atmosphere-ocean coupling problem. The method resolves some of the issues that can be crucial to the fluid-fluid interaction problems: it is a partitioned time stepping method, yet it is of high order accuracy in both space and time (the two-step algorithm considered in this report provides second order accuracy); it allows for the usage of the legacy codes (which is a common requirement when resolving flows in complex geometries), yet it can be applied to the problems with very small viscosity/diffusion coefficients. This is achieved by combining the defect correction technique for increased spatial accuracy (and for resolving the issue of high convection-to-diffusion ratio) with the deferred correction in time (which allows for the usage of the computationally attractive partitioned scheme, yet the time accuracy is increased beyond the usual result of partitioned methods being only first order accurate) into the defect-deferred correction method (DDC). The results are readily extendable to the higher order accuracy cases by adding more correction steps. Both the theoretical results and the numerical tests provided demonstrate that the computed solution is unconditionally stable and the accuracy in both space and time is improved after the correction step.

**Keywords:** Defect deferred correction, high accuracy, fluid-fluid interaction, ocean-atmosphere, implicit-explicit.

### References:

- [1] O. Axelsson and W. Layton, Optimal interior estimates for the defect-correction, finite element approach to 2-D convection-diffusion problems, ICMA report 88-116, Univ. of Pittsburgh, 1988.

## NONLINEAR WAVELETS AND THEIR STATISTICAL APPLICATIONS

Djabrane YAHIA<sup>1</sup>

<sup>1</sup>Laboratory of Applied Mathematics, Biskra University, ALGERIA

[yahia\\_dj@yahoo.fr](mailto:yahia_dj@yahoo.fr)

**Abstract:** Nonlinear wavelets and their applications in several areas of both pure and applied mathematics has provided statisticians with powerful new techniques for nonparametric curve estimation by combining recent advances in approximation theory with insights gained from applied signal analysis. Nonlinear wavelets are localized in both time and frequency and have remarkable approximation properties. In this presentation, we introduce a new nonlinear wavelet-based estimator of the regression function in the right censorship model. An asymptotic expression for the mean integrated squared error of the estimator is obtained to both continuous and discontinuous curves. The given wavelet estimator automatically adapt to a varying degrees of regularity (discontinuities, cusps, sharp spikes, etc.) of the underlying curves to be estimated when compared to other common estimation techniques, such as the kernel method, which may fail in unsmooth situations.

**Keywords:** censored data, mean integrated squared error, nonlinear wavelets, rate of convergence.

### References:

- [1] A. Antoniadis, "Wavelet methods in statistics: Some recent developments and their applications", *Statistics Surveys*, 1(2007), 16-55.
- [2] A. Antoniadis, G. Oppenheim, "Wavelets and statistics", Springer Science & Business Media, 103 (2012).
- [3] I. Daubechies, "Ten lectures on wavelets", Philadelphia: Society for industrial and applied mathematics, 61(1992), 198-202.
- [4] G. P. Nason, B. W. Silverman, "The stationary wavelet transform and some statistical applications". *Lecture Notes in Statistics-New York-Springer Verlag*, (1995), 281-281.



## SOLUTION OF FRACTIONAL HARRY DYM EQUATION WITH COLLOCATION USING RADIAL BASIS FUNCTION

Doğan KAYA<sup>1</sup>, Asif YOKUŞ<sup>2</sup>

<sup>1</sup>*Department of Mathematics, İstanbul Commerce University, İstanbul/TURKEY*

[dkaya36@yahoo.com](mailto:dkaya36@yahoo.com)

<sup>2</sup>*Department of Actuary, Firat University, Elazığ/TURKEY*

[asfyokus@yahoo.com](mailto:asfyokus@yahoo.com)

**Abstract:** In this paper, collocation method using radial basis functions is applied to solution of fractional Harry Dym differential equation. In the solution process, we will use linearization technique for non-linear term existing in the equation.  $L_2$  and  $L_\infty$  error norms are calculated with matematica program to compare the approximate solution with exact solution.

**Keywords:** Radial basis functions, Collocation method, Linearization technique.

### References:

- [1] K.Al-Khaled, M.Alquran, "An approximate solution for a fractional model of generalized Harry Dym equation", Math. Sci, 8 (2014), 125-130.
- [2] D. Kumar, J. Singh, and A.Kılıçman, "An efficient approach for fractional Harry Dym Equation by Using Sumudu Transform", Abstr. Appl. Anal., 2013(2013), Article ID 608943, 8.
- [3] S.Kumar, M.P. Tripathi, O.P. Singh, "A fractional model of Harry Dym equation and its approximate solution", Ain Shams Eng. J., 4 (2013), 111-115.
- [4] M.S.Rawashdeh, "New approach to solve the fractional Harry Dym equation using the FRDTM", Int. J. Pure Appl. Math., 95 (2014), 553-566.

## CHARACTERIZATION AND REVERSIBILITY OF 2D CELLULAR AUTOMATA WITH REFLECTIVE BOUNDARY

Ecem ACAR<sup>1</sup>, Selman UĞUZ<sup>1</sup>, Rahime KOÇ<sup>1</sup>

<sup>1</sup>Department of Mathematics, Harran University,  
63120, Şanlıurfa/TURKEY

[karakusecem@harran.edu.tr](mailto:karakusecem@harran.edu.tr), [selmanuguz@gmail.com](mailto:selmanuguz@gmail.com), [rahimekoc3@gmail.com](mailto:rahimekoc3@gmail.com)

**Abstract:** In this presentation, it is concentrated on a family of two dimensional (2D) finite linear cellular automata with reflective boundary condition over the ternary field, i.e.  $Z_3$ . It is established a relation between reversibility of cellular automata and characterization of 2D uniform cellular automata with this special boundary condition. We investigate the determination of the characterization problem of the specific cellular automata by using of the matrix algebra theory. Finally, we strongly believe that our uniform CA construction should be applied in real life applications of many scientific areas, such as image applications, cryptology, etc.

**Keywords:** Two dimensional cellular automata, Reflective boundary condition, Ternary field.

### References:

- [1] I. Siap, H. Akin, S. Uguz, "Structure and reversibility of 2D hexagonal CA", *Comp and Math App*, 62 (2011), 4161-4169.
- [2] S Uguz, H Akin, I Siap, U Sahin, "On irreversibility of Moore CA over ternary field", *Applied Math. Modelling*, In press, (2016).
- [3] I.Siap, H.Akin, F.Sah, "Garden of eden configurations for 2-D cellular automaton with rule 2460N," *Information Sciences* 180(2010), p. 3562.
- [4] S. Uguz, H. Akin, I. Siap, "Reversibility Algorithms for 3-state Hexagonal Cellular Automata With Periodic Boundaries", *International Journal of Bifurcation and Chaos*, 23 (2013),1350101.
- [5] P. Chattopadhyay, P. P. Choudhury, K. Dihidar, "Characterisation of a Particular Hybrid Transformation of Two Dimensional Cellular Automata", *Computers and Mathematics with Applications*, 38(1999), 207-216.

## ANALYSIS OF TRAINING PERFORMANCES OF INTERPOLATION METHODS FOR MODELLING HUMAN BODY MOTION

Egemen HALICI<sup>1</sup>, Erkan BOSTANCI<sup>2</sup>

<sup>1</sup>Computer Engineering Department, Ankara University  
Ankara/TURKEY

[ehalici@ankara.edu.tr](mailto:ehalici@ankara.edu.tr)

<sup>2</sup>Computer Engineering Department, Ankara University  
Ankara/TURKEY

[ebostanci@ankara.edu.tr](mailto:ebostanci@ankara.edu.tr)

**Abstract:** In this paper, the movements of human are modelled with dynamic movement primitives and then trained by the computer using various interpolation methods including Lagrange, spline and cubic spline. The main aim of the study was to assess the performances of these interpolation data in the training stage and choose the most suitable method in order to decrease the training and testing error for real-time motion capture applications. Training was performed on the Carnegie Mellon University Motion Capture Database. Step and grouping variables are introduced here to minimize the training error for the dataset. Statistical analysis of the results suggests that there are significant differences between the training results of these interpolation methods. The model was created with group value 4 and step value 6 and calculated mean square error for spline, cubic spline and Lagrange interpolations. Mc Nemar's Test, a non-parametric test to identify pairwise performance differences, was applied to the results to find the most suitable interpolation method. Spline and cubic interpolations yielded better results than Lagrange interpolation with z scores of 2.6 and 2.97, while the cubic spline outperformed spline interpolation with a z score of 3.71 with a 99.5% confidence for one and two tailed predictions.

**Keywords:** motion modelling; interpolation; dynamic movement primitives.

### References:

- [1] E. Halıcı, E. Bostancı, Modelling Human Body Motion using Lagrange Interpolation, SIU, Zonguldak, 2016.
- [2] B. Bostancı, E. Bostancı, J. C. Bansal et al. (eds.), Proceedings of the Seventh International Conference on Bio-Inspired Computing: Theories and Applications (BIC-TA 2012), Advances in Intelligent Systems and Computing 201, 2013

## A FRACTIONAL ORDER MODEL FOR OBESITY EPIDEMIC

Elif DEMİRCİ<sup>1</sup>

<sup>1</sup>*Department of Mathematics, Faculty of Sciences, Ankara University,  
Ankara/TURKEY*

[edemirci@ankara.edu.tr](mailto:edemirci@ankara.edu.tr)

**Abstract:** In this presentation, we propose a fractional order epidemic model for obesity contagion. The population size is assumed to be non-constant which is more realistic. The model considers vertical transmission of obesity and also obesity related death rate. We give local stability analysis of the model. Finally, some numerical examples are presented.

**Keywords:** Fractional differential equations, epidemic model, stability analysis, obesity.

### References:

- [1] K. Diethelm, "A fractional calculus based model for the simulation of an outbreak of dengue fever", *Nonlinear Dynamics*, 71, 4 (2013), 613-619.
- [2] K. Diethelm, "The Analysis of Fractional Differential Equations, An Application-Oriented Exposition Using Differential Operators of Caputo Type", Springer-Verlag, 2010.
- [3] N. Ozalp, E. Demirci, "A fractional order SEIR model with vertical transmission", *Mathematical and Computer Modelling*, 54, 1 (2011), 1-6.
- [4] K. Ejima, K. Aihara, H. Nishiura, "Modeling the obesity epidemic: social contagion and its implications for control", *Theoretical Biology and Medical Modelling*, (2013), 10-17.

## EXISTENCE AND CONVERGENCE THEOREMS FOR MULTIVALUED GENERALIZED HYBRID MAPPINGS IN $CAT(\kappa)$ SPACES

Emirhan HACIOGLU<sup>1</sup>, Vatan KARAKAYA<sup>2</sup>

<sup>1</sup>*Department of Mathematics, Yildiz Technical University, Davutpasa Campus,  
Esenler, 34220 Istanbul, Turkey,  
[haciogluemirhan@gmail.com](mailto:haciogluemirhan@gmail.com)*

<sup>2</sup>*Department of Mathematical Engineering, Yildiz Technical University,  
Davutpasa Campus, Esenler, 34210 Istanbul, Turkey,  
[vkaya@yahoo.com](mailto:vkaya@yahoo.com)*

**Abstract:** In this study, we give definition of some multivalued hybrid mappings which are general than multivalued nonexpansive mappings and some others. Also we give existence and convergence results in  $CAT(\kappa)$  spaces.

**Keywords:** multivalued mappings, generalized hybrid mappings, fixed point,  $\Delta$ -convergence

### References:

- [1] Espinola, R, Fernandez-Leon, A:  $CAT(\kappa)$ -Spaces, weak convergence and fixed points. *J. Math. Anal. Appl.* 353, 410-427 (2009)
- [2] M. Bridson and A. Haefliger, *Metric Spaces of Non-positive Curvature*, Springer-Verlag, Berlin, Heidelberg, 1999
- [3] Phuengrattana, Withun, and SuthepSuantai. "Existence and convergence theorems for generalized hybrid mappings in uniformly convex metric spaces." *Indian Journal of Pure and Applied Mathematics* 45.1 (2014): 121-136.
- [4] Nanjaras, Bancha, and BanchaPanyanak. "Generalized hybrid mappings on spaces." *Journal of Inequalities and Applications* 2014.1 (2014): 1-12.

## IDEAL CAUCHY CONDITION FOR INFINITE PRODUCTS

Emrah Evren KARA<sup>1</sup>, Metin BAŞARIR<sup>2</sup>, Merve İLKHAN<sup>3</sup>

<sup>1</sup>*Department of Mathematics, Düzce University,  
Düzce/TURKEY*

[karaeevren@gmail.com](mailto:karaeevren@gmail.com)

<sup>2</sup>*Department of Mathematics, Sakarya University,  
Sakarya/TURKEY*

[basarir@sakarya.edu.tr](mailto:basarir@sakarya.edu.tr)

<sup>3</sup>*Department of Mathematics, Düzce University,  
Düzce/TURKEY*

[merveilkhan@gmail.com](mailto:merveilkhan@gmail.com)

**Abstract:** In this presentation, we give  $\mathcal{I}$ -Cauchy and  $\mathcal{I}^*$ -Cauchy conditions for infinite products and prove the relation between them.

**Keywords:** Ideal convergence, ideal Cauchy condition, P-ideal.

### References:

- [1] I. J. Schoenberg, "The Integrability of Certain Functions and Related Summability Methods", *The American Mathematical Monthly*, 66(1959), 361-375.
- [2] P. Das, S. Kr. Ghosal, "Some Further Results On I-Cauchy Sequences and Condition (AP)", *Computers & Mathematics with Applications*, 59(2010), 2597-2600.
- [3] K. Dems, "On I-Cauchy Sequences", *Real Analysis Exchange* 30(2005), 123-128.

## SOME INEQUALITIES FOR $q$ -GAMMA FUNCTION

İnci EGE<sup>1</sup>, Emrah YILDIRIM<sup>2</sup>

<sup>1</sup>*Department of Mathematics, Adnan Menderes University,  
Aydın/TURKEY*

[iege@adu.edu.tr](mailto:iege@adu.edu.tr)

<sup>2</sup>*Department of Mathematics, Adnan Menderes University,  
Aydın/TURKEY*

[emrahyildirim@adu.edu.tr](mailto:emrahyildirim@adu.edu.tr)

**Abstract:** In this presentation, we obtain some monotonicity results for  $q$ -gamma function and by aid of these, we find some inequalities.

**Keywords:** Gamma function,  $q$ -gamma function, monotonicity, inequality.

### References:

- [1] E. Neumann, "Some inequalities for the gamma function", Applied Mathematics and Computation, 218.8(2011), 4349-4352.
- [2] V. Kac, P. Cheung, "Quantum Calculus", Universitext, New York, Springer-Verlag (2002).
- [3] R. Askey, "The  $q$ -gamma and  $q$ -beta functions", Appl. Anal. 8(1978), 125-141.
- [4] M. E. İsmail, M. E. Muldoon, "Inequalities and monotonicity properties for gamma and  $q$ -gamma functions", In Approximation and Computation: A Festschrift honor of Walter Gautschi (1994), 309-323.
- [5] A. De Sole, V. Kac, "On integral representations of  $q$ -gamma and  $q$ -beta functions", Atti Accad. Naz. Lincei Cl. Sci. Fis. Mat. Natur. Rend. Lincei Mat. Appl. 16.9(2005),:11-29.

## SOLVING INVERSE NODAL PROBLEM WITH JUMP CONDITIONS BY USING CHEBISYHEV POLYNOMIALS AND SOME RESULTS ON STABILITY

Emrah YILMAZ<sup>1</sup>, Hikmet KOYUNBAKAN<sup>2</sup> and Shahrbanoo KBARPOOR<sup>3</sup>

<sup>1,2</sup>*Department of Mathematics, Firat University,  
Elazığ/TURKEY*

[emrah231983@gmail.com](mailto:emrah231983@gmail.com)-[hkoyunbakan@gmail.com](mailto:hkoyunbakan@gmail.com)

<sup>3</sup>*Department of Mathematics, Mazandaran University,  
Babolsar/IRAN*

[akbarpoor.kiasary@yahoo.com](mailto:akbarpoor.kiasary@yahoo.com)

**Abstract:** In this study, we deal with an inverse nodal problem for Sturm-Liouville (SL) equation with eigen parameter-dependent boundary and jump conditions. We give some reconstruction formulas for potential function  $q$  under a condition and boundary data as a limit by using nodal points. Furthermore, we show that inverse nodal problem for SL equation is stable. Then, we use Chebisyhev polynomials of the first kind for calculating the approximate solution of the inverse nodal problem for SL equation with jump conditions. And, finally we present the numerical results by using some examples.

**Keywords:** Inverse Nodal Problem, Stability, Sturm-Liouville Equation, Chebisyhev Polynomials

### References:

- [1] C. K. Law, C. F. Yang, Reconstruction of the potential function and its derivatives using nodal data, *Inverse Problems*, (14) 299-312 (1999).
- [2] A. S. Ozkan, B. Keskin, Inverse nodal problems for Sturm-Liouville equation with eigenparameter-dependent boundary and jump conditions, *Inverse Problems in Science and Engineering*, (23) 1306-1312 (2014).
- [3] A. S. Ozkan, B. Keskin, Spectral problems for Sturm-Liouville operator with boundary and jump conditions linearly dependent on the eigenparameter, *Inverse Problems in Science and Engineering*, (20) 799-808 (2102).
- [4] J.R. McLaughlin, Stability theorems for two inverse spectral problems, *Inverse Problems*, (4) 529-540 (1988).



## SPECTRAL THEORY OF DIRAC SYSTEM ON TIME SCALES

Tuba GULSEN<sup>1</sup>, Emrah YILMAZ<sup>2</sup>

<sup>1</sup>*Department of Mathematics, Firat University,  
Elazığ/TURKEY*

[tubagulsen87@hotmail.com](mailto:tubagulsen87@hotmail.com)

<sup>2</sup>*Department of Mathematics, Firat University,  
Elazığ/TURKEY*

[emrah231983@gmail.com](mailto:emrah231983@gmail.com)

**Abstract:** In this study, we give some spectral properties of Dirac system on an arbitrary time scale. Furthermore, we have obtained eigenfunctions of first and second canonic forms of this system.

**Keywords:** Time Scales, Dirac system, Spectral Theory

### References:

- [1] S. Hilger, Ein Makettenkalkl mit Anwendung auf Zentrumsmannigfaltigkeiten Ph.D. Thesis, Universtat Wurzburg, (1988).
- [2] M. Bohner and A. Peterson, Dynamic equations on time scales; An introduction with applications, Birkhäuser Boston Inc., Boston, MA, (2001).
- [3] B. M. Levitan and I. S. Sargsjan, Sturm-Liouville and Dirac operators, Nauka, Moscow, (1991).
- [4] R. P. Agarwal, M. Bohner, D. O'Regan, Time scale boundary value problems on infinite intervals, Journal of Computational and Applied Mathematics, (2002) 141, 27-34.

## SUMMABILITY OF DOUBLE SEQUENCES OF 0'S AND 1'S

Emre TAŞ

*Department of Mathematics, AhiEvrans University,  
Kirsehir/TURKEY*

[emretas86@hotmail.com](mailto:emretas86@hotmail.com)

**Abstract:** In 1909 Borel stated that "Almost all of the sequences consisting of 0's and 1's are Cesàrosummable to  $(1/2)$ ". Then Hill has generalized Borel's result to general matrices. In this study we investigate the Borel property of 4-dimensional matrices.

**Keywords:** Double sequences, Pringsheim convergence, the Borel Property, double sequences of 0's and 1's

This work was supported by the Ahi Evran University Scientific Research Projects Coordination Unit. Project Number: **FEF.E2.16.017**

### References:

- [1] J.D.Hill, "Summability of sequences 0's and 1's", *Annals of Mathematics*, 46(1945), 556-562.
- [2] E. Taş, "The Borel property of 4-dimensional matrices", *Hacettepe Journal of Mathematics and Statistics*, 45(2016), 473-482.

## UNBOUNDED UPPER AND LOWER SOLUTION METHOD FOR FOURTH-ORDER DELAY DIFFERENTIAL EQUATIONS ON THE HALF-LINE

Erbil ÇETİN<sup>1</sup>, Ravi P. AGARWAL<sup>2</sup>

<sup>1</sup>*Department of Mathematics, Ege University,  
İzmir/TURKEY*

[erbil.cetin@ege.edu.tr](mailto:erbil.cetin@ege.edu.tr)

<sup>2</sup>*Department of Mathematics, Texas A&M University-Kingsville, Kingsville,  
Texas/USA*

[agarwal@tamuk.edu](mailto:agarwal@tamuk.edu)

**Abstract:** In this presentation, we introduce existence of solutions for fourth-order boundary value problems with delay terms on an infinite interval. First we present definitions of upper and lower solutions and Nagumo's condition of the problem. Also we establish the Green's function of the problem. Then we give sufficient conditions for the existence of a solution by using upper and lower solution method and the Schauder fixed point theorem. An example is given to illustrate the main result.

**Keywords:** Upper and lower solution method, delay differential equation, Schauder fixed point theorem.

### References:

- [1] Ch.G. Philos, Positive increasing solutions on the half line to second order nonlinear delay differential equations, *Glasg. Math. J.*, 49 (2007), no.2, 197-211.
- [2] Y. Wei, Existence and uniqueness of solutions for a second-order delay differential equation boundary value problem on the half-line, *Boundary Value Problems*. (2008). doi:10.1155/2008/752827
- [3] R. P. Agarwal and D. O-Regan, *Infinite interval problems for differential, difference and integral equations*, Kluwer Academic Publishers, Dordrecht, 2001.
- [4] J. Ehme, P.W. Eloe and J. Henderson, Upper and lower solution methods for fully nonlinear boundary value problems. *J. Differ. Equ.* 180(2002), 51-64.
- [5] H. Lian, R. P. Agarwal and J. Song, Boundary value problems for differential equations with deviating arguments. (submitted)

## STABILITY AND SQUARE INTEGRABILITY OF SOLUTIONS OF NONLINEAR FOURTH ORDER DIFFERENTIAL EQUATIONS WITH DELAY

Erdal KORKMAZ<sup>1</sup>, Cemil TUNC<sup>2</sup>

<sup>1</sup>*Department of Mathematics, Mus Alparslan University,  
Mus/TURKEY*

[korkmazerdal36@hotmail.com](mailto:korkmazerdal36@hotmail.com)

<sup>2</sup>*Department of Mathematics, YuzuncuYil University,  
Van/TURKEY*

[cemtunc@yahoo.com](mailto:cemtunc@yahoo.com)

**Abstract:** In this paper, we obtain sufficient conditions for the boundedness and square integrability of the solutions to a certain fourth order non-autonomous differential equations with delay by using Lyapunov's second method. In this work, we extend existing results on fourth order differential equations.

**Keywords:** Stability, boundedness, Lyapunov functional, delay differential equations, square integrable.

### References:

- [1] Afuwape, A .U. and Adesina, O. A.; Frequency-domain approach to stability and periodic solutions of certain fourth-order non-linear differential equations. *Nonlinear Stud.* 12, No. 3, pp. 259-269, (2005).
- [2] Burton T. A., Stability and periodic solutions of ordinary and functional differential equations .*Mathematics in science and engineering*, Volume 178, Academic Press, Inc, (1985).
- [3] Burton T.A., *Volterra Integral and Differential Equations*, *Mathematics in Science and Engineering Vol. (202)*, 2nd edition, (2005).
- [4] Chin, P. S. M.; Stability results for the solutions of certain fourth-order autonomous differential equations. *Internat. J. Control.* 49, No. 4, pp. 1163-1173, (1989).
- [5] Ezeilo, J. O. C.; On the Boundedness and the Stability of Solution of some Fourth Order Equations, *J. Math. Anal. Appl.* 5, pp. 136-146, (1962).
- [6] Ezeilo, J. O. C.; A Stability result for Solutions of a Certain Fourth Order Differential Equations. *J. London Math. Soc.* 37, pp. 28-32, (1962).

## JENSEN'S INEQUALITY WITH OPERATOR $s$ -CONVEXITY (or BRECKNER $s$ -CONVEXITY) IN HILBERT SPACE AND SOME ITS APPLICATIONS

Erdal UNLUYOL

*Department of Mathematics, Ordu University,  
Ordu/TURKEY  
[eunluyol@yahoo.com](mailto:eunluyol@yahoo.com)*

**Abstract:** In this presentation, I introduce a new operator inequality class of Jensen. Furthermore, I obtain new theorems and definitions. Also, I generalized this class. Finally, It is given some applications about this inequality.

**Keywords:** Jensen inequality, operator convex functions,  $s$ -convex or Breckner  $s$ -convex,

### References:

- [1] S. S. Dragomir, "Hermite-Hadamard's Type Inequalities for Operator Convex Functions", *Applied Mathematics and Computation*, 218(2011), 766-772.
- [2] J. Mičić, Z. Pavić, J. Pečarić, "Jensen's Inequality for operators without operator convexity", *Linear Algebra and its Applications*, 434(2011), 1228-1237.
- [3] S. S. Dragomir, "Operator Inequalities of the Jensen, Chebyshev and Grüss Type", *Springer Briefs in Mathematics*, Springer 2012, 121pp.
- [4] J. Mičić, J. Pečarić, "Recent Research on Jensen's Inequality for Operators", *Linear Algebra - Theorems and Applications*, Prof. Hassan Yasser (Ed.), InTech, DOI: 10.5772/48468. Available from: <http://www.intechopen.com/books/linear-algebra-theorems-and-applications/recent-research-on-jensen-s-inequality-for-operators>, 2012.

## WIJSMAN STATISTICAL CONVERGENCE OF DOUBLE SEQUENCES OF SETS

Fatih NURAY<sup>1</sup>, Uğur ULUSU<sup>1</sup> and Erdiñ DÜNDAR<sup>1</sup>

<sup>1</sup>*Department of Mathematics, Afyon Kocatepe University,  
Afyonkarahisar/TURKEY*

[fnuray@aku.edu.tr](mailto:fnuray@aku.edu.tr), [ulusu@aku.edu.tr](mailto:ulusu@aku.edu.tr), [edundar@aku.edu.tr](mailto:edundar@aku.edu.tr)

**Abstract:** In this paper, we study the concepts of Wijsman statistical convergence, Hausdorff statistical convergence and Wijsman statistical Cauchy double sequences of sets and investigate the relationships between them.

**Keywords:** Statistical convergence, double sequence of sets, Wijsman convergence, Hausdorff convergence.

## ROTATIONAL HYPERSURFACE IN 4-SPACE

Erhan GÜLER<sup>1</sup>, Martin MAGID<sup>2</sup>, Yusuf YAYLI<sup>3</sup>

<sup>1</sup>*Department of Mathematics, Bartın University, 74100  
Bartın/TURKEY*

[ergler@gmail.com](mailto:ergler@gmail.com), [comeguler@bartin.edu.tr](mailto:comeguler@bartin.edu.tr)

<sup>2</sup>*Department of Mathematics, Wellesley College, MA 02458  
Wellesley/UNITED STATES*

[mmagid@wellesley.edu](mailto:mmagid@wellesley.edu)

<sup>3</sup>*Department of Mathematics, Ankara University, 06100  
Ankara/TURKEY*

[yayli@science.ankara.edu.tr](mailto:yayli@science.ankara.edu.tr)

**Abstract:** We consider rotational hypersurface in the four dimensional Euclidean space. We calculate the mean and the Gaussian curvature, and some relations of the rotational hypersurface. Moreover, we give the Laplace-Beltrami operator of the rotational hypersurface.

**Keywords:** Laplace-Beltrami operator, Rotational hypersurface, Gaussian curvature, mean curvature.

## ENNEPER TYPE SURFACES IN 4-SPACE

Erhan GÜLER<sup>1</sup>, Ömer KIŞI<sup>2</sup>, Semra SARAÇOĞLU ÇELİK<sup>3</sup>

<sup>1,2,3</sup>*Bartın University, Faculty of Science, Department of Mathematics, 74100,  
Bartın, Turkey*

[eguler@bartin.edu.tr](mailto:eguler@bartin.edu.tr), [okisi@bartin.edu.tr](mailto:okisi@bartin.edu.tr), [ssaracoglu@bartin.edu.tr](mailto:ssaracoglu@bartin.edu.tr)

**Abstract:** We study a two parameter family of Enneper-type minimal surfaces using the Weierstrass representation in the four dimensional Euclidean space. We obtain implicit algebraic equations of the surfaces.

**Keywords:** Enneper-type minimal surfaces, Weierstrass representation, algebraic equation.

## ASYMPTOTICALLY $I_\sigma$ -EQUIVALENCE OF SEQUENCES OF SETS

Uğur ULUSU<sup>1</sup>, Esra GÜLLE<sup>1</sup>

<sup>1</sup>*Department of Mathematics, Afyon Kocatepe University,  
Afyonkarahisar/TURKEY*

[ulusu@aku.edu.tr](mailto:ulusu@aku.edu.tr), [egulle@aku.edu.tr](mailto:egulle@aku.edu.tr)

**Abstract:** In this paper, we introduce the concepts of Wijsman  $p$ -strongly asymptotically invariant equivalence ( $[W_{V_\sigma}^L]_p$ ), Wijsman asymptotically  $I$ -invariant equivalence ( $W_{I_\sigma}^L$ ) and Wijsman asymptotically  $I^*$ -invariant equivalence ( $W_{I_\sigma}^{L*}$ ). Also, we investigate the relationships among the concepts of Wijsman asymptotically invariant equivalence, Wijsman asymptotically invariant statistical equivalence, ( $[W_{V_\sigma}^L]_p$ ), ( $W_{I_\sigma}^L$ ) and ( $W_{I_\sigma}^{L*}$ ).

**Keywords:** Asymptotically equivalence,  $I$ -convergence, invariant convergence, sequences of sets, Wijsman convergence.

## GENERALIZED WEIGHTED STATISTICAL CONVERGENCE IN INTUITIONISTIC FUZZY NORMED LINEAR SPACES

Selma ALTUNDAĞ<sup>1</sup>, Esra KAMBER<sup>2</sup>

<sup>1</sup>*Department of Mathematics, Sakarya University,  
Sakarya/TURKEY*

[e.burdurlu87@gmail.com](mailto:e.burdurlu87@gmail.com)

<sup>2</sup>*Department of Mathematics, Sakarya University,  
Sakarya/TURKEY*

[scaylan@sakarya.edu.tr](mailto:scaylan@sakarya.edu.tr)

**Abstract:** In this paper, benefiting from a very recent investigation, we introduce a new statistical convergence type, named weighted  $\lambda$ -statistical convergence to generalize the concept of weighted statistical convergence with respect to the intuitionistic fuzzy norm  $(\mu, \nu)$ . Moreover, we establish its relation to weighted statistical convergence and a new summability method, named  $(\bar{N}_{\lambda}, p)$ -summability with respect to the intuitionistic fuzzy norm  $(\mu, \nu)$ .

**Keywords:** Statistical convergence, strong summability, intuitionistic fuzzy normed linear space.

### References:

- [1] L.A. Zadeh, "Fuzzy sets", . 8 (1965) 338-353(2014).
- [2] K.T. Atanassov, "Intuitionistic fuzzy sets", Fuzzy Sets and Systems, 20 (1986), 87-96.
- [3] R. Saadati, J.H. Park, "Intuitionistic fuzzy euclidean normed spaces", Commun. Math. Anal., 12 (2006), 85–90.
- [4] H. Fast, "Sur la convergence statistique", Colloq. Math., 2 (1951), 241–244.
- [5] M. Mursaleen, " $\lambda$ -statistical convergence", Math. Slovaca, 50 (2000) 111–115.
- [6] M. Mursaleen, V. Karakaya, M. Ertürk, F. Gürsoy, "Weighted statistical convergence and its application to Korovkin type approximation theorem", Appl. Math. and Comput., 218(2012), 9132-9137.



## OPERATOR IDEAL OF S-TYPE OPERATORS USING WEIGHTED MEAN SEQUENCE SPACE

Ezgi ERDOĞAN<sup>1</sup>, Vatan KARAKAYA<sup>2</sup>

<sup>1</sup>*Department of Mathematics, University of Marmara,  
Istanbul/TURKEY*

[ezgi.erdogan@marmara.edu.tr](mailto:ezgi.erdogan@marmara.edu.tr)

<sup>2</sup>*Department of Mathematical Engineering, Yıldız Technical University,  
Istanbul, Turkey*

[vkkaya@yahoo.com](mailto:vkkaya@yahoo.com)

**Abstract:** In this presentation, we give a different class of s-type operators by using the generalized weighted mean sequence space  $c_0(u,v)$ , and then it is shown that this new class of operators is a quasi-Banach operator ideal. Moreover, their injectivity and surjectivity are investigated according to sort of s-number. Finally, we prove that it is a closed operator ideal.

**Keywords:** Operator ideals, s-numbers, quasi-norm, weighted mean sequence space.

**Acknowledgement:** The first author was supported by TÜBİTAK- The Scientific and Technological Research Council of Turkey.

### References:

- [1] A. Maji, and P. D. Srivastava, On operator ideals using weighted Cesaro sequence space, *Egypt. Math. Soc.*, 22, 2014, 446-452.
- [2] A. Pietsch, s-numbers of Operators in Banach Spaces, *Studia Math.* 51, 1974, 201-223.
- [3] N. Şimşek, V. Karakaya, H. Polat, Operator Ideals of Generalized Modular Spaces of Cesaro Type Defined by Weighted Means, *J. Comput. Appl. Math.*, 19(5), 2015, 804-811.
- [4] B. Altay, F. Başar, Some Paranormed Sequence Spaces of Non-Absolute Type Derived by Weighted Mean, *J. Math. Anal. Appl.*, 319, 2006, 494-508.
- [5] Gh. Constantin, Operators of ces-p type, *Rend. Acc. Naz. Lincei.* 52:8, 1972, 875-878.
- [6] A. Pietsch, *Operator Ideals*, North-Holland Publishing Company, 1980.

## ON EIGENVALUES AND EIGENFUNCTIONS OF A BOUNDARY VALUE PROBLEM WITH RETARDED ARGUMENT

Khanlar R. MAMEDOV<sup>1</sup>, F. Ayça ÇETİNKAYA<sup>2</sup>

<sup>1,2</sup>Department of Mathematics, Mersin University, Mersin/TURKEY  
[hanlar@mersin.edu.tr](mailto:hanlar@mersin.edu.tr), [faycacetinkaya@mersin.edu.tr](mailto:faycacetinkaya@mersin.edu.tr)

**Abstract:** In this work, we investigate the asymptotic formulas for eigenvalues and eigenfunctions of the boundary value problem for the differential equation

$$u'' + q(x)u(x - \Delta(x)) + \lambda w(x)u(x) = 0, \quad x \in \left[0, \frac{\pi}{2}\right) \cup \left(\frac{\pi}{2}, \pi\right],$$

with boundary conditions

$$\begin{aligned} u(0) &= 0, \\ (\beta_1 + \beta_2\lambda)u'(\pi) + (\beta_3 + \beta_4\lambda)u(\pi) &= 0 \\ u(x - \Delta(x)) &\equiv u(0)\phi(x - \Delta(x)) \end{aligned}$$

and transmission conditions

$$\begin{aligned} \gamma_1 u\left(\frac{\pi}{2} - 0\right) - \delta_1 u\left(\frac{\pi}{2} + 0\right) &= 0, \\ \gamma_2 u'\left(\frac{\pi}{2} - 0\right) - \delta_2 u'\left(\frac{\pi}{2} + 0\right) &= 0, \end{aligned}$$

where the real valued function  $q(x)$  and  $\Delta(x) \geq 0$  is continuous on  $\left[0, \frac{\pi}{2}\right) \cup \left(\frac{\pi}{2}, \pi\right]$ ,  $\lambda$  is a spectral parameter,

$$w(x) = \begin{cases} w_1^2, & x \in \left[0, \frac{\pi}{2}\right) \\ w_2^2, & x \in \left(\frac{\pi}{2}, \pi\right] \end{cases}$$

$\gamma_1, \gamma_2, \delta_1, \delta_2$  are arbitrary real numbers ( $|\gamma_i| + |\delta_i| \neq 0$ ) ( $i=1,2$ ),  $\phi(x)$  is a initial continuous function on the initial set  $E_0 = \{x - \Delta(x) : x - \Delta(x) < 0, t > 0\}$  with  $\phi(0) = 0$ .

**Keywords:** asymptotics of eigenvalues and eigenfunctions, boundary value problems, differential equation with retarded argument; discontinuous coefficient.

### References:

- [1] S. B. Norkin, "Differential Equations of the Second Order with Retarded Argument", AMS; Providence, RI, (1972).

## SOME MATRIX CHARACTERIZATIONS ON THE SERIES SPACE $|\bar{N}_p^\theta|(\mu)$ AND APPLICATIONS

Fadime GÖKÇE<sup>1</sup>, Mehmet Ali SARIGÖL<sup>2</sup>

<sup>1,2</sup>*Department of Mathematics, University of Pamukkale,  
Denizli/TURKEY*

[fgokce@pau.edu.tr](mailto:fgokce@pau.edu.tr), [msarigol@pau.edu.tr](mailto:msarigol@pau.edu.tr)

**Abstract:** In this study, we introduce the notion of generalized absolute summability method which includes almost well known summabilities, and define some related series space  $|\bar{N}_p^\theta|(\mu)$  and also characterize the matrix classes  $(|\bar{N}_p^\theta|(\mu), |\bar{N}_q^\psi|(\lambda))$  and  $(|\bar{N}_p^\theta|(\mu), |\bar{N}_q|)$ . So, we deduce some known results as special cases.

**Keywords:** Absolute weighted summability, matrix transformations, sequence spaces.

### References:

- [1] Boos, J. and Cass, P., "Classical and modern methods in summability", Oxford University Press, New York, (2000).
- [2] Grosse-Erdmann, K.G., "Matrix transformations between the sequence spaces of Maddox", J. Math. Anal. Appl. 180 (1993) 223-238..
- [3] Maddox, I.J., "Elements of functional analysis", Cambridge University Press, London, New York, (1970)
- [4] Maddox, I.J., "Some properties of paranormed sequence spaces", J. London Math. Soc. 1 (1969), 316-322
- [5] Malkowsky, E. and Rakocevic, V., "On matrix domains of triangles", Appl. Math. Comp. 189 (2) (2007), 1146-1163.
- [6] Orhan, C. and Sarigöl, M.A., "On absolute weighted mean summability", Rocky Moun. J. Math. 23 (3), (1993), 1091-1097.
- [7] Sarigöl, M.A., "An inequality for matrix operators and its applications", Journal of Classical Analysis, 2 (2013), 145-150.

## ON THE ONE SUFFICIENT CONDITION FOR SHARP ESTIMATION OF ORTHONORMAL POLYNOMIALS OVER A CONTOUR OF THE COMPLEX PLANE

Fahreddin ABDULLAYEV<sup>1</sup>, Gülnare ABDULLAYEV<sup>2</sup>

<sup>1</sup>*Department of Mathematics, Mersin University,  
Mersin/TURKEY*

[fabdul@mersin.edu.tr](mailto:fabdul@mersin.edu.tr)

<sup>2</sup>*Higher School of Technical Science, Mersin University,  
Mersin/TURKEY*

[gabdullayev@yandex.ru](mailto:gabdullayev@yandex.ru)

**Abstract:** In this work, we considered the orthogonal polynomials along a contour [1,2]. We investigated the order of the height of the modulus of orthogonal polynomials over a contour with respect to the weighted Lebesgue space, where the contour and the weight function have some singularities at the finite number points on the contour [3,4].

Some sufficiently condition was obtained, when such estimation will be is sharp. Analogous question for arbitrary algebraic polynomials will be considered.

**Keywords:** Orthogonal polynomials, Algebraic polynomials, Conformal mapping, Quasicircle, Smooth curve.

### References:

- [1] G. Szegő, "Überorthogonale Polynome, die einer gegebenen Kurve der komplexen Ebene gehören", *Mathem. Zeitschr.* 9 (1921), pp.218-270.
- [2] P.K. Suetin, "Main properties of the orthogonal polynomials along a circle". *Uspekhi Math. Nauk*, Vol.21, No:2 (128), (1966), pp.41-88.
- [3] F.G. Abdullayev, P. Özkartepe, On the growth of algebraic polynomials in the whole complex plane, *Journal of Korean Math. Soc.*, Vol. 52, No:4, 2015 , pp.699-725.
- [4] F.G. Abdullayev, G.A. Abdullayev, On the some properties of the orthogonal polynomials over a contour with general Jacobi weight, *Ukr.Math.Bul*, No:1, 2016 (accepted).

## WEAK $w^2$ –STABILITY AND DATA DEPENDENCY OF MANN ITERATIVE SCHEME OF STRONGLY DEMICONTRACTIVE OPERATORS

Faik GÜRSOY

*Department of Mathematics, Adiyaman University,  
Adiyaman/TURKEY*

[faikgursoy02@hotmail.com](mailto:faikgursoy02@hotmail.com)

**Abstract:** We continue to examine the stability theory for Mann iterative method of strongly demicontractive operators (SDCOs) in the context of a weaker and more natural notion of stability called weak  $w^2$  –stability to get an insight in the corresponding result obtained in [L. Maruster, St. Maruster, On the error estimation and  $T$  –stability of the Mann iteration, J. Comput. Appl. Math., 276 (2015) 110-116]. We also study data dependency of fixed points of SDCOs. Some illustrative examples are also given to validate the theoretical results obtained herein.

**Keywords:** Mann iteration, weak stability, data dependency, demicontractive mappings.

### References:

- [1] M.L. Maruster, St. Maruster, "On the error estimation and T-stability of the Mann iteration." Journal of Computational and Applied Mathematics 276 (2015): 110-116.
- [2] W. R. Mann, "Mean value methods in iteration." Proceedings of the American Mathematical Society 4.3 (1953): 506-510.
- [3] F. Gürsoy, V. Karakaya, B. E. Rhoades, "Data dependence results of new multi-step and S-iterative schemes for contractive-like operators." Fixed Point Theory and Applications 2013.1 (2013): 1-12.
- [4] I. Timis, "On the weak stability of Picard iteration for some contractive type mappings." Annals of the University of Craiova-Mathematics and Computer Science Series 37.2 (2010): 106-114.

## APPROXIMATING FIXED POINTS OF ALMOST CONTRACTIONS BY A SIMPLER AND FASTER ITERATIVE SCHEME

Faik GÜR SOY<sup>1</sup>, Vatan KARAKAYA<sup>2</sup>, Kadri DOĞAN<sup>3</sup>

Müzeyyen ERTÜRK<sup>4</sup>

<sup>1,4</sup>*Department of Mathematics, Adiyaman University,  
Adiyaman/TURKEY*

<sup>1</sup>[faikgursoy02@hotmail.com](mailto:faikgursoy02@hotmail.com)

<sup>4</sup>[merturk3263@gmail.com](mailto:merturk3263@gmail.com)

<sup>2</sup>*Department of Mathematical Engineering, Yıldız Technical University,  
İstanbul/TURKEY*

[vkaya@yahoo.com](mailto:vkaya@yahoo.com)

*Department of Mathematics Education, Artvin Coruh University,  
Artvin/ TURKEY*

[dogankadri@hotmail.com](mailto:dogankadri@hotmail.com)

**Abstract:** Our purpose in this exposition is to prove some convergence and data dependence result in the class of almost contraction operators using a simpler and faster iterative process in the framework of Banach spaces. Some numerical examples are provided to validate the results obtained. Our results improve several known results in the existing literature.

**Keywords:** Iterative schemes, convergence, data dependence, almost contractions.

### References:

- [1] V. Karakaya, K. Doğan, F. Gürsoy, and M. Ertürk, "Fixed point of a new three-step iteration algorithm under contractive-like operators over normed spaces," *Abstract and Applied Analysis*, vol. 2013, Article ID 560258, 9 pages, 2013.
- [2] F. Gürsoy, V. Karakaya, B. E. Rhoades, "Data dependence results of new multi-step and S-iterative schemes for contractive-like operators." *Fixed Point Theory and Applications* 2013.1 (2013): 1-12.

## A GENERALIZATION OF SOME MIXED NORM SPACES

Faruk ÖZGER<sup>1</sup>, Eberhard MALKOWSKY<sup>2</sup>

<sup>1</sup>*Department of Engineering Sciences, Izmir Katip Celebi University,  
Izmir/TURKEY*

[farukozger@gmail.com](mailto:farukozger@gmail.com)

<sup>2</sup>*Državni Univerzitet u Novom Pazaru, Vuka Karadžića bb, 36300,  
Novi Pazar/SERBIA*

[ema@Bankerinter.net](mailto:ema@Bankerinter.net)

**Abstract:** In this presentation, we generalize the definition of mixed norm spaces to that of mixed paranorm spaces. We also consider the spaces of sequences that are strongly summable to zero as special cases of mixed paranorm spaces.

**Keywords:** Mixed norm spaces, mixed paranorm spaces, dual spaces.

### References:

- [1] K.-G. Grosse-Erdmann, The Blocking Technique, Weighted Mean Operators and Hardy's Inequality, Lecture Notes in Mathematics 1679, Springer Verlag (1998).
- [2] E. Malkowsky, V. Rakocevic, An Introduction into the Theory of Sequence Spaces and Measures of Noncompactness, Zbornik radova 9(17) Matematički institut SANU, Belgrade (2000) 143–234.
- [3] E. Malkowsky, F. Özger, A note on some sequence spaces of weighted means, Filomat, Vol. 26(2012) 511–518.
- [4] E. Malkowsky, F. Özger and V. Veličković, Some Spaces Related to Cesaro Sequence Spaces and an Application to Crystallography, MATCH Commun. Math. Comput. Chem., 70(3) (2013) 867-884.
- [5] E. Malkowsky, F. Özger A. Alotaibi, Some notes on matrix mappings and their Hausdorff measure of noncompactness, Filomat, (2014) 1059-1072.

## MATRICIALLY DERIVED SOLID BANACH SEQUENCE SPACES

Faruk POLAT

*Department of Mathematics, Çankırı Karatekin University,  
Çankırı/TURKEY  
[faruk.polat@gmail.com](mailto:faruk.polat@gmail.com)*

**Abstract:** Let  $F^N$  denote the vector space of all scalar sequences. If  $A$  is an infinite matrix with non-negative entries and  $\lambda$  is a solid subspace of  $F^N$ , then  $sol - A^{-1}(\lambda) = \{x \in F^N : A|x| \in \lambda\}$  is also a solid subspace of  $F^N$  which, under certain conditions on  $A$  and  $\lambda$  inherits a solid topological vector space topology from any such topology on  $\lambda$ . Letting  $\Lambda_0 = \lambda$  and  $\Lambda_m = sol - A^{-1}(\Lambda_{m-1})$  for  $m > 0$ , we derive an infinite sequence  $\Lambda_0, \Lambda_1, \Lambda_2, \dots$  of solid subspaces of  $F^N$  from the inputs  $A$  and  $\lambda$ . For  $A$  and  $\lambda$  confined to certain classes, we ask many questions about this derived sequence, and answer a few.

**Keywords:** Solid sequence space, infinite matrix, projective limit, solid topology.

## BOUNDEDNESS OF FRACTIONAL MAXIMAL OPERATOR ON GENERALIZED ORLICZ-MORREY SPACES

Fatih DERİNGÖZ

*Department of Mathematics, Ahi Evran University,  
Kırşehir/TURKEY  
[fderingoz@ahievran.edu.tr](mailto:fderingoz@ahievran.edu.tr)*

**Abstract:** We consider generalized Orlicz-Morrey spaces including their weak versions. In these spaces, we find the sufficient conditions for the boundedness of the fractional maximal operator from one generalized Orlicz-Morrey space to another one.

**Keywords:** generalized Orlicz-Morrey spaces, fractional maximal operator, Riesz potential.

This work was supported by the Ahi Evran University Scientific Research Projects Coordination Unit. Project Number: FEF.E2.16.016

### References:

- [1] V.S.Guliyev, F. Deringoz, "On the Riesz potential and its commutators on generalized Orlicz-Morrey spaces", *Journal of Function Spaces*, Article ID 617414 (2014), 11 pp.
- [2] V.S.Guliyev, F. Deringoz, "Boundedness of fractional maximal operator and its commutators on generalized Orlicz-Morrey spaces", *Complex Analysis and Operator Theory*, 9(2015), 1249-1267.



## ON ONE KIND OF POSITIVE OPERATORSIN LEBESGUE SPACE OF HARMONIC FUNCTIONS

Fatih SIRIN<sup>1</sup>, Yusuf ZEREN<sup>2</sup>

<sup>1</sup>*Department of Mathematics, Yıldız Technical University,  
İstanbul/TURKEY*

[fatih.sirin@std.yildiz.edu.tr](mailto:fatih.sirin@std.yildiz.edu.tr)

<sup>2</sup>*Department of Mathematics, Yıldız Technical University, İstanbul/TURKEY*

[yzeren@yildiz.edu.tr](mailto:yzeren@yildiz.edu.tr)

**Abstract:** In this work we consider some system of positive operators in Lebesgue Space of Harmonic functions and prove Korovkin type theorem in this space.

**Keywords:** Lebesgue Space of Harmonic functions, Korovkin type theorem, Poisson kernel.

### References:

- [1] F. Altomare, "Korovkin-type theorems and approximation by positive linear operators," *Surveys in Approximation Theory*, vol. 5, pp. 92–164, 2010.
- [2] P. P. Korovkin, Convergence of linear positive operators in the spaces of continuous functions (Russian), *Doklady Akad. Nauk. SSSR (N.S.)*, 90 (1953), 961–964.
- [3] P. P. Korovkin, *Linear Operators and Approximation Theory*, translated from the Russian ed. (1959), Russian Monographs and Texts on Advances Mathematics and Physics, Vol. III, Gordon and Breach Publishers, Inc. New York, Hindustan Publ. Corp. (India), Delhi, 1960.
- [4] K. Izuchi, H. Takagi and S. Watanabe, Sequential Korovkin type theorems and weighted composition operators, *Acta Sci. Math. (Szeged)* 62 (1996), 161–174.
- [5] Garnett, J. B. *Bounded Analytic Functions*, Academic Press, 1981.

## NUMERICAL RECKONING COINCIDENCE POINTS OF NONSELF MAPPINGS VIA A JUNGCK-MODIFIED SP ITERATIVE METHOD

Fatma ÖZTÜRK ÇELİKER

*Department of Mathematics, Yıldız Technical University, İstanbul/TURKEY*  
[fatozmat@gmail.com](mailto:fatozmat@gmail.com)

**Abstract:** Current literature on the iterative approximation of fixed points reveals that there have been substantial endeavors to introduce diverse iterative methods of self-operators and investigate their more qualitative properties such as convergence, data dependency and stability. Since the case of nonself-mappings is much more complicated than that of self-mappings, it is rarely considered in the literature. Inspired by the work of Khan et al. [1] and [2], here we handle this problem using a new iterative method of two nonself operators.

**Keywords:** Convergency, data dependency, Jungck-type iterative method.

### References:

- [1] A.R. Khan, F.Gürsoy, and V. Karakaya, "Jungck-Khan iterative scheme and higher convergence rate." *International Journal of Computer Mathematics* 2015: 1-14.
- [2] A.R. Khan, F.Gürsoy, and V. Kumar, "Stability and data dependence results for Jungck-Khan iterative scheme." 40.3 (2016): 631-640.
- [3] F. ÖztürkÇeliker, "Convergence analysis for a modified SP iterative method." *Sci. World J.* 2014, Article ID 840504 (2014).

**COMMON FIXED POINT THEOREMS FOR WEAKLY  
COMPATIBLE MAPPINGS, EMPLOYING AN IMPLICIT  
RELATION WITH COMPLEX COEFFICIENTSON  
COMPLEX VALUED METRIC SPACE**

Fayyaz ROUZKARD

*Farhangian University, Tehran, IRAN*  
fayyazrouzkard@gmail.com

**Abstract:** A general common fixed point theorem for two pairs of weakly compatible mappings using an implicit function is proved without any continuity requirement which generalizes the result due to Popa [3, Theorem 3]. We establish common fixed point theorems involving two pairs of weakly compatible mapping satisfying certain rational expressions with complex coefficients are proved in complex valued metric space.

Some related results are also derived besides furnishing illustrative examples to highlight the realized improvements. The presented theorems generalize, extend and improve many existing results in the literature.

**Keywords:** implicit functions, weakly compatible mappings, complex coefficients, coincidence and Complex valued metric space.

**References:**

- [1] A. Azam, B. Fisher and M. Khan, "Common Fixed Point Theorems in Complex Valued Metric Spaces", *Numerical Functional Analysis and Optimization*, 32:(2011), 3, 243253
- [2] J. Ali and M. Imdad, "Unifying a multitude of common fixed point theorems employing an implicit relation", *Commun. Korean Math. Soc.* 24, 1,(2009), 41-55
- [3] V. Pupa, "Some fixed point theorems for weakly compatible mappings", *Rad. Mat.* 10(2001),245–252.
- [4] F. Rouzkard and M. Imdad, "Some common fixed point theorems on complex valued metric space" *Computers and Math. With Appl.* 64(2012) 1866-1874

## RESTORATION OF DEGRADED FACE IMAGE USING NON LINEAR DIFFERENTIAL EQUATION FOR RECOGNITION

Fella BERRIMI<sup>1</sup>, Khier BENMAHAMMED<sup>2</sup>

<sup>1</sup>*Department of Technology, Ferhat ABBES University,  
Setif/ALGERIA*

[fellaber@yahoo.fr](mailto:fellaber@yahoo.fr)

<sup>2</sup>*Department of Electronics, Ferhat ABBES University,  
Setif/ALGERIA*

[khierben@gmail.com](mailto:khierben@gmail.com)

**Abstract:** In this paper, we search to find a good estimate of the degraded face image for recognizing the person presented in this face. First, the degraded face image is restored with an anisotropic diffusion method based on non linear differential equation (PDE). This approach is an efficient new method to remove noise from an image by performing isotropically smooth in the homogeneous region (low gradient) in preference to inhomogeneous region (height gradient) in order to prevent the destruction of discontinuities. After the restoration task, the recognition one is performed using the principal components analysis (PCA) method that decomposes the face image into small set of characteristics (eigenvectors) which catch the total variation in collection of training faces(classes) where each class contains a few images describing a person with different poses and looks (hair style, glasses,...). The training set created a new space called eigenface space where the restored image is projected, so it is redefined in this space using eigenvectors. Finally, we can recognize the person presented in the test face on selecting the face class that have the minimum distance with the projected image using the mean square distance and studding the different cases. Experiments on the Extended Yale B face database where the test face image is artificially degraded using the Gaussian blur show that the proposed method substantially improves the recognition performance compared to other methods.

**Keywords:** anisotropic diffusion based on non linear differential equation, linear method based on principal components analysis, restoration of degraded face image, face recognition.

### References:

- [1] M. Turk, A. Pentland, "Face recognition using Eigenfaces", *Proc. IEEE Conference on Computer Vision and Pattern Recognition*, (1991), 586-591.
- [2] P. Perona, J. Malik, "Scale-space and edge detection using anisotropic diffusion", *IEEE Trans. PAMI*, vol. 12, No. 7, (1990), 629-639.

## CHARACTERIZATION OF THREE DIMENSIONAL CELLULAR AUTOMATA WITH PERIODIC BOUNDARY OVER $\mathbb{Z}_m$

Ferhat ŞAH<sup>1</sup>, Hasan AKIN<sup>2</sup> Fatih TAŞÇI<sup>3</sup>

<sup>1</sup>*Department of Mathematics, Adiyaman University,  
Adiyaman/TURKEY  
[fsah@adiyaman.edu.tr](mailto:fsah@adiyaman.edu.tr)*

<sup>2</sup>*Department of Mathematics, Faculty of Education, Zirve University,  
[akinhasan25@gmail.com](mailto:akinhasan25@gmail.com)*

<sup>3</sup>*Department of Mathematical Engineering, Yıldız Technical University,  
İstanbul/TURKEY  
[tasci@yildiz.edu.tr](mailto:tasci@yildiz.edu.tr)*

**Abstract:** A quick look at the literature reveals that there are just a few study regarding with three dimensional cellular automata. This situation motivate us to study the algebraic behavior of three dimensional linear cellular automata over  $\mathbb{Z}_m$ . We provide necessary and sufficient conditions for a three dimensional linear cellular automata over  $\mathbb{Z}_m$  to be reversible or irreversible. The obtained result characterizes three dimensional linear cellular automata under the periodic boundary conditions. Finally, we give an application to show validity of our result.

**Keywords:** 3D Cellular automata, Matrix Representation, Finite Fields, Periodic Boundary.

### References:

- [1] Sah, F., Siap, İ., Akın, H., "Characterization of three dimensional cellular automata over  $\mathbb{Z}_m$  ." AIP Conf. Proc. (2012). 1470: 138
- [2] Sah, F., Tasci, F., Akın, H., "Attractors and three dimensional cellular automata over  $\mathbb{Z}_m$  ." "International Conference on Applied Analysis and Mathematical Modelling (ICAAMM) 8-12 June Istanbul, (2015).
- [3] Tsalides, P., Hicks, P.J. and York, T.A., " Three - dimensional cellular automata and VLSI applications", IEE Proceedings, (1989). 136(6):490 –495

## NUMERICAL APPROACH TO SOLVE SINGULAR INTEGRO-DIFFERENTIAL EQUATIONS USING TAYLOR SERIES EXPANSION

Fernane KHAIREDDINE<sup>1</sup>, EllagouneFATEH<sup>2</sup>

<sup>1,2</sup>*Department of Mathematics, University of 8 May 1945,  
P.O.Box 401, 24000 Guelma-Algeria*

<sup>1</sup>[kfernane@yahoo.fr](mailto:kfernane@yahoo.fr)<sup>2</sup>[fellagoune@gmail.com](mailto:fellagoune@gmail.com)

**Abstract:**In this paper, we apply Taylor series expansion for approximating and then transform the given nth-order weakly singular linear Volterra and Fredholm integro-differential equations to one ordinary linear differential equation. The solution of this last differential equation is the approximate solution of the integro-differential equation. Finally, some different examples are considered the results of these examples indicated that the procedure of transformation method is simple and effective, and could provide an accurate approximate solution or exact solution.

**Keywords:**Taylor series expansion, General Abel Integral, Integro-differential Equations, Weakly singular Fredholm integral-equations, Weakly singular Volterra integral-equations.

### References

- [1] Sah, F., Siap, İ., Akın, H., "Characterization of three dimensional cellular automata over  $Z_m$  ." AIP Conf. Proc. (2012). 1470: 138
- [2] H. Adibi, A. Taherian, Numerical Solution of the Most General Nonlinear Fredholm Integro-Differential-Difference Equations by using Taylor Polynomial Approach, Int. J. Math. Modell.Com-put. **2** (4) (2012) 283-298
- [3] K. E. Atkinson, A discrete Galerkin method for first kind integral equations with logarithmic kernel, J. Int. Eq. Appl. **1** (1988) 343-363.
- [4] K. G. Beauchamp, Applications of walsh and related functions with an introduction to sequence theory, Academic Press, London, 1984
- [5] H. . Brunner, On the numerical solution of nonlinear Volterra Fredholm by collocation methods. SIAM, integral equations J. Numer. Anal. **27** (1990), no. 4, 987-1000.
- [6] A. Chakrabarti and A. J. George, A formula for the solution of general Abel integral equation. Appl. Math. Lett. **7** (1994), no. 2, 87-90.

## EXTRAGRADIENT METHOD FOR SOLVING EQUILIBRIUM PROBLEM IN BANACH SPACES

Zeynab JOUYMANDI<sup>1</sup>, Fridoun MORADLOU<sup>2</sup>

<sup>1</sup>*Department of Mathematics, Sahand University of Technology,  
Tabriz/IRAN*

[z\\_jouymandi@sut.ac.ir](mailto:z_jouymandi@sut.ac.ir)

<sup>2</sup>*Department of Mathematics, Sahand University of Technology,  
Tabriz/IRAN*

[moradlou@sut.ac.ir](mailto:moradlou@sut.ac.ir)

**Abstract:** In this presentation, using sunny generalized nonexpansive retraction, which is different from the metric projection, we propose a new extragradient algorithm for finding the solution set of an equilibrium problem (EP) in Banach spaces. The extragradient method is well known because of its efficiency in numerical test. In all papers, authors have used metric projection in Hilbert spaces and generalized metric projection in Banach spaces. To obtain strong convergence for the sequences which are generated by our algorithm, we assume that the equilibrium function  $f$  satisfies in  $\phi$ -Lipschitz-type condition.

**Keywords:** Equilibrium problem, Extragradient method, Sunny generalized nonexpansive retraction.

### References:

- [1] T. T. V. Nguyen, J. J. Strodiot and V. H. Nguyen, The interior proximal extragradient method for solving equilibrium problems, *J. Glob. Optim.*, **44** (2009), 175–192.
- [2] A. N. Iusem and W. Sosa, on the proximal point method for equilibrium problem in Hilbert spaces, *Optimization*, **59** (2010) 1259–1274.
- [3] D. Q. Tran, L. D. Muu and V. H. Nguyen, Extragradient algorithms extended to equilibrium problems, *Optimization* **57** (2008), 749–776.
- [4] P. T. Vuong, J. J. Strodiot and V. H. Nguyen, Extragradient methods and line search algorithms for solving Ky Fan inequalities and fixed point problems, *J. Optim. Theory Appl.*, **155** (2012), 605–627.

## NUMERICAL INTEGRATION VIA SPARSE GRIDQUASI-INTERPOLATION WITH GAUSSIANS

Fuat USTA<sup>1</sup>, Jeremy LEVESLEY<sup>2</sup>

*<sup>1</sup>Department of Mathematics, Düzce University,  
Düzce/TURKEY*

[fuatusta@duzce.edu.tr](mailto:fuatusta@duzce.edu.tr)

*<sup>2</sup>Department of Mathematics, University of Leicester,  
Leicester/UK*

[jl1@leicester.ac.uk](mailto:jl1@leicester.ac.uk)

**Abstract:** Sparse grid approximation is one of the most powerful methods for approximation of functions especially in high dimensions, 5-10, say. In this presentation we will define a quadrature formula via quasi interpolation by using sparse grid with Gaussian kernel. Then in order to overcome convergence problem we define multilevel version of this algorithm. Finally we present the results of numerical experimentation for numerical integration for high dimensions.

**Keywords:** Sparse grid, quasi interpolation, Gaussians, high dimensional interpolation, quadrature, multilevel algorithm.

### References:

- [1] E. H. Georgoulis, J. Levesley, and F. Subhan. Multilevel sparse kernel based interpolation. *SIAM Journal of Scientific Computing*, 35:815-832, 2013.
- [2] V. Mazya and G. Schmidt. *Approximate Approximations*. 2007. Providence.



## USING KERNEL BASED METHODS FOR NEW TYPE CONFORMABLE ODE PROBLEMS

Fuat USTA<sup>1</sup>

<sup>1</sup>*Department of Mathematics, Düzce University,*

*Düzce/TURKEY*

[fuatusta@duzce.edu.tr](mailto:fuatusta@duzce.edu.tr)

**Abstract:** In this presentation, we introduced a new scheme for solving the newly defined conformable ordinary differential equation [1] via the mesh-free numerical method. In order to solve these type differential equations, we use the radial basis functions with collocation technique. Then We present the results of numerical experimentation for numerical solution of newly defined conformable ordinary differential equations.

**Keywords:** Newly defined conformable derivatives, radial basis functions, collocation technique.

### References:

- [1] D. R. Anderson and D. J. Ulness, Newly defined conformable derivatives, *Advances in Dynamical Systems and Applications*, 10 (2015), p. 109-137.
- [2] C. Franke and R. Schaback, Solving partial differential equations by collocation using radial basis functions, *Applied Mathematics and Computation*, 93 (1998), pp. 73 - 82.

## AN EXISTENCE THEOREM OF MULTIPLE POSITIVE SOLUTIONS TO SEMIPOSITONE BOUNDARY VALUE PROBLEMS

Fulya YÖRÜK DEREN<sup>1</sup>, Nüket AYKUT HAMAL<sup>2</sup>, Tuğba ŞENLİK ÇERDİK<sup>3</sup>

<sup>1,2,3</sup>*Department of Mathematics, Ege University,  
İzmir/TURKEY*

[fulya.yoruk@ege.edu.tr](mailto:fulya.yoruk@ege.edu.tr), [nuket.aykut@ege.edu.tr](mailto:nuket.aykut@ege.edu.tr), [tubasenlik@gmail.com](mailto:tubasenlik@gmail.com)

**Abstract:** In this talk, we investigate the existence of multiple positive solutions for semipositone boundary value problems of three-point boundary conditions by means of the Leggett- Williams fixed point theorem.

**Keywords:** Positive solution, fixed point theorem, semipositone.

### References:

- [1] J. Henderson, N. Kosmatov, Positive solutions of the semipositone Neumann boundary value problem, *Mathematical Modelling and Analysis*, 20:5, (2015) 578-584.
- [2] K. Deimling, "Nonlinear functional analysis, Springer, Newyork", 1985.
- [3] D. Guo, V. Lakshmikantham, *Nonlinear problems in abstract cones*. Academic Press, Orlando, 1988.
- [4] X. Han, "Positive Solutions for a three-point boundary value problem at resonance", *J. Math. Anal. Appl.* 336 (2007) 556-568.
- [5] U. Akcan, N. Aykut Hamal, Existence and monotone iteration of concave positive symmetric solutions for a three-point second-order boundary value problems with integral boundary conditions .

## GENERALIZED ABSOLUTE CESÀRO SUMMABILITY SPACES AND MATRIX OPERATORS

G. Canan HAZAR<sup>1</sup>, M. Ali SARIGÖL<sup>2</sup>

<sup>1</sup>*Department of Mathematics, Pamukkale University,  
Denizli/TURKEY*

[gchazar@pau.edu.tr](mailto:gchazar@pau.edu.tr)

<sup>2</sup>*Department of Mathematics, Pamukkale University,  
Denizli/TURKEY*

[msarigol@pau.edu.tr](mailto:msarigol@pau.edu.tr)

**Abstract:** In this presentation, we introduce a new space  $|C_{\lambda, \mu}|_k$  as the set of series summable by absolute Cesàro summability  $|C, \lambda, \mu|_k$  of Das [2], investigate its some algebraic and topological properties, and characterize some matrix operators defined on that space. Moreover, these characterizations correspond to problems of absolute summability factors and comparison of these summability methods for the special matrix transformations such as identity matrix  $I$  and the matrix  $W = (w_{nv})$  defined by  $w_{nv} = \varepsilon_v$  for  $v = n$ , zero otherwise. Hence we generalize some well known results of Bosanquet [1], Flett [3], Mehdi [6], Mazhar [5], Orhan and Sarigöl [10] and Sarigöl [7,9].

**Keywords:** Sequence spaces, Absolute Cesàro summability, matrix transformations, dual spaces, BK spaces.

### References:

- [1] L.S. Bosanquet, "Note on convergence and summability factors I", J. London Math. Soc., 20(1945), 39-48.
- [2] G. Das, "A Tauberian theorem for absolute summability", Proc. Cambridge Philos., 67(1970), 321-326.
- [3] T. M. Flett, "On an extension of absolute summability and some theorems of Littlewood and Paley", Proc. London Math. Soc., 7(1957), 113-141.
- [4] I. J. Maddox, "Elements of functional analysis", Cambridge University Press, New York, (1970).
- [5] S. M. Mazhar, "On the absolute summability factors of infinite series", Tohoku Math. J., 23 (1971), 433-451.

## A NEW ITERATIVE ALGORITHM FOR QUASI BREGMAN NOEXPANSIVE MAPPINGS

G. ZAMANI ESKANDANI AND M. RAEISI

*Faculty of Sciences, Department of Mathematics,  
University of Tabriz, Tabriz, Iran*

[zamani@tabrizu.ac.ir](mailto:zamani@tabrizu.ac.ir)

[m.raeisi@tabrizu.ac.ir](mailto:m.raeisi@tabrizu.ac.ir)

**Abstract.** In this paper, we propose a new iterative algorithm for finding common fixed points of infinitely countable family of quasi Bregman nonexpansive operators and common solutions of finite family of equilibrium problems in reflexive Banach spaces.

**Keywords:** Bregman projection, Legendre function, quasi Bregman nonexpansive, Equilibrium problems.

### References:

- [1] I. J. Maddox, "Elements of functional analysis", Cambridge University Press, New York, (1970).
- [2] L. M. Bregman, A relaxation method for finding the common point of convex sets and its application to the solution of problem in convex programming, USSR Comput. Math. Math. Phys., 7 (1967), 200- 217
- [3] J.W. Chen, Z. Wan and Y. Zou, Strong convergence theorems for firmly nonexpansive-type mappings and equilibrium problems in Banach spaces, Optimization, 62, 483-497.
- [4] S. Reich and S. Sabach, Two strong convergence theorems for Bregman strongly nonexpansive operators in reflexive Banach spaces, Nonlinear Anal., 73 (2010), 122-135
- [5] S. Reich and S. Sabach, Two strong convergence theorems for a proximal method in reflexive Banach spaces, Numer. Funct. Anal. Optim. 31 (2010), 22-44

## APPROXIMATE SOLUTIONS OF DELAY PSEUDO-PARABOLIC EQUATIONS

Gabil M. AMIRALIYEV<sup>1</sup>, İlhame AMIRALI<sup>2</sup>

<sup>1</sup>*Department of Mathematics, Erzincan University, Erzincan/TURKEY,*  
[gabilamirali@yahoo.com](mailto:gabilamirali@yahoo.com)

<sup>2</sup>*Department of Mathematics, Düzce University,*  
*Düzce/TURKEY*  
[ailhame@gmail.com](mailto:ailhame@gmail.com)

**Abstract:** In this presentation, linear and nonlinear pseudo-parabolic equations with time delay are examined. For the solving numerically the considered initial-boundary value problems difference schemes are constructed and analysed. Based on the method of energy estimates the order of convergence is obtained. The error estimates are obtained in the discrete norm. Some numerical results confirming the expected behavior of the method are shown.

**Keywords:** Pseudo-Parabolic, Initial-boundary value, Finite Difference, Delay Equations

### References:

- [1] Y. Fan, I. S. Pop, "A class of pseudo-parabolic equations: existence, uniqueness of weak solutions, and error estimates for the Euler-implicit discretization", *Mathematical Methods in the Applied Sciences*, 34 (2011), 2329-2339.
- [2] P. L. Davis, "A quasilinear parabolic and a related third-order problem", *Journal of Mathematical Analysis and Applications*, 40 (1972), 327-335.
- [3] G. M. Amiraliyev, I. G. Amiraliyev, "Difference schemes for the singularly Perturbed Sobolev Equations", in *Proceedings of the International Conference on Difference Equations, Special Functions and Applications*, pp. 23-40, Munich, Germany, 2005.

## SOME IDENTITIES OF THE HUMBERT AND GENERALIZED CHEBYSHEV POLYNOMIALS

Gulsah OZDEMIR, Yılmaz SIMSEK

*Department of Mathematics, Akdeniz University,  
Antalya/TURKEY*

[ozdemir.gulsah@hotmail.com](mailto:ozdemir.gulsah@hotmail.com), [ysimsek@akdeniz.edu.tr](mailto:ysimsek@akdeniz.edu.tr)

**Abstract:** In [1], we constructed some generating functions for two-variable polynomials related to a family of the Fibonacci type polynomials and numbers. By using these functions and their functional equations with PDE, we derived many identities and relations associated with some well-known polynomials and numbers such as the Fibonacci numbers, the Fibonacci polynomials, the Jacobsthal polynomials, the Chebyshev polynomials, the Vieta-Fibonacci polynomials, the Vieta-Lucas polynomials, the Humbert polynomials and the Geganbauer polynomials. In this paper, we modify generating functions for the two-variable polynomials of the Fibonacci type polynomials. By using these generating functions, we give many new identities and relations for the Humbert polynomials and the generalized Chebyshev polynomials. Finally, we give some remarks and observations on these generating functions and related infinite series.

**Keywords:** Generating function, Fibonacci numbers and polynomials, Chebyshev polynomials, Humbert polynomials, Geganbauer polynomials.

### References:

- [1] G. Ozdemir, Y. Simsek, Generating Functions For Two-Variable Polynomials Related To A Family of Fibonacci Type Polynomials and Numbers, to appear in Filomat 2016.
- [2] H. M. Srivastava and H. L. Manocha, A Treatise on Generating Functions, Ellis Horwood Limited Publisher, Chichester (1984). Kumar, "Strong Convergence of a New Three Step Iterative Scheme in Banach Spaces", American Journal of Computational Mathematics, 2(2012), 345-357.
- [3] G. B. Djordjevic, Polynomials related to generalized Chebyshev polynomials, Filomat 23(3) (2009) 279-290.
- [4] M. Giuseppe, M. Gradimir, Interpolation Processes Basic Theory and Applications, Springer-Verlag Berlin Heidelberg, 2008.

## A NEW SMOOTHING METHOD VIA BEZIER CURVE FOR NON-SMOOTH FUNCTIONS

Ahmet ŞAHİNER<sup>1</sup>, Gülden KAPUSUZ<sup>1</sup>, Nurullah YILMAZ<sup>1</sup>

<sup>1</sup>*Department of Mathematics, SuleymanDemirelUniversty,  
Isparta/TURKEY*

[guldenkapsuz92@gmail.com](mailto:guldenkapsuz92@gmail.com), [ahmetnur32@gmail.com](mailto:ahmetnur32@gmail.com),  
[nurullahyilmaz@sdu.edu.tr](mailto:nurullahyilmaz@sdu.edu.tr)

**Abstract:** In this study, we propose a new smoothing technique based on the Bezier curve for non-smooth functions. We use this smoothing approach in a global optimization method and construct an algorithm for this global optimization method. We apply the algorithm to the test problems in order to illustrate the efficiency of the method.

**Keywords:** Global Optimization, Non-Smooth, Non-Lipschitz, Smoothing

### References:

- [1] D. Bertsekas, Nondifferentiable optimization via approximation, *Mathematical Programming Study* 3 (1975) 1-25.
- [2] Zang, A smooting out technique for min-max optimization, *Math. Prog.*, 19 (1980), 61-77.
- [3] A. Ben-Tal, M. Teboule, Smoothing technique for nondifferentiable optimization problems, *lecture notes in mathematics*, 1405, Springer-Verlag, Heidelberg, 1989, 1-11.
- [4] C. Chen, O.L. Mangasarian, A Class of Smoothing Functions for Nonlinear and Mixed Complementarity Problem, *ComputOptimAppl*, 5, (1996) 97-138.
- [5] Farin, G., *A Survey of Curves and Surfaces Methods in CAGD*, Computer Aided Geometric Desing, 1984, 1-60.

## VIABILITY PROBLEM FOR SECOND ORDER DIFFERENTIAL INCLUSIONS

Gülseren ÇİÇEK<sup>1</sup>, Elimhan MAHMUDOV<sup>2</sup>

<sup>1</sup>*Department of Mathematics, Istanbul University,  
Istanbul/TURKEY*

[cicekgul@istanbul.edu.tr](mailto:cicekgul@istanbul.edu.tr)

<sup>2</sup>*Department of Mathematical Engineering, Istanbul Technical University,  
Istanbul/TURKEY*

[elimhan22@yahoo.com](mailto:elimhan22@yahoo.com)

**Abstract:** In this presentation, we derive the optimality conditions for the viability problem for second order differential inclusions. Applying optimality conditions of problems with geometric constraints, optimality conditions for second order discrete inclusions are formulated. Using locally adjoint mapping we conceive necessary and sufficient conditions for the optimality of the discrete approximation problem. Then passing to the limit, sufficient optimality conditions to the optimal problem described by second order differential inclusions are established.

**Keywords:** second order discrete differential inclusion, transversality condition, Euler-Lagrange inclusion, locally adjoint mapping, dual cone.

### References:

- [1] E. Mahmudov, "Approximation and Optimization of Discrete and Differential Inclusions", Elsevier, ISBN: 9789756797221, 396p. (2011).
- [2] J.P. Aubin, A. Cellina, "Differential Inclusions", Springer-Verlag, Grundlehren der Math., (1984), 342p.
- [3] E. Mahmudov, "Transversality Condition and optimization of higher order ordinary differential inclusions", Optimization: A Journal of Mathematical Programming and Operations Research, Vol.64, 10(2015), 2131-2144.
- [4] M. Aitalioubrahim, S. Sajid, "Viability problem with Perturbation in Hilbert Space", Electronic J. of Qualitative Theory of Differential Equations, 7(2007), 1-14.



## IDENTITIES ON THE $\varepsilon_{4n,1}$ -INTEGRAL TRANSFORM

A. Neşe DERNEK<sup>1</sup>, Gülşen MENSİMLİ<sup>2</sup>,

<sup>1</sup>Department of Mathematics, University of Marmara, Istanbul/TURKEY  
[ndernek@marmara.edu.tr](mailto:ndernek@marmara.edu.tr)

<sup>2</sup>Department of Mathematics, University of Marmara, Istanbul/TURKEY  
[gulsen.mensimli@yahoo.com](mailto:gulsen.mensimli@yahoo.com)

**Abstract:** In this presentation the authors prove a Parseval- Goldstein type theorem involving the  $\varepsilon_{\{4n,1\}}$ - generalized exponential integral transform. The theorem is then shown to yield a number of new identities involving several well- known integral transforms. Using the theorem and its corollaries a number of interesting infinite integrals are presented.

**Keywords**  $\varepsilon_{4n,1}$ -transform,  $L_{4n}$ -transform,  $P_{4n}$ -transform, Laplace transform, Parseval-Goldstein Type Theorems

### References:

- [1] D. Brown, N. Dernek, O. Yürekli, "Identities for the  $\varepsilon_{2,1}$  Transform and Their Applications", Appl. Math.Comput., 187(2007), 1557-1566.
- [2] N. Dernek, F. Aylıkçı, "Identities for the  $\mathcal{L}_n$ -transform, the  $\mathcal{L}_{2n}$ -transform and the  $P_{\{2n\}}$ -transform and their applications", J. Inequal. Spec. Funct., (2014), Vol. 5, Issue 4, 1-17.
- [3] N. Dernek, E. Ö. Ölçücü, F. Aylıkçı, "New Identities and Parseval type relations for the generalized integral transforms  $\mathcal{L}_{4n}$ ,  $P_{4n}$ ,  $F_{s,2n}$  and  $F_{c,2n}$ ", Appl. Math. Comput., 269, (2015), 536- 547.
- [4] N. Dernek, F. Aylıkçı, G. Balaban, "New identities for the generalized Glasser transform, the generalized Laplace transform and the  $\varepsilon_{2n,1}$ - transform", IECMSA-IV., Book of Abstracts, (2015), 135-138.
- [5] A. Erdelyi, W. Magnus, F. Oberhettinger, and F.G. Tricomi, "Tables of Integral Transforms", Vol. I, Vol II, New York: McGraw Hill, 1954.
- [6] W. Magnus, F. Oberhettinger, R. P. Soni, "Formulas and Theorems for the Special Functions of Mathematical", Physics Springer-Verlag New York Inc., (1966).

## ON THE PARANORMED TAYLOR SEQUENCE SPACES

SerkanDEMİRİZ<sup>1</sup>, Hacer Bilgin ELLİDOKUZOĞLU<sup>2</sup>

<sup>1</sup>Department of Mathematics, Gaziosmanpaşa University, Tokat/TURKEY  
[serkandemiriz@gmail.com](mailto:serkandemiriz@gmail.com)

<sup>2</sup>Department of Mathematics, RecepTayyipErdoğan University,  
Rize/TURKEY  
[hacer.bilgin@erdogan.edu.tr](mailto:hacer.bilgin@erdogan.edu.tr)

**Abstract:** In this study, the sequence spaces  $t_0^r(p)$ ,  $t_c^r(p)$  and  $t^r(p)$  of non-absolute type which are the generalization of the Maddox's sequence spaces have been introduced and it is proved that the spaces  $t_0^r(p)$ ,  $t_c^r(p)$  and  $t^r(p)$  are linearly isomorphic to the spaces  $c_0(p)$ ,  $c(p)$  and  $\ell$ , respectively. Furthermore, the  $\alpha$ -,  $\beta$ - and  $\gamma$ -duals of these spaces have been computed and their bases have been constructed and some topological properties of these spaces have been investigated. Besides this, some matrix classes have been characterized.

**Keywords:** Paranormed Taylor sequence spaces, matrix domain, matrix transformations

### References:

- [1] M. Kirişçi, On the Taylor sequence spaces of non-absolute type which Include the Spaces  $c_0$  and  $c$ , Journal of Mathematical Analysis, 6 (2) (2015), 22-35.
- [2] F. Başar, Summability Theory and Its Applications, BenthamScience Publ., e-books, Monographs, Istanbul, 2012.
- [3] K. G. Grosse-Erdmann, Matrixtransformations between the sequence spaces of Maddox. J. Math. Anal. Appl., 180 (1993), 223–238.
- [4] F. Başar, B. Altay, Matrix mappings on the space  $bs(p)$  and its  $\alpha$ -,  $\beta$ - and  $\gamma$ -duals, Aligarh Bull. Math., 21(1) (2002), 79-91.
- [5] I. J. Maddox, Paranormed sequence spaces generated by infinite matrices. Proc. Camb. Philos. Soc., 64 (1968), 335–340.

**ON THE TAYLOR SEQUENCE SPACES OF NON-ABSOLUTE TYPE WHICH INCLUDE THE SPACES  $\ell_p$  and  $\ell_\infty$ : ( $1 \leq p < \infty$ )**

Hacer Bilgin ELLİDOKUZUOĞLU<sup>1</sup>, Serkan DEMİRİZ<sup>2</sup>

<sup>1</sup>*Department of Mathematics, Recep Tayyip Erdoğan University,  
Rize /TURKEY*

[hacer.bilgin@erdogan.edu.tr](mailto:hacer.bilgin@erdogan.edu.tr)

<sup>2</sup>*Department of Mathematics, Gaziosmanpaşa University, Tokat /TURKEY*

[serkandemiriz@gmail.com](mailto:serkandemiriz@gmail.com)

**Abstract:** In this presentation, we introduce Taylor sequence spaces  $t_p^r$  and  $t_\infty^r$  consisting of all sequences whose  $T(r)$ -transforms are in the spaces  $\ell_p$  and  $\ell_\infty$ , respectively. We investigate some properties and compute  $\alpha$ -,  $\beta$ - and  $\gamma$ -duals of these spaces. Afterwards, we characterize some matrix classes of Taylor sequence spaces  $t_p^r$  and  $t_\infty^r$ .

**Keywords:** Taylor sequence spaces, matrix domain, matrix transformations

**References:**

- [1] M. Kirişçi, On the Taylor sequence spaces of non-absolute type which include the spaces  $c_0$  and  $c$ , Journal of Mathematical Analysis, 6 (2) (2015), 22-35.
- [2] F. Başar and B. Altay, On the space of sequences of  $p$ -bounded variation and related matrix mappings, Ukrainian Math. J., 55(1) (2003), 136-147.
- [3] F. Başar, Summability Theory and Its Applications, Bentham Science Publ., e-books, Monographs, Istanbul, 2012.
- [4] M. Stieglitz, H. Tietz, Matrixtransformationen von Folgenräumen Eine Ergebnisübersicht, Math. Z. 154 (1977), 1-16.
- [5] A. Wilansky, Summability through functional analysis, North-Holland Math., New York, 1984.

## LACUNARY STATISTICAL CONVERGENCE OF ORDER $(\alpha, \beta)$ AND STRONG $N_{\alpha}^{\beta}(\theta, p)$ –SUMMABILITY

Hacer ŞENGÜL

Department of Mathematics, Siirt University,  
Siirt/TURKEY

[hacer.sengul@hotmail.com](mailto:hacer.sengul@hotmail.com)

**Abstract:** In this presentation, we introduce the concepts of lacunary statistical convergence of order  $(\alpha, \beta)$  and strong  $N(\theta, p)$  –summability of order  $(\alpha, \beta)$  for sequences of complex (or real) numbers and give some inclusion relations between the sets of lacunary statistical convergence of order  $(\alpha, \beta)$ , strong  $N_{\alpha}^{\beta}(\theta, p)$  –summability and statistical convergence of order  $(\alpha, \beta)$ .

**Keywords:** Statistical convergence, lacunary sequence, strong summability.

### References:

- [1] R. Çolak, "Statistical convergence of order  $\alpha$ ", Modern Methods in Analysis and Its Applications, New Delhi, India: Anamaya Pub, (2010), 121-129.
- [2] J. Fridy, C. Orhan, "Lacunary Statistical Convergence", Pacific J. Math., 160, pp. (1993), 43-51.
- [3] J. Fridy, C. Orhan, "Lacunary Statistical Summability", J. Math. Anal. Appl, 173, pp. (1993), no. 2, 497-504.
- [4] M. Et, H. Şengül, "Some Cesaro-type summability spaces of order  $\alpha$  and lacunary statistical convergence of order  $\alpha$ ", *Filomat* 28 (2014), no. 8, 1593-1602.
- [5] H. Şengül, M. Et, "On lacunary statistical convergence of order  $\alpha$ ", *Acta Math. Sci. Ser. B Engl. Ed.* 34 (2014), no. 2, 473-482.
- [6] R. Savaş Eren, E. Savaş, "Double lacunary statistical convergence of order  $\alpha$ ", *Indian J. Math.* 57 (2015), no. 1, 1-15.
- [7] H. Çakallı, "A study on statistical convergence", *Funct. Anal. Approx. Comput.* 1 (2009), no. 2, 19-24.

## LACUNARY STATISTICAL CONVERGENCE OF ORDER $(\alpha, \beta)$ IN TOPOLOGICAL GROUPS

HacerŞENGÜL<sup>1</sup>, Mikail ET<sup>2</sup>

<sup>1</sup>*Department of Mathematics, Siirt University, Siirt/TURKEY*

[hacer.sengul@hotmail.com](mailto:hacer.sengul@hotmail.com)

<sup>2</sup>*Department of Mathematics, Fırat University, Elazığ/TURKEY*

[mikailet68@gmail.com](mailto:mikailet68@gmail.com)

**Abstract:** In this presentation, the concept of lacunary statistical convergence of order  $(\alpha, \beta)$  is generalized to topological groups, and some inclusion relations between the set of all statistically convergent sequences of order  $(\alpha, \beta)$  and the set of all lacunary statistically convergent sequences of order  $(\alpha, \beta)$  are given.

**Keywords:** Topological groups, statistical convergence, lacunary sequence.

### References:

- [1] H. Çakallı, "Lacunary statistical convergence in topological groups". *Indian J. Pure Appl. Math.* 26(1995), no. 2, 113-119.
- [2] H. Çakallı, E. Savaş, "Statistical convergence of double sequences in topological groups", *J. Comput. Anal. Appl.* 12 (2010), no. 2, 421-426.
- [3] J. Fridy, C. Orhan, "Lacunary Statistical Convergence", *Pacific J. Math.*, 160, pp. (1993), 43-51.
- [4] J. Fridy, C. Orhan, "Lacunary Statistical Summability", *J. Math. Anal. Appl.* 173, pp. (1993), no. 2, 497-504.
- [5] R. Çolak, "Statistical convergence of order  $\alpha$ ", *Modern Methods in Analysis and Its Applications*, New Delhi, India: Anamaya Pub, (2010), 121-129.

## $A^I$ -STATISTICAL CONVERGENCE OF ORDER $\alpha$ ( $0 < \alpha < 1$ )

Hafize GÜMÜŞ

<sup>1</sup>Department of Mathematics Education, Necmettin Erbakan University  
Ereğli/Konya/TURKEY  
[hgumus@konya.edu.tr](mailto:hgumus@konya.edu.tr)

**Abstract:** Following a very recent approach, in this study we investigate  $A^I$ -statistical convergence of order  $\alpha$  with respect to a sequence of modulus functions where  $A = (A_{ki})$  is an infinite matrix and  $\lambda = (\lambda_n)$  is a non-decreasing sequence of positive numbers. We call this new convergence as  $[S_A^\lambda(I, F)]^\alpha$ -convergence. Furthermore, we define  $[V_A^\lambda(I, F)]^\alpha$ -convergence and  $[S_A(I, F)]^\alpha$ -convergence and we mainly investigate their relationship.

**Keywords:** Statistical convergence, ideal, filter,  $A^I$ -statistical convergence,  $\lambda = (\lambda_n)$  sequence.

### References:

- [1] P. Das, E. Savas, "On  $I$ -statistical and  $I$ -lacunary statistical convergence of order  $\alpha$ ", Bull. Iranian Math. Soc., Vol.40, No.2 (2014), 459-472.
- [2] U. Yamanci, M. Gürdal, S. Saltan, " $A^I$ -statistical convergence with respect to a sequence of modulus functions", Contemporary analysis and Applied Mathematics, Vol.2, No.1(2014), 136-145.
- [3] T. Bilgin, "Lacunary strong  $A$ -convergence with respect to a modulus", Mathematica XLVI(4), (2001), 9-46.
- [4] J. S. Connor, "On strong matrix summability with respect to a modulus and statistical convergence", Canad. Math. Bull. 32(1989), 194-198.

## A NUMERICAL ANALYSIS FOR SOLUTION OF DIFFERENTIAL EQUATIONS USING THE COMPLEMENTARY FUNCTIONS METHOD

Hakan PEKEL

*Department of Mechanical Engineering, Nigde University,  
Nigde/TURKEY*  
[hpekel@nigde.edu.tr](mailto:hpekel@nigde.edu.tr)

**Abstract:** In some problems the assumption yields a two-point boundary value problem with a governing ordinary differential equation of variable coefficients. Since general analytical solutions of such equations especially for higher order ones are not available a numerical analysis method is employed. One of them is known as Complementary Functions Method (CFM). The main idea of the method is to reduce the boundary value problem to an initial-value problem. The problem considered is written in canonical form to transform a set of  $n$  linear ordinary differential equations. The homogeneous and particular solutions are obtained using matrix calculations. This study gives the accurate numerical results for some special cases using the Fortran's subroutines.

**Keywords:** Complementary functions method, canonical form, boundary value problems.

### References:

- [1] S.M. Roberts, J.S. Shipman, "Fundamental matrix and two-point boundary-value problems", *Journal of Optimization Theory and Applications*, 28.1(1979),77-78.
- [2] R.P. Agarwal, "On the method of complementary functions for nonlinear boundary-value problems", *J. Optimiz Theory Appl*, 36.1(1982), 139-144.
- [3] V.Yildirim, "Free vibration analysis of non-cylindrical coil springs by combined use of the transfer matrix and the complementary functions methods", *Commun. Numer. Meth. En.*,13(1997), 487-494.
- [4] N. Tutuncu, B. Temel, "An efficient unified method for thermoelastic analysis of functionally graded rotating disks of variable thickness", *Mechanics of Advanced Materials and Structures*, 20(2013), 38-46.

## PERFORMANCE ANALYSIS OF STOCHASTIC BEAM AND VARIABLE NEIGHBORHOOD SEARCH UNDER PARTIALLY SHADED PHOTOVOLTAIC SYSTEMS

Zehan KESILMIŞ<sup>1</sup>, Halil EROL<sup>1</sup>, Mahmut UÇMAN<sup>1</sup>

<sup>1</sup>*Department of Electrical and Electronics Engineering, OsmaniyeKorkut Ata University,*

*Osmaniye/TURKEY*

[halilerol@osmaniye.edu.tr](mailto:halilerol@osmaniye.edu.tr)

**Abstract:** Solar photovoltaic (PV) array which is exposed to the uniform solar irradiance exhibits the non-linear Power-Volt characteristic. Maximum power point (MPP) tracking is challenging due to varying climatic conditions in solar photovoltaic (PV) system. Also, the tracking algorithm becomes more complicated due to the presence of multiple peaks in the power voltage characteristics under the condition of partial shading. This paper presents a Stochastic Beam Search (SBS) based algorithm and Variable neighborhood search (VNS) for maximum power point tracking (MPPT) at partial shading condition in PV system. A mast is placed in front of the modules so as to scatter the partial shading effect over the entire array. The rearrangement of modules is performed without varying the electrical connection of the modules in the array. It is validated that the power generation of array under a moving shadow condition is enhanced and the various partial shading losses are reduced by optimal parameter selection.

**Keywords:** Solar Photovoltaic; MPPT; Partial Shading, Stochastic beam search, Variable neighborhood search.

### References:

- [1] Syafaruddin, Karatepe E, Hiyama T. Polar coordinate fuzzy controller based real-time maximum-power point control of photovoltaic system. *Renew Energy* 2009;34:2597e606.
- [2] Maki A, Valkealahti S. Power losses in long string and parallel-connected short strings of series-connected silicon-based photovoltaic modules due to partial shading conditions. *IEEE Trans Energy Convers* 2012;27:173e83.
- [3] Martinez-Moreno F, Munoz J, Lorenzo E. Experimental model to estimate shading losses on PV arrays. *Sol Energy Mater Sol Cells* 2010;94:2298e303.



## A STUDY ON ABSOLUTE ALMOST CONVERGENCE

Hamdullah ŞEVLİ<sup>1</sup>, Büşra BALKAŞ<sup>2</sup>

<sup>1</sup>*Department of Mathematics, İstanbul Commerce University,  
İstanbul/TURKEY*

[hsevli@ticaret.edu.tr](mailto:hsevli@ticaret.edu.tr)

<sup>2</sup>*Graduate School of Natural and Applied Sciences, İstanbul Commerce  
University, İstanbul/TURKEY*

[busra-balkas@hotmail.com](mailto:busra-balkas@hotmail.com)

**Abstract:** Lorentz [1] provided an authentic characterization of almost convergent sequences. Using Lorentz's definition a lot of papers appeared dealing with almost convergence. Among them Nanda and Nayak [2] defined the concept of almost bounded variation and later Das, Kuttner and Nanda [3] introduced the concept of absolute almost convergence. The aim of this presentation is to survey this two concepts and to describe some of the many results which have been proved for absolute almost convergence. Furthermore, some matrix transformations have been characterized.

**Keywords:** Almost convergence, absolute almost convergence, absolute summability.

### References:

- [1] G.G. Lorentz, "A contribution to the theory of divergent series", Acta Math. 80 (1948) 167–190.
- [2] S. Nanda, K.C. Nayak, "Some new sequence spaces", Indian J. Pure Appl. Math. 9 (8) (1978) 836–846.
- [3] G. Das, B. Kuttner, S. Nanda, "Some sequence spaces and absolute almost convergence", Trans. Amer. Math. Soc., 283 (1984) 729–739.
- [4] G. Das and B. K. Ray, "Lack of Tuberaian Theorem for Absolute Almost Convergence", Analysis Mathematica, 35(2009), p.37-49.
- [5] E. Savaş, H. Şevli, B.E. Rhoades, "Triangles which are bounded operators on  $A_k$ ", Bulletin of the Malaysian Mathematical Sciences Society, 32(2), (2009), 223-231.

## COMPOSITION OPERATORS ON WEIGHTED BESOV SPACES

Hamid VAEZI<sup>1</sup>, Ebrahim ZAMANI<sup>2</sup>

<sup>1</sup>*Department of Mathematics, University of Tabriz,  
Tabriz, IRAN*

[hvaezi@tabrizu.ac.ir](mailto:hvaezi@tabrizu.ac.ir)

<sup>2</sup>*Department of Mathematics, University of Tabriz,  
Tabriz, IRAN*

[Ebrahim485@yahoo](mailto:Ebrahim485@yahoo).

**Abstract:** Let  $D$  denote the open unit disc in the complex plane and  $A$  is normalized Lebesgue measure on  $D$ . The weighted Besov space  $B_p(\sigma)$ ; ( $p > 1$ ) is the space of analytic functions  $f$  on  $D$  such that  $\int_D |f'(z)|^p \sigma(z) dA(z) < \infty$ , where  $\sigma$  is a weight function on  $D$ . In this article we study composition operators on weighted Besov spaces with admissible Bekolle weights.

**Keywords:** Composition operator, Bekolle weight, Besov space.

### References:

- [1] D. Békollé, "Inégalité a poids pour le projecteur de Bergman dans la boule unité de  $\mathbb{C}^n$ ", *Studia Math.*, 71(1981/82) 305-323.
- [2] O. Constantin, "Carleson embeddings and some classes of operators on weighted Bergman spaces", *J. Math. Anal. Appl.*, 365(2010), 668-682.
- [3] K. Kellay, P. Lefevre, "Compact composition operators on weighted Hilbert spaces of analytic functions", *J. Math. Anal. Appl.* 386(2012), 718-727.
- [4] K. Zhu, "Operator Theory in Function Spaces", Marcel Dekker, New York, 1990.

## IMPROVING THE CONVERGENCE ORDER OF THE REGULARIZATION METHOD FOR FREDHOLM INTEGRAL EQUATIONS OF THE SECOND KIND

Hamza GUEBBAI, Sami SEGNI

**Abstract:** We build a numerical approximation method, for Fredholm integral equation solution of the second type. This method is based on the regularization by convolution and Fourier series expansion. It provides a better convergence order.

**Keywords:** Integral equation; Weak singularity; Convolution; Fourier series

### References:

- [1] M. Ahues, F.D. d'Almeida, R.R. Fernandes Piecewise constant Galerkin approximations of weakly singular integral equations Int. J. Pure Appl. Math., 55 (4) (2009), pp. 569–580
- [2] M. Ahues, A. Largillier, B.V. Limaye Spectral Computations with Bounded Operator, CRC, Boca Raton (2001)
- [3] K.E. Atkinson A Survey of Numerical Methods for the Solution of Fredholm Integral Equations of the Second Kind, Society for Industrial and Applied Mathematics, Philadelphia, Pa. (1976)
- [4] H. Guebbai, Regularization and Fourier series for Fredholm integral equations of the second kind with a weakly singular kernel, Accepted in Num. Fun. Ana. Opti.

## EULER SUMMABILITY KIND VARIOUS CONVERGENCE OF SETS

Harun POLAT

*MuşAlparslan University Art and Science Faculty, Department of Mathematics,  
Muş / Turkey.*

[h.polat@alparslan.edu.tr](mailto:h.polat@alparslan.edu.tr)

**Abstract.** In this paper we present definitions of Kuratowski Euler convergence, Hausdorff Euler convergence, Wijsman Euler convergence, Fisher Euler convergence and Mosco Euler convergence of sequences of sets. Also we characterize the connection between of their.

**Keywords.** Euler convergence, Kuratowski, Hausdorff, Wijsman, Fisher and Mosco convergence.

### References:

- [1] C. Kuratowski, "Topology", Academic Press, New York, 1966.
- [2] J.G. Kemeny, J.L. Snell, "Finite Markov Chains", D.VanNostrand, Princeton, NJ, 1960.
- [3] M. Baronti, P. Papini, "Convergence of sequences of sets, Methods of functional analysis in approximation theory", ISNM 76, Birkhauser, Basel, 1986.
- [4] Y. Sonntag, C. Zălinescu, "Set convergences, An attempt of classification", Trans. Amer. Math. Soc. 340 (1) (1993) 199-226.

## GIBBS MEASURES FOR THE POTTS-SOS MODEL WITH FOUR STATES ON CAYLEY TREE OF ORDER ARBITRARY

Halit SAYGILI<sup>1</sup>, Hasan AKIN<sup>2</sup>

<sup>1</sup>*Department of Mathematics, Gaziantep University, 27310  
Gaziantep/TURKEY  
[hsaygili@gantep.edu.tr](mailto:hsaygili@gantep.edu.tr)*

<sup>2</sup>*Department of Mathematics, Faculty of Education, Zirve University, 27260  
Gaziantep / Turkey  
[hasan.akin@zirve.edu.tr](mailto:hasan.akin@zirve.edu.tr)*

**Abstract:** In this paper, we study a new model, the so-called Potts and solid-on-solid model (mixed P-SOS model), with spin values 0,1,2,3 on a Cayley tree of order arbitrary. We prove the existence Gibbs measures by analyzing fixed points of one-dimensional system of equations. We obtain all translation-invariant splitting Gibbs measures corresponding to the model. These measures are categorized by solutions to a nonlinear vector-valued functional equation.

**Keywords:** Cayley tree, Gibbs measure, Potts-Sos model, Configuration space.

### References:

- [1] F.Y. Wu, "The Potts model", Rev. Mod. Phys., 54 (1982) 235-268.
- [2] C. Kuelske, U. A. Rozikov, "Extremality of translation-invariant phases for a three-state sos-model on the binary tree", J. Stat Phys., 160 (3), (2015) 659-680.
- [3] Rozikov, U.A., Shoyusupov, ShA, "Gibbs measures for the SOS model with four states on a Cayley tree", Theor. Math. Phys. 149(1), (2006)1312-1323.
- [4] A. E. Mazel and Yu. M. Suhov, "Random surfaces with two-sided constraints: An application of the theory of dominant ground states" J. Stat Phys., 64,(1991)111-134.

## BOUNDEDNESS OF THE CALDERON-ZYGMUND SINGULAR INTEGRAL OPERATOR AND ITS COMMUTATORS ON MODIFIED MORREY SPACES

Hatice ARMUTCU<sup>1</sup>, Yusuf ZEREN<sup>2</sup> and Vagif S. GULIYEV<sup>3</sup>

<sup>1,2</sup>*Department of Mathematics, Yildiz Technical University,  
İstanbul/TURKEY*

[malinki05@windowslive.com](mailto:malinki05@windowslive.com), [yzeren@yildiz.edu.tr](mailto:yzeren@yildiz.edu.tr)

<sup>3</sup>*Department of Mathematics, Ahi Evran University,  
Kırşehir/TURKEY*

*Institute of Mathematics and Mechanics of NAS of  
Azerbaijan / Baku*

[vagif@guliyev.com](mailto:vagif@guliyev.com)

### Abstract:

Let  $1 \leq p < \infty$ ,  $0 \leq \lambda \leq n$ ,  $[t]_1 = \min\{1, t\}$ . We denote by  $\tilde{L}_{p,\lambda} = \tilde{L}_{p,\lambda}(\mathbb{R}^n)$  the modified Morrey space, as the set of locally integrable functions  $f(x)$ ,  $x \in \mathbb{R}^n$ , with the finite norms

$$\|f\|_{\tilde{L}_{p,\lambda}} = \sup_{\substack{t>0, \\ x \in \mathbb{R}^n}} \left( [t]_1^{-\lambda} \int_{B(x,t)} |f(y)|^p dy \right)^{\frac{1}{p}}$$

We study the boundedness of the Calderon-Zygmund singular integral and its commutators on modified Morrey spaces.

**Keywords:** Calderon-Zygmund singular integral operator, commutator Calderon-Zygmund singular integral operator, modified Morrey space, BMO space.

### References:

- [1] Guliyev, V.S., Hasanov, J., ve Zeren, Y., (2011). "Necessary and Sufficient Conditions for the Boundedness of the Riesz Potential in Modified Morrey Spaces", Journal Mathematical Inequalities, Volume 5, Number 4: 491-506.

## ON WEIGHTED IYENGAR TYPE INEQUALITIES FOR CONFORMABLE FRACTIONAL INTEGRALS

M. Zeki SARIKAYA<sup>1</sup>, Hatice YALDIZ<sup>2</sup>

<sup>1</sup>*Department of Mathematics, Duzce University,  
Duzce/TURKEY*

[sarikayamz@gmail.com](mailto:sarikayamz@gmail.com)

<sup>2</sup>*Department of Mathematics, Duzce University,  
Duzce/TURKEY*

[yaldizhatice@gmail.com](mailto:yaldizhatice@gmail.com)

**Abstract:** In this presentation, we establish integral inequalities of Iyengar's inequality type involving conformable fractional integrals.

**Keywords:** Iyengar inequality, weighted quadrature rule, conformable fractional integral.

### References:

- [1] D. R. Anderson, Taylor's formula and integral inequalities for conformable fractional derivatives, arXiv:1409.5888, 2014.
- [2] P. Cerone, S.S. Dragomir, On a weighted generalization of Iyengar type inequalities involving bounded first derivative, *Math. Inequal. Appl.* 3(1) (2000)35-44.
- [3] D.S. Mitrinović, J.E. Pečarić, A.M. Fink, *Inequalities for Functions and Their Integrals and Derivatives*, Kluwer Academic Publishers, 1994.
- [4] M. Abu Hammad, R. Khalil, conformable fractional heat differential equations, *International Journal of Differential Equations and Applications* 13( 3), 2014, 177-183.
- [5] M. Abu Hammad, R. Khalil, Abel's formula and wronskian for conformable fractional differential equations, *International Journal of Differential Equations and Applications* 13( 3), 2014, 177-183.
- [6] R. Khalil, M. Al horani, A. Yousef, M. Sababheh, A new definition of fractional derivative, *Journal of Computational Applied Mathematics*, 264 (2014), 65-70.
- [7] D. S. Mitrinović, J. E. Pečarić and A. M. Fink, *Classical and New Inequalities in Analysis*, Kluwer Academic Publishers, 1993.

## ON TRIGONOMETRIC APPROXIMATION BY DEFERRED-NÖRLUND $(D.N_p)$ MEANS IN $LIP_\alpha$ CLASS

Hilal BAYINDIR<sup>1</sup>, UğurDEĞER<sup>2</sup>

<sup>1</sup>Department of Mathematics, Mersin University, Mersin/TURKEY

[hilalbayindir2@gmail.com](mailto:hilalbayindir2@gmail.com)

<sup>2</sup>Department of Mathematics, Mersin University, Mersin/TURKEY

[udeger@mersin.edu.tr](mailto:udeger@mersin.edu.tr)

**Abstract:** In [1], Lal studied the degree of approximation for the functions belonging to the  $Lip_\alpha$  ( $0 < \alpha \leq 1$ ) class using Cesáro-Nörlund  $(C^1.N_p)$  means of their Fourier series where  $p := \{p_n\}$  is a non-increasing sequence. Later Mishra *et al.* investigated the degree of approximation of conjugate functions belonging to the  $Lip_\alpha$  class by  $(C^1.N_p)$  means of conjugate series of its Fourier series in [2] where the condition of monotonicity on the sequence  $p$  was replaced by a weaker assumption. In [3], we know that the deferred Cesáro means which was considered by R<sub>p</sub> Agnew has useful properties not possessed by the Cesáro means. Taking into deferred Cesáro means we will give Deferred-Nörlund  $(D.N_p)$  means and with this perspective we shall present results related to trigonometric approximation of functions belonging to Lipschitz class by the  $(D.N_p)$  means of its Fourier series. Moreover, we state results on degree of approximation to conjugates of functions belonging to Lipschitz class by the  $(D.N_p)$  means of its conjugate Fourier series.

**Keywords:** Lipschitz class, Deferred-Cesaromeans, Deferred-Nörlund means, Trigonometric approximation

### References:

- [1] S.Lal, "Approximation of functions belonging to the generalized Lipschitz class by  $(C^1.N_p)$  summability method of fourier seies", Applied Mathematics and Computation, 209(2009), 346-350.
- [2] L.N.Mishra, V.N.Mishra and V.Sonavane, "Trigonometric approximation of functions belonging to Lipschitz class by matrix  $(C^1.N_p)$  operator of conjugate series Fourier series", 1(2013), 127.
- [3] RPAgnew, "On deferred Cesáromeans", Ann. Math., [2] 33 [3] (1932), 413-421.



## EXPONENT OF CONVERGENCE OF SOLUTIONS OF CERTAIN LINEAR DIFFERENTIAL EQUATIONS IN THE DISC

Houari FETTOUCH

*Department of Mathematics, Abdelhamid Ibn Badis University,  
Mostaganem/ALGERIA*

[houari.fettouch@univ-mosta.dz](mailto:houari.fettouch@univ-mosta.dz)

**Abstract:** In this paper we investigate the  $n$ -iterated exponent of convergence of  $f^{(i)}-\varphi$  where  $f \neq 0$  is a solution of linear differential equation with analytic or meromorphic coefficients in the unit disc and  $\varphi$  is a small function of  $f$  by making use the Nevanlinna theory of values distribution of a meromorphic function (see [1]). This work is an extension and counterpart of recent results in the complex plane by Xu et al. [2] and Tu et al. [3], to the unit disc.

**Keywords:** Linear differential equations, exponent of convergence of solutions, order of growth.

### References:

- [1] W.K. Hayman, Meromorphic functions, Clarendon Press, Oxford, 1964.
- [2] H.Y. Xu, J. Tu, and X.M. Zheng, On the hyper exponent of convergence of zero of  $f^{(i)}-\varphi$  of higher order linear differential equation, Advances in Difference Equations, Vol. 2012(2012), No. 114, 1-16.
- [3] J. Tu, and H.Y. Xu, On the hyper exponent of convergence of zero of  $f^{(i)}-\varphi$  of higher order linear differential equation, Advances in Difference Equations, Vol. 2013 (2013), No. 71, 1-16.

## COUPLED COINCIDENCE POINT THEOREMS FOR A GENERALIZED COMPATIBLE IN PARTIALLY METRIC SPACES

Hukmi KIZILTUNC<sup>1</sup>, Esra YOLACAN<sup>2</sup>

<sup>1</sup>Department of Mathematics, Ataturk University, Erzurum/TURKEY  
[hukmu@atauni.edu.tr](mailto:hukmu@atauni.edu.tr)

<sup>2</sup>Republic of Turkey Ministry of National Education, Tokat/TURKEY  
[yolacanesra@gmail.com](mailto:yolacanesra@gmail.com)

**Abstract:** In this presentation, in the setting of partially ordered metric spaces, using the notion of generalized compatibility of a pair  $\{F, G\}$ , of mappings  $F, G: X \times X \rightarrow X$ , we establish the existence and uniqueness of coupled coincidence point involving  $(\varphi, \psi)$ -contractive condition without mixed  $G$ -monotone property of  $F$ . Hence the derived coupled fixed point results do not have the mixed monotone property of  $F$ . Our results improve and generalize the results of Jain et al. (Journal of Inequality and Applications 2012 2012:285.) and Berinde (Nonlinear Anal. TMA 74, 983-992 (2011)).

**Keywords:** Coupled coincidence point, generalized compatibility, ordered set.

### References:

- [1] M. Jain, K. Tas, S. Kumar, N. Gupta, "Coupled common fixed point results involving a  $(\varphi, \psi)$ -contractive condition for mixed  $g$ -monotone operators in partially ordered metric spaces", Journal of Inequalities and Applications, 2012, **2012**: 285.
- [2] V. Berinde, "Coupled fixed point for  $\phi$ -contractive mixed monotone mappings in partially ordered metric spaces", Nonlinear Anal. TMA 75, 3218-3228 (2012).
- [3] N. V. Luong, N. X. Thuan, "Coupled fixed points in partially ordered metric spaces and application" Nonlinear Anal. TMA 74, 983-992 (2011).
- [4] T.G. Bhaskar, V. Lakshmikantham, "Fixed point theorems in partially ordered metric spaces and applications", Nonlinear Anal. TMA 65, 1379-1393 (2006).

## A VARIATION ON HALF CAUCHY SEQUENCES

Huseyin CAKALLI

*Graduate School of Science and Engineering, Maltepe  
University, Istanbul/TURKEY*

[huseyincakalli@maltepe.edu.tr](mailto:huseyincakalli@maltepe.edu.tr); [hcakalli@gmail.com](mailto:hcakalli@gmail.com)

**Abstract:** In this presentation, we investigate the concepts of up continuity and down continuity. A real valued function  $f$  on a subset  $E$  of  $\mathbb{R}$ , the set of real numbers is up continuous if it preserves upward half Cauchy sequences, i.e. the sequence  $(f(\alpha_n))$  is upward half Cauchy whenever  $(\alpha_n)$  is an upward half Cauchy sequence of points in  $E$ ; and is down continuous if it preserves downward half Cauchy sequences, i.e. the sequence  $(f(\alpha_n))$  is downward half Cauchy whenever  $(\alpha_n)$  is a downward half Cauchy sequence of points in  $E$ , where a sequence  $(\alpha_k)$  of points in  $\mathbb{R}$  is called upward half Cauchy if for each  $\epsilon > 0$  there exists an  $n_0 \in \mathbb{N}$  such that  $\alpha_m - \alpha_n < \epsilon$  for  $m > n \geq n_0$ , and called downward half Cauchy if for for each  $\epsilon > 0$  there exists an  $n_0 \in \mathbb{N}$  such that  $\alpha_m - \alpha_n < \epsilon$  for  $m > n \geq n_0$ . It turns out that not only the set of up continuous functions, but also the set of down continuous functions is a proper subset of the set of continuous functions.

**Keywords:** Sequences, series, summability, continuity.

### References:

- [1] D. Burton, J. Coleman, "Quasi-Cauchy sequences", Amer. Math. Monthly, 117 (2010), 328-333.
- [2] H.Cakalli, "Sequential definitions of compactness", Appl. Math.Lett.21 (2008), 594-598.
- [3] H.Cakalli, "Forward continuity", J.Comput.Anal.Appl. 13 (2011), 225-230.
- [4] H. Cakalli, "On G-continuity", Comput.Math. Appl. 61 (2011), 313-318.
- [5] J. Collins and J. Zimmer, "An asymmetric Arzelà-Ascoli theorem", Topology and its Applications, 154(2007), 2312-2322.
- [6] J.Connor and K.G. Grosse-Erdmann, "Sequential definitions of continuity for real functions", Rocky Mountain J. Math., 33(1)(2003), 93-121.
- [7] O. Mucuk, T. Sahan, "On G-Sequential Continuity", Filomat, 28 (2014), 1181-1189.
- [8] F.J. Palladino, "On half Cauchy sequences", Arxiv:1102.4641v1, (2012), 3 pages.
- [9] I.L. Reilly, P.V. Subrahmanyam, and M.K. Vamanamurthy, "Cauchy sequences in quasi pseudometric spaces", Monatsh. Math., 93(2) (1982), 127-140.

## A VARIATION ON LACUNARY STATISTICAL QUASI CAUCHY SEQUENCES

Huseyin ÇAKALLI<sup>1</sup>, Huseyin KAPLAN<sup>2</sup>

<sup>1</sup>Graduate School of Science and Engineering, Maltepe University, Istanbul/TURKEY

[huseyincakalli@maltepe.edu.tr](mailto:huseyincakalli@maltepe.edu.tr); [hcakalli@gmail.com](mailto:hcakalli@gmail.com)

<sup>2</sup>Department of Mathematics, Nigde University, Nigde/TURKEY

[hkaplan@nigde.edu.tr](mailto:hkaplan@nigde.edu.tr)

**Abstract:** In this presentation, the concept of a lacunary statistically  $\delta$ -quasi-Cauchy sequence is investigated. In this investigation, we proved interesting theorems related to lacunary statistically  $\delta$ -ward continuity, and some other kinds of continuities. A real valued function  $f$  defined on a subset  $A$  of  $\mathbb{R}$ , the set of real numbers, is called lacunary statistically  $\delta$ -ward continuous on  $A$  if it preserves lacunary statistically  $\delta$ -quasi-Cauchy sequences of points in  $A$ , i.e.  $(f(\alpha_k))$  is a lacunary statistically  $\delta$ -quasi-Cauchy sequence whenever  $(\alpha_k)$  is a lacunary statistically  $\delta$ -quasi-Cauchy sequence of points in  $A$ , where a sequence  $(\alpha_k)$  is called lacunary statistically  $\delta$ -quasi-Cauchy if  $(\Delta\alpha_k)$  is a lacunary statistically quasi-Cauchy sequence. It turns out that the uniform limit process preserves this kind of continuity, and the set of lacunary statistically  $\delta$ -ward continuous functions is a closed subset of the set of continuous functions.

**Keywords:** Sequences, series, summability, continuity.

### References:

- [1] D. Burton, J. Coleman, "Quasi-Cauchy sequences", Amer. Math. Monthly, 117 (2010), 328-333.
- [2] H.Cakalli, "Sequential definitions of compactness", Appl. Math.Lett.21 (2008), 594-598.
- [3] H.Cakalli, "Forward continuity", J.Comput.Anal.Appl. 13 (2011), 225-230.
- [4] H. Cakalli, "On G-continuity", Comput.Math. Appl. 61 (2011), 313-318.
- [5] H. Cakalli, delta-quasi-Cauchy sequences, Math. Comput.Modelling, 53, No:1-2, (2011), 397-401. MR
- [6] H.Cakalli, C.G. Aras, A. Sonmez, "Lacunary statistical ward continuity", AIP Conf. Proc. 1676, 020042 (2015); <http://dx.doi.org/10.1063/1.4930468>
- [7] J.Connor and K.G. Grosse-Erdmann, "Sequential definitions of continuity for real functions", Rocky Mountain J. Math., 33(1)(2003), 93-121.
- [8] J.A. Fridy, and C.Orhan, "Lacunary statistical convergence", Pacific J. Math., 160(1) (1993), 43-51.

## ON COMPUTING THE AVERAGE LOWER DOMINATION NUMBERS OF SOME TREES

Hüseyin AKSAN<sup>1</sup>, Tufan TURACI<sup>2</sup>

<sup>1</sup>Department of Mathematics, Karabük University,  
Karabük/TURKEY

[huseyin.aksn25@gmail.com](mailto:huseyin.aksn25@gmail.com)

<sup>2</sup>Department of Mathematics, Karabük University,  
Karabük/TURKEY

[tufanturaci@karabuk.edu.tr](mailto:tufanturaci@karabuk.edu.tr)

**Abstract:** Let  $G = (V(G), E(G))$  be an undirected simple connected graph and let  $D \subseteq V(G)$  be a set of vertices. The set  $D$  is a  $k$ -dominating set of  $G$  if  $|N_G(u) \cap D| \geq k$  for all  $u \in V(G) \setminus D$ , where  $k \in \mathbb{N}^+$ . The  $k$ -domination number  $\gamma_k(G)$  of  $G$  is the minimum cardinality of a  $k$ -dominating set of  $G$ . 1-domination number is also called domination number  $\gamma(G)$  and 1-domination set is called dominating set. The average lower domination number of  $G$ , denoted by  $\gamma_{av}(G)$ , is defined as

$$\gamma_{av}(G) = \frac{1}{|V(G)|} \sum_{v \in V(G)} \gamma_v(G),$$
 where the lower domination number  $\gamma_v(G)$  is

the minimum cardinality of a dominating set of the graph  $G$  that contains the vertex  $v$ . In this presentation, exact values of the average lower domination number and average lower 2-domination number of some trees namely comet graph, double comet graph,  $k$ -ary tree and  $E_p^t$  graph are obtained.

**Keywords:** Connectivity; Domination number; Average lower domination numbers; Trees.

### References:

- [1] E. Aslan and A. Kirlangic, "The Average Lower Domination Number of Graphs", Bulletin of the Inter. Math. Virt. Inst., 3(2013), 155-160.
- [2] M.A. Henning, "Trees with Equal Average Domination and Independent Domination Numbers", Ars Combinatoria, 71(2004), 305-318.
- [3] T. Turacı, "The Concept of Vulnerability in graphs and Average Lower 2-domination Number", 28.th National Mathematics Conference, September 7-9, 2015, Antalya/TURKEY.

## THE AVERAGED MODULUS OF SMOOTHNESS AND ONE SIDED APPROXIMATION IN ORLICZ SPACES

Hüseyin KOÇ

<sup>1</sup>MEB, Department of Mathematics, Balıkesir University,  
Balıkesir/TURKEY

[huseyinkoc79@yahoo.com](mailto:huseyinkoc79@yahoo.com)

**Abstract:** In this presentation, firstly we give basic properties of averaged modulus of smoothness in Orlicz spaces  $L_\varphi^*$ . Then we prove some direct and converse one sided approximation problems in Orlicz spaces  $L_\varphi^*$

**Keywords:** Averaged modulus of smoothness, one sided approximation, direct theorem, converse theorem.

### References:

- [1] R. Akgün, "Inequalities for one sided approximation in Orlicz spaces, Hacettepe journal of mathematics and statistics"40(2), 231-240, (2011).
- [2] A.YU. Sadrin, "Orders of one sided approximations of functions in  $L_p$ -metric, Analysis Mathematica", 12,175-184,(1986).
- [3] B.Sendov, V. A. Popov, "The averaged moduli of smoothness", Pure and Applied Mathematics,(New York), Wiley, Chichester, (1988).
- [4] H. Koc, "Simultaneous approximation of functions in Orlicz spaces with Muckenhoupt weights", Complex Variables and Elliptic Equations, Taylor and Francis, England, DOI: 10.1080/17476933.2016.1142538
- [5] H. Koç, "Simultaneous Approximation by Polynomials in Orlicz Spaces Generated by Quasiconvex Young Functions", Kuwait Journal of Science, Kuwait, in press.
- [6] H. Koç, R. Akgün, "Approximation by Interpolating Polynomials in Weighted Symmetric Smirnov Spaces", Hacettepe journal of mathematics and statistics. 41 (5), 343-349, (2012).

## ON THE PARAMETERIZED SINGULARLY PERTURBED BOUNDARY VALUE PROBLEMS

Ilhame AMIRALI<sup>1</sup>, Gabil M. AMIRALIYEV<sup>2</sup>

<sup>1</sup>*Department of Mathematics, Düzce University,  
Düzce/TURKEY*

[ilhame@gmail.com](mailto:ilhame@gmail.com)

<sup>2</sup>*Department of Mathematics, Erzinçan University, Erzinçan/TURKEY*

[gabilamirali@yahoo.com](mailto:gabilamirali@yahoo.com)

**Abstract:** In this presentation, the boundary value problems for parameterized singularly perturbed second-order nonlinear ordinary differential equation are considered. The boundary layer behavior of the solution and its first and second derivatives have been established. Examples are presented which are in agreement with the theoretical analysis.

**Keywords:** Depending on a parameter, Asymptotic bounds, Singular perturbation, Boundary layer.

### References:

- [1] G. M. Amiraliyev, M. Kudu, H. Duru, "Finite Difference Method for Parameterized Singularly Perturbed Problem", J. Appl. Math., 3 (2004), 191-199.
- [2] I. G. Amiraliyeva, G. M. Amiraliyev, "Uniform Difference Method for Parameterized Singularly Perturbed Delay Differential Equations", Numer. Algor., 52(2009), 509-520.
- [3] P. A. Farrel, A. F. Hegarty, J. J. H. Miller, E. O'Riordan, G. I. Shishkin, "Robust Computational Techniques for Boundary Layers", Chapman Hall/CRC, New York, 2000.

## OPERATIONS ON $\mathbb{B}^{-1}$ -CONVEX SETS AND $\mathbb{B}^{-1}$ -CONVEX FUNCTIONS

Gabil ADILOV<sup>1</sup>, İlknur YESILCE<sup>2</sup>

<sup>1</sup>*Department of Mathematics, Akdeniz University,  
Antalya/TURKEY*

[gabiladilov@gmail.com](mailto:gabiladilov@gmail.com)

<sup>2</sup>*Department of Mathematics, Mersin University,  
Mersin/TURKEY*

[ilknuryesilce@gmail.com](mailto:ilknuryesilce@gmail.com)

**Abstract:**  $\mathbb{B}^{-1}$ -convexity that is an important abstract convexity type for mathematical economy was introduced in [1,2]. Its applications to mathematical economy were given in [2]. Separation of  $\mathbb{B}^{-1}$ -convex sets by  $\mathbb{B}^{-1}$ -measurable maps was studied in [3].  $\mathbb{B}^{-1}$ -convex functions were defined and examined in [4]. In this presentation, we introduce some new operations on  $\mathbb{B}^{-1}$ -convex sets and  $\mathbb{B}^{-1}$ -convex functions.

**Keywords:** Abstract convexity,  $\mathbb{B}^{-1}$ -convex sets,  $\mathbb{B}^{-1}$ -convex functions.

### References:

- [1] G. Adilov and I. Yesilce, " $\mathbb{B}^{-1}$ -convex sets and  $\mathbb{B}^{-1}$ -measurable maps", *Numerical Functional Analysis and Optimization*, 33(2)(2012), 131-141.
- [2] W. Briec, Q. B. Liang, "On Some Semilattice Structures for Production Technologies", *European Journal of Operational Research*, 215(2011), 740-749.
- [3] G. Tinaztepe, I. Yesilce and G. Adilov, "Separation of  $\mathbb{B}^{-1}$ -convex Sets by  $\mathbb{B}^{-1}$ -measurable Maps", *Journal of Convex Analysis*, 21(2)(2014), 571-580.
- [4] G. Adilov and I. Yesilce, " $\mathbb{B}^{-1}$ -convex functions", *Journal of Convex Analysis*, 24(2)(2017).



## SOME SPECIAL NUMBERS AND POLYNOMIALS RELATED TO K-ARY LYNDON WORDS

Irem KUCUKOGLU<sup>1</sup>, Yilmaz SIMSEK<sup>2</sup>

<sup>1,2</sup>*Department of Mathematics, Faculty of Science, University of Akdeniz,  
Antalya/TURKEY*

<sup>1</sup>[ikucukoglu@akdeniz.edu.tr](mailto:ikucukoglu@akdeniz.edu.tr)

<sup>2</sup>[ysimsek@akdeniz.edu.tr](mailto:ysimsek@akdeniz.edu.tr)

**Abstract:** The aim of this talk is to investigate  $k$ -ary Lyndon words of length prime and their generating functions. Firstly, we survey and investigate not only these numbers related arithmetical functions, Mobius inversion formula, Necklace polynomials, but also de Bruijn sequences and graphs. Finally, we give relations between the numbers of  $k$ -ary Lyndon words of length prime and many numbers such as the Bernoulli numbers, the Euler numbers and the Frobenius-Euler numbers.

**Keywords:** Lyndon words, Necklace polynomials, De Bruijn sequences, Generating functions, Special numbers, Special polynomials, Arithmetical functions, Mobius inversion formula.

### References:

- [1] H. Ozden, Y. Simsek, "Modification And Unification Of The Apostol-Type Numbers And Polynomials And Their Applications", *Appl. Math. Comput.***235** (2014), pp.338-351.
- [2] I. Kucukoglu, Y. Simsek, "On  $k$ -ary Lyndon Words And Their Generating Functions", to appear in AIP Conf. Proc. of ICNAAM(2016)
- [3] N. G. de Bruijn, "A Combinatorial Problem", *Nederl. Akad. Wetensch. Proc.***49** (1946) 758-764.
- [4] R. Lyndon, "On Burnside problem I", *Trans. American Math. Soc.***77**(1954), 202-215.
- [5] R. Sivaramakrishnan, "*Classical Theory of Arithmetic Functions*", Marcel Dekker, Inc., (New York-Basel), 1989.
- [6] T. van Aardenne-Ehrenfest and N. G. de Bruijn, "Circuits and trees in oriented linear graphs", *Simon Stevin* **28** (1951), 203-217.

## A NEW ITERATION SCHEME FOR A HYBRID PAIR OF NONEXPANSIVE MAPPINGS

Izhar UDDIN

*Department of Mathematics, Jamia Millia Islamia,*

*New Delhi/INDIA*

[izharuddin1@jmi.ac.in](mailto:izharuddin1@jmi.ac.in)

**Abstract:** In this paper, we construct an iteration scheme involving a hybrid pair of nonexpansive mappings and utilize the same to prove some convergence theorems. In process, we remove a restricted condition (called end-point condition) in Sokhuma and Kaewkhao's results [Sokhuma and Kaewkhao, Fixed Point Theory Appl. 2010, Art. ID 618767, 9 pp.].

**Keywords:** Banach space, convergence theorems, fixed point.

### References:

- [1] K. Sokhuma and A. Kaewkhao, Ishikawa iterative process for a pair of single-valued and multivalued nonexpansive mappings in Banach spaces, Fixed Point Theory Appl. Art. ID 618767 (2010).
- [2] N. Shahzad and H. Zegeye, On Mann and Ishikawa iteration schemes for multi-valued maps in Banach spaces, Nonlinear Anal. 71, (2009), 838-844.
- [3] Izhar Uddin, M. Imdad and Javid Ali, Convergence theorems for a hybrid pair of generalized nonexpansive mappings in Banach spaces, Bull. Malays. Math. Sci. Soc., 38, (2015), 695–705.

## TAUBERIAN THEOREMS FOR WEIGHTED MEANS OF DOUBLE SEQUENCES OF FUZZY NUMBERS

Ümit TOTUR<sup>1</sup>, İbrahim ÇANAK<sup>2</sup>

<sup>1</sup>*Department of Mathematics, Adnan Menderes University,  
Aydın/TURKEY*

[utotur@adu.edu.tr](mailto:utotur@adu.edu.tr)

<sup>2</sup>*Department of Mathematics, Ege University, İzmir/TURKEY*

[ibrahim.canak@ege.edu.tr](mailto:ibrahim.canak@ege.edu.tr)

**Abstract:** In this paper, we give necessary and sufficient Tauberian conditions under which convergence in Pringsheim's sense of a double sequence of fuzzy numbers follows from convergence of weighted means  $(N,p,q)$ . These conditions are weaker than the two-dimensional analogues of Landau's condition and Schmidt's slow oscillation condition.

**Keywords:** Fuzzy numbers, double sequences, slow oscillation,  $(N,p,q)$  summability, Tauberian theorems.

### References:

- [1] C.-P. Chen, J. Hsu, "Tauberian theorems for weighted means of double sequences", *Analysis Mathematica*, 26(2000), 243-262.
- [2] F. Moricz, "Tauberian theorems for Cesaro summable double sequences", *Studia Mathematica*, 110(1994), 83-96.
- [3] U. Stadtmüller, "Tauberian theorems for weighted means of double sequences", *Analysis Mathematica*, 25(1999), 57-68.
- [4] F. Moricz, U. Stadtmüller, "Summability of double sequences by weighted mean methods and Tauberian conditions for convergence in Pringsheim's sense", *International Journal of Mathematics and Mathematical Sciences*, 65(2004), 3499-3511.

## SPECTRAL SINGULARITIES OF THE IMPULSIVE STURM LIOUVILLE OPERATORS ON THE SEMI AXIS

İbrahim ERDAL<sup>1</sup>, Şeyhmus YARDIMCI<sup>2</sup>

<sup>1</sup>*Department of Mathematics, Ankara University,  
Ankara/TURKEY*

[ierdal@ankara.edu.tr](mailto:ierdal@ankara.edu.tr)

<sup>2</sup>*Department of Mathematics, Ankara University, Ankara/TURKEY*

[Seyhmus.Yardimci@ankara.edu.tr](mailto:Seyhmus.Yardimci@ankara.edu.tr)

**Abstract:** We consider the second order differential equation

$$(1) \quad -y'' = \lambda^2 \rho(x)y, \quad x \in [0, \infty) \setminus \{1\}$$

with boundary condition

$$(2) \quad y(0) = 0$$

and impulsive condition

$$(3) \quad \begin{bmatrix} y_+(1) \\ y'_+(1) \end{bmatrix} = \begin{bmatrix} a & b \\ c & d \end{bmatrix} \begin{bmatrix} y_-(1) \\ y'_-(1) \end{bmatrix}$$

where  $a, b, c, d$  are complex numbers,

$$\rho(x) = \begin{cases} \gamma^2 & \text{if } 0 \leq x < 1 \\ 1 & \text{if } 1 < x < \infty \end{cases}, \quad \gamma > 1$$

and  $\lambda$  is a spectral parameter. Let  $L$  denote the operator generated by (1),(2) and (3) in  $L^2(0, \infty)$ . In this study, we investigate eigenvalues and spectral singularities of  $L$  depending on the choice of coupling constants  $a, b, c, d$ .

**Keywords:** Sturm Liouville operators, spectral singularity, impulsive condition.

### References:

- [1] A. Mostafazadeh, "Spectral Singularities of a general point interaction", J. Phys. A: Math. Theory, 44(2011), 375302(9pp.).
- [2] G. Sh. Guseinov, "On the concept of spectral singularities", Pramana J. of Phys., 73(2009), 587-603.
- [3] A.M. Krall, E. Bairamov, Ö. Çakar, "Spectrum and spectral singularities of a quadratic pencil of a Schrödinger operator with a general boundary condition", J Diff. Equations, 151(1999), 252-267.

## NORM INEQUALITIES FOR A PARTICULAR CLASS OF MATRICES

<sup>1</sup>İbrahim Halil GÜMÜŞ, <sup>2</sup>Omar HİRZALLAH, <sup>3</sup>Fuad KİTTANEH

<sup>1</sup>*Department of Mathematics, Faculty of Arts and Sciences, Adiyaman University,  
Adiyaman/TURKEY*

[igumus@adiyaman.edu.tr](mailto:igumus@adiyaman.edu.tr)

<sup>2</sup>*Department of Mathematics, Hashemite University, Zarqa/JORDAN*

[o.hirzal@hu.edu.jo](mailto:o.hirzal@hu.edu.jo)

<sup>3</sup>*Department of Mathematics, The University of Jordan, Amman/JORDAN*

[fkitt@ju.edu.jo](mailto:fkitt@ju.edu.jo)

**Abstract:** In this talk, we discuss some norm inequalities for accretive dissipative  $2 \times 2$  block matrices. More precisely, we prove Schatten  $p$ -norm inequalities for this particular class of matrices. Our results generalize and improve some earlier results.

**Keywords:** Accretive-dissipative matrix, Schatten  $p$ -norm, Inequality.

### References:

- [1] A. George and Kh. D. Ikramov, On the properties of accretive-dissipative matrices, *Math. Notes* 77 (2005), 767-776.
- [2] M. Lin and D. Zhou, Norm inequalities for accretive-dissipative operator matrices, *J. Math. Anal. Appl.*, 407 (2013), 436-442.
- [3] Y. Zhang, Unitarily invariant norm inequalities for accretive dissipative operator matrices, *J. Math. Anal. Appl.*, 412 (2014), 564-569.
- [4] I. H. Gumus et al., Norm inequalities involving accretive-dissipative  $2 \times 2$  block matrices, *Linear Algebra Appl.* (2016), <http://dx.doi.org/10.2016/j.laa.2016.04.015>.

## ZWEIER SUPER BANACH SPACES

İbrahim ŞANLIBABA

*Department of Mathematics, NevşehirHacıBektaşVeliUniversity,  
Nevşehir/TURKEY*

[ibrahimsanlibaba@gmail.com](mailto:ibrahimsanlibaba@gmail.com)

**Abstract:** This In this paper, we have given some definitions and theorems about super metric (or ultra metric) and super normed(or ultra normed) spaces which exists in the mathematical literature knowledge base. After, we have defined some new type super-Banach spaces which are super isomorphic to some super Banach spaces and given some interesting properties. Furthermore, some inclusions are proved about these new type super Banach.

**Keywords:** Ultra metric, ultra norm, super norm, non-Archimedean space, ultra convergent.

### References:

- [1] Altay, B. and Başar, F., Some Euler sequence spaces of non-absolute type, Ukrainian Math. J. 57 (1)(2005), 1--17.
- [2] Altay, B. and Başar, F., Some paranormed Riesz sequence spaces of non-absolute type, Southeast Asian Bull. Math. 30(5)(2006), 591--608.
- [3] Altay, B. and Başar, F., Some paranormed sequence spaces of non-absolute type derived by weighted mean, J. Math. Anal. Appl. 319(2)(2006), 494--508.
- [4] Kirişçi, M. and Başar, F., Some new sequence spaces derived by the domain of generalized difference matrix, Comput. Math. Appl. 60 (5)(2010), 1299--1309.
- [5] Şengönül, M. and Kayaduman, K., On the Riesz almost convergent sequences spaces, Abstract and Applied Analysis, 2012(2012), 691694.
- [6] Şengönül, M., On The Zweier Sequence Space, Demonstratio Mathematica, Vol:XL, No:1, 2007.

## AN OPTIMAL MULTIPLE SWITCHING PROBLEM UNDER WEAK ASSUMPTIONS

Imen HASSAIRI

<sup>1</sup>*Department of Mathematics, University of Sfax, TUNUSIE*  
imen.hassairi@yahoo.fr

**Abstract:** This work studies the problem of optimal multiple switching in finite horizon, when the switching costs functions are continuous and belong to the class D. This problem is solved by means of the Snell envelope of processes.

**Keywords:** Real options, Snell envelope, stopping time, optimal switching.

### References:

- [1] R. Carmona and M. Ludkovski, Pricing asset scheduling flexibility using optimal switching, *Appl. Math. Finance*, 15(2008), 405-447.
- [2] C. Dellacherie and P.A. Meyer, *Probabilities et Potential*, V-VIII, Hermann, Paris, 1975.
- [3] C. Dellacherie and P.A. Meyer, *Probabilities et Potential*, I-IV, Hermann, Paris, 1980.

## ROBIN BOUNDARY VALUE PROBLEM FOR THE BELTRAMI EQUATION

İlker GENÇTÜRK<sup>1</sup>, Kerim KOCA<sup>2</sup>

<sup>1</sup> Department of Mathematics, Kırıkkale University,  
Kırıkkale/TURKEY

[ilkergencturk@gmail.com](mailto:ilkergencturk@gmail.com)

<sup>2</sup> Department of Mathematics, Kırıkkale University,  
Kırıkkale/TURKEY

[kerimkoca@gmail.com](mailto:kerimkoca@gmail.com)

**Abstract:** In this work, we present a solvability condition of the Robin boundary value problem for the Beltrami equation with constant coefficients given by  $w_{\bar{z}} + cw_z = f, f \in L_p(D, \mathbb{C}) \cap C(\bar{D}, \mathbb{C}); p > 2, [w(z) + \frac{\partial w}{\partial \bar{v}}] \Big|_{\partial D} = \gamma, \gamma \in C(\bar{D}, \mathbb{C})$  on the unit disk  $D = \{z \in \mathbb{C} : |z| < 1\}$ . We also present an elementary solution using singular operator.

**Keywords:** Beltrami equation, Robin boundary value problem, singular integral operator.

### References:

- [1] G. Harutyunyan, "Boundary value problems for the Beltrami operator", *Complex Variables and Elliptic Equations: An International Journal*, 52(6)(2007), 475–484.
- [2] H. Begehr, "Boundary value problems in complex analysis I-II", *Bol. Asoc. Mat. Venezolana*, 2005, 65–85, 165–184.
- [3] H. Begehr, "Complex Analytic Methods for Partial Differential Equations An Introductory Text", World Scientific, Singapore, 1994.



## A SIMPLE APPROACH TO THE SOLUTION OF SPECIAL STRUCTURED NONHOMOGENEOUS HIGHER ORDER LINEAR DIFFERENTIAL EQUATIONS WITH CONSTANT COEFFICIENTS

İnayet DERİN<sup>1</sup>, Yakup HAMEŞ<sup>2</sup>

<sup>1</sup>*Department of Electrical and Electronics Engineering, Iskenderun Technical University, İskenderun-Hatay/TURKEY*  
[i.derin@hotmail.com](mailto:i.derin@hotmail.com)

<sup>2</sup>*Department of Electrical and Electronics Engineering, Iskenderun Technical University, İskenderun-Hatay/TURKEY*  
[yakuphames@hotmail.com](mailto:yakuphames@hotmail.com)

**Abstract:** Due to such Differential Equations is linear with Constant Coefficient; it is solved by the consecutive integral method, the undetermined coefficients method and variation of parameters method. Nevertheless, for higher order of  $n$ , the undetermined coefficients method is required solutions of multi-variable undefined linear equations system. Variations of parameters method is also required both obtaining linear equations system with many-unknowns coefficients in the form of derivative functions and integration of such unknown coefficients in the form of derivative functions in these systems.

All of these methods are include difficulties. In the present work, a simple approach to the solution of special structured nonhomogeneous higher order linear differential equations with constant coefficients is presented. The proposed method can be used directly and briefly. This method is proved with sample solutions.

**Keywords:** Higher Order Linear Differential Equations, Constant coefficient, Nonhomogeneous solution, simple approach.

### References:

- [1] J. Jia, T. Sogabe, "On particular solution of ordinary differential equations with constant coefficients", *Applied Mathematics and Computation*, 219 (2013) 6761–6767.
- [2] R. K. Nagle, E. B. Saff, A. D. Snider, "Fundamentals of Differential Equations", Pearson Education, (2012) 318–326.

## ON SOME PROPERTIES OF VECTOR-VALUED WEIGHTED VARIABLE EXPONENT SOBOLEV SPACES

İsmail AYDIN

*Department of Mathematics, Sinop University,*

*Sinop/TURKEY*

[iaudin@sinop.edu.tr](mailto:iaudin@sinop.edu.tr)

**Abstract:** In this presentation, we define vector-valued weighted variable exponent Sobolev spaces and mention some their basic properties, such as completeness, separable, reflexive and uniformly convex. Furthermore, we obtain several density theorems in this spaces. Finally, we give some results about embeddings theorems and its applications in vector-valued weighted variable exponent Sobolev spaces.

**Keywords:** Vector-valued variable exponent weighted Sobolev space, Embeddings, Density theorem.

### References:

- [1] I.Aydin, On Variable Exponent Amalgam Spaces, Analele Stiintifice Ale Universitatii Ovidius Constanta-Seria Matematica, Vol.20(3), 5-20(2012).
- [2] I.Aydin, Weighted Variable Sobolev Spaces and Capacity, Hindawi Publishing Corporation, Journal of Function Spaces and Applications, Volume 2012, Article ID 132690, 17 pages, doi: 10.1155/2012/132690
- [3] C.Cheng and J.Xu, Geometric Properties of Banach Space Valued Bochner-Lebesgue Spaces With Variable Exponent, Journal of Mathematical Inequalities, Vol.7(3), 461-475 (2013).

## EDGE OPERATIONS IN GRAPHS AND ZAGREB INDICES

Ismail Naci CANGUL<sup>1</sup>, Aysun YURTTAS<sup>2</sup>, Muge TOGAN<sup>3</sup>, Ahmet Sinan CEVIK<sup>4</sup>

<sup>1,2</sup>*Department of Mathematics, Uludag University,  
Bursa/TURKEY*

cangul@uludag.edu.tr

**Abstract:** Topologic indices, also called graph indices, are important mathematical tools which give information about the graph. The first and second Zagreb indices are two of them. They were calculated for many graph types and there are also general results on them. In this paper we study the change of these indices when an edge is deleted. Also the change of the first Zagreb index when a number of edges are deleted is calculated. These enables us to study the properties of larger graphs in terms of the properties of smaller graphs which can be calculated easily..

**Keywords:** Graph, topological index, Zagreb index, edge operations.

### References:

- [1] Ranjini, P. S., Lokesh, V., Cangul, I. N., On the Zagreb Indices of the Line Graphs of the Subdivision Graphs, Applied Mathematics and Computation, 218 (3), (2011), 699-702.
- [2] Das, K. Ch., Yurttas, A., Togan, M., Cangul, I. N., Cevik, A. S., The Multiplicative Zagreb Indices of Graph Operations, Journal of Inequalities and Applications, 90, doi:10.1186/1029-242X-2013-90, 2013, 1-14.
- [3] Togan, M., Yurttas, A., Cangul, I. N., Some formulae and I nequalities on several Zagreb indices of r-subdivision graphs, Enlightments of Pure and Applied Mathematics (EPAM), 1 (1), 2015, 29-45

## INITIAL TIME DIFFERENCE GENERALIZED MONOTONE ITERATIVE TECHNIQUE UNIFIED BY THE UPPER AND LOWER SOLUTIONS

İsmet ARSLAN<sup>1</sup>, Coşkun YAKAR<sup>2</sup>, Muhammed ÇİÇEK<sup>3</sup>

<sup>1</sup>*Department of Mathematics, Gebze Technical University,  
Kocaeli/TURKEY  
iarslan@gtu.edu.tr*

<sup>2</sup>*Department of Mathematics, Gebze Technical University,  
Kocaeli/TURKEY  
cyakar@gtu.edu.tr*

<sup>3</sup>*Department of Mathematics, Bursa Technical University,  
Bursa/TURKEY  
muhammed.cicek@btu.edu.tr*

**Abstract:** In this work, the monotone iterative methods for initial value problems have been investigated by choosing upper and lower solutions with initial time difference when the forcing function has sum of two different natural ones.

**Keywords:** Initial time difference, monotone iterative technique, existence theorems, comparison results.

### References:

- [1] Ladde, G. S, Lakshmikantham, V. and Vatsala A. S., Monotone Iterative Technique for Nonlinear Differential Equations (Pitman Publishing Inc., Boston, 1985).
- [2] Deekshitulu, Gvsr., Generalized monotone iterative technique for fractional R-L differential equations , Nonlinear Studies 16 (1), 85--94, 2009.
- [3] Sokol M., and Vatsala, A. S., A Unified Exhaustive Study of monotone iterative method for initial value problems, Nonlinear Studies 8 (4), 429-438, (2001).
- [4] Bhaskar T.G. and McRae F.A., Monotone iterative techniques for nonlinear problems involving the difference of two monotone functions, Applied Mathematics and Computation 133, 187-192, (2002)

## ON NONLINEAR BOUNDARY VALUE PROBLEM

Janpou NEE<sup>1</sup>

<sup>1</sup>*General Education Center, ChiengKuo Technology University,  
Changhua/Taiwan  
[jpnee@ctu.edu.tw](mailto:jpnee@ctu.edu.tw)*

**Abstract:** In this article, the existence and non-existence of a semi-linear elliptic equation with nonlinear boundary value problem is studied. Moreover, the uniqueness of the solution that corresponding to the boundary value and the local behavior of the solution are proved.

**Keywords:** Nonlinear boundary value problem, existence, uniqueness, local extrema, positive solution.

### References:

- [1] Gabriel T'ellez and Emmanuel Trizac, Exact asymptotic expansions for the cylindrical Poisson-Boltzmann equation, *Journal of Statistical Mechanics: Theory and Experiment*, 2006, (2006).
- [2] Dan Ben-Yaakov, D. Andelman, D. Harries, R. Podgornik, Beyond standard Poisson-Boltzmann theory: ion-specific interactions in aqueous solutions, *J. Phys.: Condens. Matter*, 21, (2009).
- [3] Paweł Grochowski, Joanna Trylska, Continuum molecular electrostatics, salt effects, and counterion binding—A review of the Poisson-Boltzmann theory and its modifications, *Biopolymers*, Vol 89, No. 2, pp. 93-113, 2008.

## UNIFIED RELATION-THEORETIC METRICAL FIXED POINT THEOREMS UNDER AN IMPLICIT CONTRACTIVE CONDITION WITH AN APPLICATION

Md. AHMADULLAH, Javid ALI, M. IMDAD

*Department of Mathematics, Aligarh Muslim University  
Aligarh 202002, India  
javid@amu.ac.in*

**Abstract:** The main purpose of this article is to establish metrical relation-theoretic fixed point theorems via an implicit contractive condition which is general enough to yield a multitude of corollaries corresponding to several well known contraction conditions (e.g. Banach (Fund. Math. 3, 133-181(1922)), Kannan (Am. Math. Mon. 76, 405-408 (1969)), Reich (Can. Math. Bull. 14, 121-124(1971)), Bianchini (Boll. Unione Mat. Ital. 5, 103-108 (1972)), Chatterjea (C. R. Acad. Bulg. Sci. 25, 727-730 (1972)), Hardy and Rogers (Can. Math. Bull. 16, 201-206 (1973)), Ciri (Proc. Am. Math. Soc. 45, 267-273 (1974)) and several others) wherein even such corollaries are new results on their own. As simple we utilize our main results, to prove a theorem on the existence and uniqueness of the solution of an integral equation besides furnishing an illustrative example.

**Keywords:** Complete metric space, binary relations, implicit relations, fixed point.

### References:

- [1] A. Alam, M. Imdad, "Relation-theoretic contraction principle", J. Fixed Point Theory Appl., 17(2015), 693-702.
- [2] J. Ali, M. Imdad, "An implicit function implies several contraction conditions", Sarajevo J. Math., 4(17)(2008), 269-285.
- [3] V. Berinde, F. Vetro, "Common fixed points of mappings satisfying implicit contractive conditions", Fixed Point Theory Appl., 2012:105.
- [4] J.J. Nieto, R.R. Lopez, "Contractive mapping theorems in partially ordered sets and application to ordinary differential equations", Order, 22(3)(2008), 223-239.

## PARAMETRIC ORDERED GENERALIZED VARIATIONAL INCLUSIONS INVOLVING NODSM MAPPINGS

Javid IQBAL<sup>1</sup>, Rais AHMAD<sup>2</sup>

<sup>1</sup>*Department of Mathematical Sciences, Baba Ghulam Shah Badshah University, Rajouri, Jammu and Kashmir, India.*  
[javid2iqbal@yahoo.co.in](mailto:javid2iqbal@yahoo.co.in)

<sup>2</sup>*Department of Mathematics, Aligarh Muslim University, Aligarh 202002, India*  
[raisain\\_123@rediffmail.com](mailto:raisain_123@rediffmail.com)

**Abstract:** In this paper, we consider  $(\beta, \frac{\lambda}{\omega})$ -NODSM set-valued mappings and we define a resolvent operator as  $J_{\omega M, \frac{\lambda}{\omega}} = [I + \frac{\lambda}{\omega}(\omega M)]^{-1}$ . We discussed some properties of the resolvent operator  $J_{\omega M, \frac{\lambda}{\omega}}$  and then applied it to solve a parametric ordered generalized variational inclusion problem in real ordered Banach spaces.

**Keywords:** Central factorial numbers, Stirling numbers, Shifting operator, Averaging operator, Combinatorial sum, Generating function.

## ON SOME RESULT OF NEW THREE-STEP ITERATION PROCESS ON THE CONVEX METRIC SPACES

Kadri DOĞAN<sup>1</sup>, Yılmaz ALTUN<sup>2</sup>

<sup>1</sup>*Department of Elementary Education, Artvin Coruh University, Artvin/TURKEY*  
[dogankadri@hotmail.com](mailto:dogankadri@hotmail.com)

<sup>2</sup>*Department of Mathematics, Yıldız Technical University, İstanbul/TURKEY*  
[altuny4787@gmail.com](mailto:altuny4787@gmail.com)

**Abstract:** In this presentation, we introduce a new three step iteration process and show that the iteration process converges to the unique fixed point of contraction mappings on the convex metric spaces. Furthermore, we obtain this iteration process is equivalent to Mann iteration method and T-stable.

**Keywords:** Fixed point iteration, strong convergence, convex metric spaces

## ON THE CONVERGENCE RESULT OF NEW THREE-STEP ITERATION PROCESS ON THE GENERALIZED BANACH SPACES

Kadri DOĞAN<sup>1</sup>, Vatan KARAKAYA<sup>2</sup>, Faik GÜRSOY<sup>3</sup>

<sup>1</sup>*Department of Elementary Education, Artvin Coruh University,  
Artvin/TURKEY*

[dogankadri@hotmail.com](mailto:dogankadri@hotmail.com)

<sup>2</sup>*Department of Mathematical Engineering, Yıldız Technical University,  
İstanbul/TURKEY*

[vkkaya@yahoo.com](mailto:vkkaya@yahoo.com)

<sup>3</sup>*Department of Mathematics, Adiyaman University, Adiyaman/TURKEY*

[faikgursoy02@hotmail.com](mailto:faikgursoy02@hotmail.com)

**Abstract:** In this presentation, we introduce a new three step iteration process and show that the iteration process strongly converges to the unique fixed point of contraction mappings on the G- Banach spaces. Furthermore, we obtain this iteration process is equivalent to Mann iteration method.

**Keywords:** Fixed point iteration, strong convergence, G-Banach spaces

## BACKWARD SOBOLEV TYPE FRACTIONAL STOCHASTIC EVOLUTION EQUATIONS IN HILBERT SPACES

Kerboua MOURAD

**Abstract.** In this paper, we examine the approximate controllability of class of semilinear fractional backward stochastic evolution equations of Sobolev type in Hilbert spaces. We use Hölder's inequality, fixed point technique, fractional calculus, stochastic analysis and methods adopted directly from deterministic control problems for the main results. A new set of sufficient conditions is formulated and proved for the fractional backward control system to be approximately controllable. An example is given to illustrate the abstract results.

**Keywords:** Approximate controllability, backward fractional Sobolev type equation, stochastic system, fixed point technique, semigroups.



## q- GREEN'S FORMULA ON THE COMPLEX PLANE IN THE SENSE OF HARMAN

Kerim KOCA<sup>1</sup>, İker GENÇTÜRK<sup>2</sup>, Mustafa AYDIN<sup>3</sup>

<sup>1</sup>Department of Mathematics, Kırıkkale University, Kırıkkale/TURKEY

[kerimkoca@gmail.com](mailto:kerimkoca@gmail.com)

<sup>2</sup>Department of Mathematics, Kırıkkale University, Kırıkkale/TURKEY

[ilkergerenturk@gmail.com](mailto:ilkergerenturk@gmail.com)

<sup>3</sup>Department of Mathematics, Kırıkkale University, Kırıkkale/TURKEY

[mustafa.aydin868@gmail.com](mailto:mustafa.aydin868@gmail.com)

**Abstract:** Consider the square discrete set

$$D = \{z_{mn} = aq^m + iaq^n = (aq^m, aq^n): 0 \leq m, n \leq \infty; m, n \in \mathbb{N}\}$$

on the complex domain  $\mathbb{C}$  where  $0 < q < 1, a \in \mathbb{R}^+ = (0, \infty)$ . The discrete boundary of  $D$  is  $\partial D = \gamma_1 \cup \gamma_2 \cup \gamma_3 \cup \gamma_4$  where

$$\gamma_1 = \{aq^n: 0 \leq n < \infty; n \in \mathbb{N}\}, \gamma_2 = \{a + iaq^n: 0 \leq n < \infty; n \in \mathbb{N}\}$$

$$\gamma_3 = \{aq^n + ia: 0 \leq n < \infty; n \in \mathbb{N}\}, \gamma_4 = \{iaq^n: 0 \leq n < \infty; n \in \mathbb{N}\}.$$

In this work, we proved the following Green's Identity in the sense of Harman

$$\int_{\gamma} (f * g)(\zeta) d_q \zeta = \frac{1-q}{q} a \sum_{m=0}^{\infty} \sum_{n=0}^{\infty} [f(z_{mn})Bg(qz_{mn}) - qg(qz_{mn})Lf(z_{mn})]$$

for the discrete functions  $f(z), g(z)$  defined on  $D$ . We also presented some corollaries of this result. Here,

$$Bg(z) = \bar{z}g(z)g(x, q^{-1}y) + iyg(q^{-1}x, y);$$

$$Lf(z) = \bar{z}f(z)g(x, qy) + iyg(qx, y)$$

for  $z = x + iy$

**Keywords:** q-derivative, line q-integrals, q-Green's Formula, q-analogue of Cauchy Integral Formula.

### References:

- [1] C.J.Harman, "Discrete Geometric Function Theory I", *Applicable Analysis*, 7(1978), 315-336.

## BERNOULLI MATRIX-COLLOCATION METHOD FOR SOLVING GENERAL FUNCTIONAL INTEGRO-DIFFERENTIAL EQUATIONS WITH HYBRID DELAYS

Kübra ERDEM BİÇER<sup>1</sup>, Mehmet SEZER<sup>2</sup>

<sup>1,2</sup>*Department of Mathematics, Celal Bayar University,  
Manisa/TURKEY*

[kubra.erdem@cbu.edu.tr](mailto:kubra.erdem@cbu.edu.tr), [mehmet.sezer@cbu.edu.tr](mailto:mehmet.sezer@cbu.edu.tr)

**Abstract:** In this presentation, we apply a matrix method based on Bernoulli polynomials and collocation points to solve integro-functional equations with hybrid delays. The main problem is reduced to a system of algebraic equations by using this method. After solving this system, we have the coefficients of the approximate solution of the given problem. The accuracy and applicability of this method is illustrated by examples by using developed error-estimation technique related to residual function.

**Keywords:** Bernoulli polynomials, Functional-differential equations, Pantograph equations, Collocation-Matrix method.

### References:

- [1] S. Yu. Reutskiy, "A new collocation method for approximate solution of the pantograph functional differential equations with proportional delay", *Applied Mathematics and Computation*, 266 (2015), 642–655.
- [2] S. Yüzbaşı, "Laguerre approach for solving pantograph-type Volterra integro-differential equations", *Applied Mathematics and Computation*, 232 (2014), 1183–1199.
- [3] M.T. Rashed, "Numerical solution of functional differential, integral and integro-differential equations", *Applied Mathematics and Computation*, 156 (2004), 485–492.
- [4] J. Biazar, M. G. Porshokouhi, B. Ghanbari, M. G. Porshokouhi, "Numerical solution of functional integral equations by the variational iteration method", *Journal of Computational and Applied Mathematics*, 235 (2011), 2581–2585.

## A NEW UNIDIMENSIONAL BISECTION METHOD FOR GLOBAL OPTIMIZATION

Lakhdar CHITER<sup>1</sup>, Abdelmalek KOUADRI<sup>2</sup>

<sup>1</sup>*Department of Mathematics, Setif University,  
19000 Setif/Algeria  
[chiter1@yahoo.fr](mailto:chiter1@yahoo.fr)*

<sup>2</sup>*Systems and signals laboratory, University of Boumerdes, Av. de  
l'indépendance, 35000, Boumerdes, Algeria  
[ab\\_kouadri@hotmail.com](mailto:ab_kouadri@hotmail.com)*

**Abstract:** In this talk, the global optimization problem of a univariate function satisfying the Lipschitz condition over an interval with an unknown Lipschitz constant is considered. In the proposed algorithm, the objective function is evaluated at two equidistant points for each generated interval. The optimization operates at both local and global levels, where bisection is used instead of trisection, consequently, more complete information about the objective function is considered than using the central-sampling strategy as used in most DIRECT-type algorithms. The performance of the new method is analyzed in terms of the most popular and widely used criteria; the number of iterations, the number of function evaluations, and the computer (CPU) time in comparison with the well known DIRECT algorithm. We show that it is possible to extend univariate algorithms for high dimension problems, this can be done in the framework of diagonal methods, but this investigation is still under way.

**Keywords:** Global optimization, Lipschitz optimization, bisection, diagonal partitions.

### References:

- [1] Jones, D. R., Perttunen, C. D., Stuckman, B. E. (1993) Lipschitzian optimization without the Lipschitz constant. *Journal of Optimization Theory and Application*, Vol. 79 (1), pp. 157-181.
- [2] Sergeyev, Y. D., Kvasov, D. E. (2006) Global Search Based on Efficient Diagonal Partitions and a Set of Lipschitz Constants. *SIAM Journal on Optimization*, Vol. 16(3), pp. 910-937.
- [3] Kvasov, D. E., Sergeyev, Y. D. (2012), Lipschitz gradients for global optimization in a one-point based partitioning scheme, *Journal of Computational and Applied Mathematics*, 236 pp. 4042–4054.

## COMPACTNESS OF MAXIMAL OPERATOR IN WEIGHTED LEBESGUE SPACES WITH VARIABLE EXPONENT

<sup>1</sup>Lutfi AKIN, <sup>2</sup>Yusuf ZEREN

<sup>1</sup>Mardin Artuklu University, Faculty of Economics and Administrative Sciences  
Department of Business Administration

Email: [lutfiakin@artuklu.edu.tr](mailto:lutfiakin@artuklu.edu.tr)

<sup>2</sup>Yildiz Technical University, Science Faculty, Department of Mathematic

Email: [yzeren@yildiz.edu.tr](mailto:yzeren@yildiz.edu.tr)

**Abstract:**  $\rho : (0, l) \rightarrow (1, \infty)$  measurable function,  $L^{\rho(x)}(0, l)$  ;  
 $f : (0, l) \rightarrow R$  measurable functions class.  $f$  is positive functions  
 $I = (a, b)$  ,  $L^p(a, b, w) = L^p(w)$  weighted Lebesgue space norm is

$$\|f\|_{p,w} = \left( \int_a^b |f(x)|^p w(x) dx \right)^{1/p} < \infty, \quad 0 < p < \infty. \quad f : (0, l) \rightarrow R$$

measurable functions, so that  $\limsup_{x \rightarrow 0} |f(x) - f(0)| \ln \frac{1}{W(x)} < \infty$ .

**Theorem:** Let  $p, q \in \Lambda_0 \cap \pi$  and  $f(x) \geq 0$  measurable functions  
with  $p^- > 1$  ,

$q(0) \geq p(0) > 1$ . If there are conditions

$$\limsup_{t \rightarrow 0} V(t)^{1/q(0)} W(t)^{1/p'(0)} = 0 \quad \text{and} \quad \sup_{t \in (0, \infty)} V(t)^{1/q(0)} W(t)^{1/p'(0)} < \infty.$$

Then from  $L^{\rho(\cdot)}(0, l)$  to  $L^{q(\cdot)}(0, l)$ ,

$$Mf(x) = \sup_{r>0} \frac{1}{|B(x,r)|} \int_{\bar{B}(x,r)} f(y) dy \text{ maximal operator is compact.}$$

**Keywords:** Maximal operator, variable exponent, weighted functions,  
Lebesgue space.

### References:

- [1] Mamedov, F.I. and Zeren, Y., (2011).” On a two-weighted estimation of maximal operator in the Lebesgue space with variable exponent”, Ann.Mat.Pura Appl. (4) 190, No:2, 263–275.

## FIXED POINT THEOREMS FOR INTEGRAL TYPE MAPPINGS IN BANACH SPACE

M. Abdussamed MALDAR<sup>1</sup>, Vatan KARAKAYA<sup>2</sup>

<sup>1</sup>*Department of Mathematics, Aksaray University,  
Aksaray/TURKEY*

[mmaldar@aksaray.com](mailto:mmaldar@aksaray.com)

<sup>2</sup>*Department of Mathematical Engineering, Yıldız Technical University,  
İstanbul/TURKEY*

[vkkaya@yahoo.com](mailto:vkkaya@yahoo.com)

**Abstract:** In this presentation, we introduce a new mapping called Reich integral type. We prove existence of fixed points for mapping defined on Banach spaces satisfying the Reich integral type condition. Also, we prove that Picard-Mann hybrid iteration process converges to unique fixed point of this mappings. Furthermore, we show that Picard-Mann hybrid iteration process is equivalent to Mann iteration method. Finally, we give a stability result for Reich integral type mapping by using Picard-Mann hybrid iteration process.

**Keywords:** Strong convergence, integral type mappings, stability

### References:

- [1] Akewe, H., Okeke A. G., "Stability results for multistep iteration satisfying a general contractive condition of integral type in a normed linear spaces", *Abstract and Applied Analysis*, 12 pages, 2014.
- [2] Berinde, V., "On the stability of some fixed point procedures", *Bul. Ştiinţ. Univ. Baia Mare, Ser. B, Matematica-Informatica*, 18, No:1(2002), 7-14.
- [3] Branciari, A., "A fixed point theorem for mappings satisfying a general contractive condition of integral type", *Int. J. Math. Math. Sci.*, no 9, 2002, 521-536.
- [4] Doğan, K., Karakaya V., "On the convergence and stability results for a new general iterative process", *Scientific world journal*, 8 (2014).
- [5] Harder, A.M. ve Hicks, T.L., "Stability results for fixed point iteration procedures", *Math. Japon*, (1988), 693-706
- [6] Khan, SH: "A Picard-Mann hybrid iterative process." *Fixed Point Theory and Appl.*, (2013).
- [7] Mann, W.R. "Mean value methods in iteration, *Proceedings of the American Mathematical Society*", Vol. 4, No. 3(1953).
- [8] Olatinwo, M. O., "Some stability results for Picard and Mann iteration processes using contractive condition of integral type", *creative Math. and inf.*, 19(2010).

## STATISTICALLY CONVERGENCE OF SEQUENCES OF FUZZY NUMBERS BY A MODULUS FUNCTION

Mahmut IŞIK

Faculty of Education, Harran University,

Şanlıurfa/TURKEY

[misik63@yahoo.com](mailto:misik63@yahoo.com)

**Abstract:** In this study, we generalize the concept of  $\Delta$ -statistical convergence defined by a modulus function of sequences of fuzzy numbers using the sequence  $\theta = (k_r)$  and give some inclusion relations.

**Keywords:** Statistical Convergence, Lacunary Sequence, Fuzzy Numbers.

### References:

- [1] Altınok, H and Colak, R. "Almost lacunary statistical and strongly almost lacunary convergence of generalized difference sequences of fuzzy numbers", *The Journal of Fuzzy Mathematics*, 17(4) (2009), 951–967.
- [2] Mursaleen, M and Basarir, M. "On some new sequence spaces of fuzzy numbers", *Indian Journal of Pure and Applied Mathematics*, 34(9) (2003), 1351–1357.
- [3] Nanda, S. "On sequences of fuzzy numbers", *Fuzzy Sets and Systems*, 33 (1989), 123-126.
- [4] Ü, Çakan, and Altin, Y. "Some classes of statistically convergent sequences of fuzzy numbers generated by a modulus function", *Iranian Journal of Fuzzy Systems*. 12 (2015), no. 3, 47—55.
- [5] Fast, H. "Sur la convergence statistique", *Colloquium Mathematicum*, 2 (1951), 241–244.

## ON SOME INVARIANT SEQUENCE SPACES

Mahmut KARAKUŞ

<sup>1</sup>Department of Mathematics, YüzüncüYıl University,  
Van/TURKEY

[matfonks@gmail.com](mailto:matfonks@gmail.com), [mkarakus@yyu.edu.tr](mailto:mkarakus@yyu.edu.tr)

**Abstract:** Invariant sequence spaces are much important in topological sequence spaces theory. Especially, it is very helpful for investigations of the duality of sequence spaces. For instance, if the sequence space  $X$  satisfies the condition  $l_{\infty}.X = X$  then its  $\alpha$ -,  $\beta$ - and  $\gamma$ - duals are same [4]. Garling [2] investigated  $B$ - and  $B_0$ -invariant sequence spaces and Buntinas [3] introduced and investigated  $q$ - and  $q_0$ - invariant sequence spaces and recently, Grosse- Erdmann [1] studied on  $l_1$  invariant sequence spaces. In this study, we introduce and investigate  $q_0^r$ -invariant sequence spaces, that is, sequence spaces  $X$  with  $q_0^r.X = X$ .

**Keywords:**  $FK$ -sequence spaces, Köthe-Toeplitz duals,  $AK$ -,  $AB$ -,  $\sigma B$ - and  $\sigma K$ - properties of a sequence.

### References:

- [1] K.-G. Grosse-Erdmann, "On  $l_1$  invariant sequence spaces", J. Math. Anal. Appl., 262(2001), 112-132.
- [2] D. J. H. Garling, "On topological sequence spaces", Proc. Camb. Philos. Soc., **63**(115)(1967), 997-1019.
- [3] M. Buntinas, "Convergent and bounded Cesàro sections in  $FK$ -spaces", Math. Z., 121(1971), 191-200.
- [4] J. Boos, "Classical and modern methods in summability", Oxford university press, New York (2000), 600.

## ON SOLIDNESS OF SEQUENCE SPACES

Mahmut KARAKUŞ

Department of Mathematics, Yüzüncü Yıl University,  
Van/TURKEY

[matfonks@gmail.com](mailto:matfonks@gmail.com), [mkarakus@yyu.edu.tr](mailto:mkarakus@yyu.edu.tr)

**Abstract:** An  $FK$ - sequence space  $X$  is said to be solid if the condition  $I_{\infty} \cdot X = X$  holds. This property plays a prominent role within the theory of sequence spaces. Goes proved that if  $X$  is a solid  $FK$ - space then it has  $FAK$ - property [1]. Sember defined  $UAB$ - and  $UFAK$ - properties which are same in a  $K$ - space  $X$ , and he showed that every sequence in a solid  $FK$ - space has  $UFAK$ - property [2]. In this study, we investigate solidness of  $FK$ - sequence spaces.

**Keywords:**  $FK$ - spaces, solid spaces, Köthe-Toeplitz duals,  $UFAK$ - and  $UAB$ - properties of a sequence.

### References:

- [1] G. Goes, "Summen von  $FK$ - Räumen, funktionale abschnittskonvergenz und umkehrsätze", Tohoku Math. J., 26(1974), 487-504.
- [2] J. J. Sember, "On unconditional section boundedness in sequence spaces", Rocky Mount. J. Math., 7(4)(1977), 699-706.
- [3] J. Boos, "Classical and modern methods in summability", Oxford university press, New York (2000), 600.



## THREE-STEP ITERATIVE SCHEME FOR APPROXIMATING FIXEDPOINTS OF MULTIVALUED NONEXPANSIVE MAPPINGS

Makbule KAPLAN

*Faculty of Education, Sinop University,  
SINOPTURKEY*

mkaplan@sinop.edu.tr

**Abstract:** In this presentation, we introduce a new three-step iterative scheme to approximate a common fixed point of multivalued nonexpansive mappings in a uniformly convex real Banach space and establish strong and weak convergence theorems for the proposed process. Our results extend important results.

**Keywords:** Three step iterative scheme, multivalued mappings, strong and weak convergence.

### References:

- [1] S. H. Khan, J.K. Kim, 'Common fixed points of two nonexpansive mappings by a modified faster iteration scheme', Bull Korean Math Soc. 47, 5, 973-985, 2010.
- [2] M. Kaplan, A. Kopuzlu, A., Three-step iterative scheme for approximating fixed points of multivalued nonexpansive mappings, Advances in Fixed Point Theory, 3, 2, 273-285, 2013.
- [3] J.S. Jung, 'Strong convergence theorems for multivalued nonexpansive mappings in Banach spaces', Nonlinear Anal. 66, 2345-2354, 2007.
- [4] B. Panyanak, 'Mann and Ishikawa iterative processes for multivalued mappings in Banach spaces', Comp. Math. Appl. 54, 872-877, 2007.
- [5] K.P.R. Sastry, G.V.R. Babu, 'Convergence of Ishikawa iterates for a multivalued mapping with a fixed point', Czechoslovak Math. J. 55, 817-826, 2005.
- [6] M. Abbas, S.H. Khan, A.R. Khan, R.P. Agarwal, 'Common fixed points of two multivalued nonexpansive mappings by one-step iterative scheme', Applied Mathematics letters 24, 97-102, 2001.

## INVERSE SPECTRAL AND INVERSE NODAL PROBLEMS FOR STRUM-LIOUVILLE EQUATIONS WITH POINT $\delta'$ - INTERACTION

Manaf MANAFOV

*Department of Mathematics, Adiyaman University,  
Adiyaman/TURKEY  
[mmanafov@adiyaman.edu.tr](mailto:mmanafov@adiyaman.edu.tr)*

**Abstract:** We study inverse spectral and inverse nodal problems for Strum-Liouville equations with point  $\delta'$ -interaction a finite interval. Inverse spectral problems consist in recovering operators from their spectral characteristics. Such problems play an important role in mathematics and have many applications in natural sciences (see, for example, monographs [1,3,5]). Inverse nodal problems consist in constructing operators from the given nodes (zeros) of eigenfunctions (see [2,4,6]). In this study, uniqueness results are proved, and using the nodal set of eigenfunctions the given problem reconstructed.

**Keywords:** Strum-Liouville Equations, Inverse spectral and Inverse Nodal Problems, Point  $\delta'$  -Interaction.

### References:

- [1] G. Frelling, V. A. Yurko, "Inverse Strum-Liouville Problems and Their Applications", NOVA Science PUBL., New York, 2001.
- [2] C. K. Law, C. F. Yang, "Reconstructing the potential function and its derivatives using nodal data", *Inverse Problems* (4/2) (1998), 299-312.
- [3] B. M. Levitan, "Inverse Strum-Liouville Problems", VNU Science Press, Utrecht, 1987.
- [4] M. Dzh. Manafov, A. Kablan, "Inverse spectral and inverse nodal problems for energy-dependent Strum-Liouville Equations with  $\delta$ -interaction", *Elect. J. of Diff. Equations*, vol.2015(2015), No.26, 1-10.
- [5] V. A. Marchenko, "Strum-Liouville Operators and Their Applications", *Operator Theory: Advanced and Application*, Birkhauser: Basel, 22, 1986.
- [6] C.-T. Shieh, V. A. Yurko, "Inverse nodal and inverse spectral problems for discontinuous boundary value problems", *J. Math. Anal., Appl.*, 347 (2008), 266-272.

## LOG-CONVEXITY OF WEIGHTED AREA INTEGRAL MEANS OF MONOMIALS ON THE UNIT DISK

Martin At. STANEV

*Department of Mathematics and Physics, University of Forestry,  
Sofia/BULGARIA*

[martin\\_stanev@yahoo.com](mailto:martin_stanev@yahoo.com)

**Abstract:** An open problem (see [1], p.12) about finding necessary and sufficient conditions on parameters  $a$  and  $p$  for which the weighted area integral mean of monomials is log-convex with respect to the  $\log(r)$  is solved. Here, a modification of the method developed in a series of papers [2], [3], [4], [5] is applied. Furthermore, an example of a generalized weight function is considered and it is demonstrated that in the case  $p=2$  log-convexity in  $\log(r)$  of this type of integral means does not depend on the asymptotic behavior of the weight function.

**Keywords:** logarithmic convexity, holomorphic functions, Hardy spaces, area integral means

### References:

- [1] Chunjie Wang, Kehe Zhu, Logarithmic convexity of integral means for analytic functions, *Math. Scand.* 114 (2014), 149-160, <http://arxiv.org/abs/1101.2998v1> (2011).
- [2] Chunjie Wang, Jie Xiao and Kehe Zhu, Logarithmic convexity of integral means for analytic functions II, *J. Aust. Math. Soc.* 98 (2015) 117-128, DOI: 10.1017/S1446788714000457 <http://arxiv.org/abs/1308.4881v1> (2013)
- [3] Chunjie Wang, Jie Xiao, Gaussian Integral Means of Entire Functions, *Complex Anal. Oper. Theory*, 8 (2014) 1487-1505. DOI:10.1007/s11785-013-0339-x. <http://arxiv.org/abs/1301.0349v3> (2013)
- [4] Chunjie Wang, Jie Xiao, Gaussian Integral Means of Entire Functions, *Complex Anal. Oper. Theory*, 8 (2014) 1487-1505. DOI: 10.1007/s11785-013-0339-x. <http://arxiv.org/abs/1301.0349v3> (2013)
- [5] Chunjie Wang, Jie Xiao, Gaussian Integral Means of Entire Functions: logarithmic convexity and concavity, <http://arxiv.org/abs/1405.6193v1> (2014)
- [6] C. Wang and J. Xiao: Addendum to "Gaussian integral means of entire functions", *Complex Anal. Oper. Theory* 10 (2016) 495-503. DOI 10.1007/s11785-015-0447-x. 117-128, DOI: 10.1017/S1446788714000457

## POROSITY LIMIT AND CLUSTER POINTS OF REAL VALUED SEQUENCES

Maya ALTINOK<sup>1</sup>, Mehmet KÜÇÜKASLAN<sup>2</sup>

<sup>1</sup>*Department of Mathematics, Mersin University,  
Mersin/TURKEY*

[mayaaltinok@mersin.edu.tr](mailto:mayaaltinok@mersin.edu.tr)

<sup>2</sup>*Department of Mathematics, Mersin University,  
Mersin/TURKEY*

[mkkaslan@gmail.com](mailto:mkkaslan@gmail.com)

**Abstract:** In this talk, we shall define notions of porosity-limit and porosity-cluster point of real valued sequences. These two notions, are not equivalent and they are compared with the usual limit point of sequences. Then, we give some theorems about the sets of porosity limit and porosity cluster points of real valued sequences. Also we will show that, if the set  $\mathbb{N} \setminus M$  is porous, where  $M = \{k \in \mathbb{N} : x_k \leq x_{k+1}\}$ , and  $x$  is bounded on  $M$ , then  $x$  is a porosity convergent sequence.

**Keywords:** Local upper porosity, porosity of subsets of natural numbers, porosity convergence, porosity limit points, porosity cluster points.

### References:

- [1] M. Altınok, O. Dövgöshey, M. Küçükökaslan, "Local one-sided porosity and pretangentspaces", *Analysis*, DOI: 10.1515/anly-2015-0011, September 2015.
- [2] M. Altınok, M. Küçükökaslan, "On porosity-convergence of real valued sequences", (To Appear).
- [3] B. S. Thomson, "Real functions", *Lecture Notes in Mathematics*, 1170, Springer-Verlag, Berlin, Heidelberg, New York, Tokyo, 1985.

## RELATION-THEORETIC METRICAL FIXED POINT THEOREMS UNDER NONLINEAR CONTRACTIONS

Md AHMADULLAH, Mohammad IMDAD, Rqeeb GUBRAN

*Department of Mathematics, Aliragh Muslim University,  
Aligarh/INDIA*

[ahmadullah2201@gmail.com](mailto:ahmadullah2201@gmail.com)

[mhimdad@gmail.com](mailto:mhimdad@gmail.com)

[rqeeb@gmail.com](mailto:rqeeb@gmail.com)

**Abstract:** We establish fixed point theorems for nonlinear contractions on a metric space (not essentially complete) endowed with an arbitrary binary relation. Our results extend, generalize, modify and unify several familiar results especially those contained in Samet and Turinici [Commun. Math. Anal. 13, 82-97 (2012)] and Alam and Imdad [J. Fixed Point Theory Appl. 17(4), 693-702 (2015)]. Interestingly a corollary to one of our main results proved under symmetric relation which remains a sharpened version of a theorem due to Samet and Turinici. Finally, we use examples to highlight the realized improvements in the present paper.

**Keywords:** Complete metric spaces; binary relations; contraction mappings; fixed point.

### References:

- [1] M. Ahmadullah, J. Ali, M. Imdad: Unified relation-theoretic metrical fixed point theorems under an implicit contractive condition with an application, Fixed Point Theory Appl. 2016:42, 1-15 (2016).
- [2] A. Alam and M. Imdad: Relation-theoretic contraction principle, J. Fixed Point Theory Appl. 17(4), 693-702 (2015).
- [3] A. Alam, and M. Imdad: Relation-theoretic metrical coincidence theorems, arXiv: 1603.09159 (2016).
- [4] S. Banach: Sur les operations dans les ensembles abstraits et leur application aux equations integrales, Fund. Math. 3, 133-181 (1922).
- [5] H. Ben-El-Mechaiekh: The Ran-Reurings fixed point theorem without partial order: A simple proof, J. Fixed Point Theory Appl. 16, 373-383 (2015).

## STEADY-STATE SKELETON OF THE 3D POINT CLOUDS VIA QUANTUM GRAPHS

Mehmet Ali BALCI, Ömer AKGÜLLER

*Department of Mathematics, MuğlaSıtkıKoçman University,  
Muğla/TURKEY*

[mehmetalibalci@mu.edu.tr](mailto:mehmetalibalci@mu.edu.tr)

[oakguller@mu.edu.tr](mailto:oakguller@mu.edu.tr)

**Abstract:** Point Clouds are mathematical concepts that can be sourced by shape acquisition devices, such as laser range scanners, with applications in geoscience, archival arts, prosthetics medicine, manufacturing, and security. These 3D scanners provide in general raw data in the form of unorganized point clouds. With the increasing popularity and very broad applications of this source of data, it is computationally less complex and has less error possibilities to work directly with this representation, without having to go to the intermediate step of fitting a surface to it. In our study, we aim to solve one of the skeleton construction problems of geometry processing by using the so called Quantum Graphs whose edges are the solution of the initial-boundary problem of the Sobolev functions. We first obtain the vertices of the Quantum Graph by using the local Rips-Vietoris complex representation of the point cloud, and then solve the second order ODE called steady-state equation by using the Homotopy Perturbation Method respect to the initial-boundary conditions at the vertices.

**Keywords:** Quantum Graphs, Point Cloud Processing, Homotopy Perturbation Method, Rips-Vietoris Complex

### References:

- [1] Aanjaneya, M., Chazal, F., Chen, D., Glisse, M., Guibas, L.J., Morozov, D. "Metric graph reconstruction from noisy data", SoCG '11 Proceedings of the twenty-seventh annual symposium on Computational geometry, 37-46. (2011)
- [2] Berkolaiko, G., Carlson, R., Fulling, S., Kuchment, P. (Editors) Quantum Graphs and Their Applications, Contemp. Math., v. 415, American Math. Society, Providence, RI, USA. (2006).
- [3] Chambers, E.X., de Silva, V., Erickson, J., Ghrist, R., "Vietoris-Rips Complexes of Planar Point Sets", Discrete & Computational Geometry, 44(1), 75-90. (2010)

## NUMERICAL SOLUTION OF A SINGULARLY PERTURBED PROBLEM BY USING HYBRIDIZABLE DISCONTINUOUS GALERKIN METHOD

Mehmet Fatih KARAASLAN

*Department of Statistics, Yıldız Technical University,  
İstanbul/TURKEY  
[mfatih@yildiz.edu.tr](mailto:mfatih@yildiz.edu.tr)*

**Abstract:** In this work, a current numerical method called as hybridizable discontinuous Galerkin (HDG) method is presented for solving a type of singularly perturbed problem (SPP) with boundary conditions (BCs). The main feature of the HDG method is that it can be implemented in an efficient way through a hybridization procedure which reduces the globally coupled unknowns to approximations at the element boundaries. For stability of the global linear system which is constructed for SPP, it is a crucial point to choose stability parameter. It has to be suitably defined to guarantee the existence and uniqueness of the numerical solution. However, the associated matrix in the system is tridiagonal, symmetric and positive definite. Thus, HDG method is successfully implemented for ordinary or partial differential equations. From this point of view, HDG approximation of the SPP with boundary layer is examined on some examples for  $L^2$ -norm.

**Keywords:** Hybridizable discontinuous Galerkin method, singularly perturbed problem, hybridization, stability parameter

### References:

- [1] F. Çeliker, B. Cockburn, K. Shi, "Hybridizable Discontinuous Galerkin Methods for Timoshenko Beams", *J.Sci. Comput.*, 44(2014), 1-37.
- [2] B. Cockburn, J. Gopalakrishnan, R. Lazarov, "Unified hybridization of discontinuous galerkin, Mixed, and continuous galerkin methods for second Order elliptic problems", *SIAM J.Numer. Anal.*, 47(2)(2009), 1319–1365.
- [3] J.J. Miller, E. O'Riordan, G.I. Shishkin, "Fitted numerical methods for singular perturbation problems: error estimates in the maximum norm for linear problems in one and two dimensions", World Scientific, (1996).

## THE DYNAMICS OF POSITIVE SOLUTIONS OF A HIGHER ORDER DIFFERENCE EQUATION WITH ARBITRARY POWERS AND DELAYS

Mehmet GÜMÜŞ<sup>1</sup>, Yüksel SOYKAN<sup>2</sup>

<sup>1</sup>*Department of Mathematics, Bülent Ecevit University, Zonguldak/TURKEY  
m.gumus@beun.edu.tr*

<sup>2</sup>*Department of Mathematics, Bülent Ecevit University, Zonguldak/TURKEY  
[yuksel\\_soykan@hotmail.com](mailto:yuksel_soykan@hotmail.com)*

**Abstract:** The purpose of this talk is to investigate the local asymptotic stability of equilibria, the periodic nature of solutions, the existence of unbounded solutions and the global behavior of solutions of the nonlinear difference equation

$$x_{n+1} = \frac{\alpha x_{n-(k+1)}}{\beta + \gamma x_{n-k}^p x_{n-(k+2)}^q}, n = 0, 1, \dots$$

where the parameters  $\alpha, \beta, \gamma, p, q$  are non-negative numbers and the initial values  $x_{-(k+2)}, x_{-(k+1)}, \dots, x_{-1}, x_0$  are arbitrary positive numbers.

**Keywords:** Equilibria, global stability, periodicity, oscillation, solution.

### References:

- [1] V. Kocić, G. Ladas, "Global behavior of nonlinear difference equations of higher order with applications", Kluwer Academic Publishers, Dordrecht, (1993).
- [2] M. R. S. Kulenović, G. Ladas, "Dynamics of second order rational difference equations", Chapman & Hall/CRC, (2001).
- [3] E. M. Elsayed, "New method to obtain periodic solutions of period two and three of a rational difference equation", Nonlinear Dynamics, 79(2014), 241-250.
- [4] O. Ocalan, Global dynamics of a non-autonomous rational difference equation, J. Appl. Math. & Informatics, 32(5-6) (2014), 843-848.



## NUMERICAL SOLUTION OF NONLINEAR FRACTIONAL- INTEGRO DIFFERENTIAL EQUATIONS AND SYSTEMS

Mehmet ŞENOL

*Department of Mathematics, NevşehirHacıBektaşVeli University,  
Nevşehir/TURKEY*

[msenol@nevsehir.edu.tr](mailto:msenol@nevsehir.edu.tr)

**Abstract:** In this presentation, a numerical method, namely perturbation-iteration algorithm (shortly PIA), have been employed to give approximate solutions of some nonlinear fractional-integro differential equations (FIDEs) and systems. Comparing with the exact solutions and some other method solutions, we prove that the PIA produces reliable and accurate results for FIDEs. We also give some tables and figures to illustrate our results.

**Keywords:** Fractional-integro differential equations, Caputo fractional derivative, Initial value problems, Perturbation-Iteration Algorithm.

### References:

- [1] I. Podlubny, "Fractional differential equations: an introduction to fractional derivatives, fractional differential, to methods of their solution and some of their applications", Academic press, (1998).
- [2] Y. Aksoy, M. Pakdemirli, "New perturbation–iteration solutions for Bratu-type equations", *Computers & Mathematics with Applications*, 59 (2010): 2802-2808.
- [3] M. Şenol, İ.T. Dolapci, Y. Aksoy, M. Pakdemirli, "Perturbation-Iteration Method for First-Order Differential Equations and Systems", *Abstract and Applied Analysis*, (2013).
- [4] İ.T. Dolapci, M. Şenol, M. Pakdemirli, "New perturbation iteration solutions for Fredholm and Volterra integral equations", *Journal of Applied Mathematics*, (2013).
- [5] M. Şenol, İ.T. Dolapci, "On the Perturbation–Iteration Algorithm for fractional differential equations", *Journal of King Saud University-Science* 28.1 (2016): 69-74.

## FIXED POINTS FOR SOME MULTIVALUED MAPPING IN $G_p$ – METRIC SPACES

Melek Kübra AYHAN<sup>1</sup>, Cafer AYDIN<sup>2</sup>

<sup>1</sup>Sütçü İmam University, Institute of Science and Technology, Department of Mathematics,  
Kahramanmaraş / TURKEY

E-mail: [melekkubra.ayhan@gmail.com](mailto:melekkubra.ayhan@gmail.com)

<sup>2</sup>Sütçü İmam University, Faculty of Science and Arts, Department of Mathematics, Kahramanmaraş / TURKEY

E-mail: [caydin61@gmail.com](mailto:caydin61@gmail.com)

**Abstract:** In [4], Banach defined a theorem about existence and uniqueness of fixed point. Also in [3], W. Takahashi studied fixed point on multivalued mapping in metric space. In this work, we carried this contractions to  $G_p$  metric spaces which are new generalized metric spaces, by means of multivalued mappings. Firstly, we implement

Banach contraction such that for all  $x, y, z \in X, H_{G_p}(Tx, Ty, Tz) \leq \alpha G_p(x, y, z)$  where  $\alpha \in (0, 1)$ . Other one, we apply for Takahashi contractive, such that for all

$$x, y, z \in X, H_{G_p}(Tx, Ty, Tz) \leq k(G_p(x, y, z)) \cdot G_p(x, y, z)$$

where  $k$  is a function of  $(0, \infty)$  to  $[0, 1)$  such that  $\lim_{r \in t^+} k(r) < 1$  for every  $t \in [0, \infty)$ . Thus, we proved that existence of fixed point in  $G_p$  metric spaces with multivalued mapping using these contractions.

**Keywords:** Fixed point, Multivalued mapping,  $G_p$  metric space

### References:

- [1] I. Podlubny, "Fractional differential equations: an introduction to fractional derivatives, fractional differential, to methods of their solution and some of their applications", Academic press, (1998).
- [2] Aydi H, Abbas M, Vetro C, Partial Hausdorff metric and Nadler's fixed point theorem on partial metric spaces. Topol. Appl. 159, 3234-3242 (2012).
- [3] H. Aydi, E. Karapınar, P. Salimi, Some Fixed Point Results in GP-Metric Spaces, Journal of Applied Mathematics, Volume 2012, Article ID 891713, 16 pages.
- [4] N. Mizoguchi and W. Takahashi, Fixed point theorems for multivalued mappings on complete metric spaces, J. Math. Anal. Appl., 141, 177-188 (1989).
- [5] S. Banach, Sur les opérations dans les ensembles abstraits et leur équations intégrales, Fund. Math. J. 3 (1922) 133-181

## FIXED POINT THEOREMS FOR EXPANSIVE MAPPINGS IN $G_p$ -METRIC SPACES

Meltem KAYA<sup>1</sup>, Hasan FURKAN<sup>2</sup>

<sup>1</sup>*Department of Mathematics, KahramanmaraşSütçü İmam University,  
Kahramanmaraş/TURKEY  
[meltemkaya55@hotmail.com](mailto:meltemkaya55@hotmail.com)*

<sup>2</sup>*Department of Mathematics, KahramanmaraşSütçü İmam  
University, Kahramanmaraş/TURKEY  
[hasanfurkan@hotmail.com](mailto:hasanfurkan@hotmail.com)*

**Abstract:** In the present paper, we define the concept of expansive mapping in the context of  $G_p$ -metric spaces in a similar manner expansive mapping in metric spaces. Furthermore, we obtain some results on fixed points of expansive type mappings. Also, we prove some common fixed point results for expansive mappings by using the notion of weak compatibility in  $G_p$ -metric space. Our results generalize some comparable results in metric spaces and partial metric spaces to  $G_p$ -metric spaces. Moreover, some examples are introduced in order to support our new results.

**Keywords:** Fixed point theorems,  $G_p$ -metric space, expansive mappings, weakly compatible mappings.

**Acknowledgements:** M. Kaya has been supported by the Scientific and Technological Research Council of Turkey (TUBITAK Programme, 2211-A).

### References:

- [1] M. R. A. Zand, A. D. Nezhad, "A generalization of partial metric spaces", *J. Contemp. Appl. Math.*, 24, 86-93, (2011).
- [2] V. Parvaneh, J.R. Roshan, Z. Kadelburg, "On generalized weakly  $GP$ -contractive mappings in ordered  $GP$ -metric spaces", *Gulf J. Math.*, 1, 78-97, (2013).
- [3] S. Z. Wang, B. Y. Li, Z. M. Gao, K. Iseki, "Some fixed point theorems for expansion mappings", *Math. Japon*, 29, 631-636, (1984).
- [4] P. Z. Daffer, H. Kaneko, "On expansive mappings", *Math. Japon*, 37, 733-735, (1992).
- [5] X. Huang, C. Zhu, X. Wen, "Fixed point theorems for expanding mappings in partial metric spaces", *An. Şt. Univ. Ovidius Constanta*, 20(1), 213-224, (2012).

## SOME PROPERTIES OF GENERALIZED METRIC SPACES

Merve İLKHAN<sup>1</sup>, Emrah Evren KARA<sup>2</sup>

<sup>1</sup>*Department of Mathematics, Düzce University,  
Düzce/TURKEY*

[merveilkhan@gmail.com](mailto:merveilkhan@gmail.com)

<sup>2</sup>*Department of Mathematics, Düzce University,  
Düzce/TURKEY*

[karaeevren@gmail.com](mailto:karaeevren@gmail.com)

**Abstract:** In this presentation, we give some results in G-metric spaces and introduce the notions of G-uniformly continuity and G-Cauchy continuity. We investigate the relations between the classes of G-uniformly continuous, G-Cauchy continuous and G-continuous functions. Also we characterize G-totally bounded sets in generalized metric spaces via G-Cauchy sequences.

**Keywords:** G-metric spaces, G-convergence, G-Cauchy sequences, G-continuity.

### References:

- [1] Z. Mustafa, B. Sims, "A new approach to generalized metric spaces", *Journal of Nonlinear and Convex Analysis*, 7(2006), 289-297.
- [2] Z. Mustafa, B. Sims, "Some remarks concerning D-metric spaces", *Proceedings of the International Conferences on Fixed Point Theory and Applications, Valencia (Spain), (2003)*, 189-198.
- [3] Z. Mustafa, H. Aydi, E. Karapınar, "On common fixed points in G-metric spaces using (E.A) property", *Computers and Mathematics with Applications*, 64(2012), 1944-1956.
- [4] M. Abbas, B.E. Rhoades, "Common fixed point results for noncommuting mappings without continuity in generalized metric spaces", *Applied Mathematics and Computation*, 215(2009), 262-269.

## ON RIESZ SECTIONS IN SEQUENCE SPACES

Merve TEMİZER ERSOY<sup>1</sup>, Hasan FURKAN<sup>2</sup>, Bilal ALTAY<sup>3</sup>

<sup>1</sup>*Department of Mathematics, Kahramanmaraş Sutcu Imam University,  
Kahramanmaraş/TURKEY  
[mervetemizer@hotmail.com](mailto:mervetemizer@hotmail.com)*

<sup>2</sup>*Department of Mathematics, Kahramanmaraş Sutcu  
Imam University, Kahramanmaraş/TURKEY  
[hasanfurkan@hotmail.com](mailto:hasanfurkan@hotmail.com)*

<sup>3</sup>*Department of Primary Education, Inonu University, Malatya/TURKEY  
[bilal.altay@inonu.edu.tr](mailto:bilal.altay@inonu.edu.tr)*

**Abstract:** The theory of FK-spaces was introduced by Zeller in [1] and some properties of sectional subspaces in FK-spaces were investigated by Zeller in [2]. The notion of Cesaro sections in FK-spaces was studied in [3]. In [4], Buntinas examined Toeplitz sections in sequence spaces and characterized some properties. In this presentation, we introduce Riesz sections in sequence spaces and examine some properties of them.

**Keywords:** FK-spaces, K-spaces, Sequence spaces, AK-spaces, semi-conservative space.

**Acknowledgements:** M. TEMİZER ERSOY has been supported by the Scientific and Technological Research Council of Turkey (TUBITAK Programme, 2228-B).

### References:

- [1] K. Zeller, "Allgemeine Eigenschaften von Limitierungsverfahren", Math. Z., 53(1951), 463-487.
- [2] K. Zeller, "Abschnittskonvergenz in FK- Raumen", Math. Z., 55(1951), 55-70.
- [3] M. Buntinas, "Convergent and Bounded Cesaro Sections in FK-space", Math. Z., 121(1971), 191-200.
- [4] M. Buntinas, "On Toeplitz sections in sequence spaces", Math. Proc. Camb. Phil. Soc., 78(1975), 451-460.

## STABILITY AND CONVERGENCE ANALYSIS OF THE FINITE ELEMENT DISCRETIZATION OF THE NAVIER- STOKES TIME-FILTERING REGULARIZATION

Osman Raşit IŞIK<sup>1</sup>, Meryem ÖZBUNAR<sup>2</sup>

<sup>1</sup>*Department of Elementary Mathematics Education, Muğla Sıtkı Koçman  
University,  
Muğla/TURKEY  
[osmanrasit@mu.edu.tr](mailto:osmanrasit@mu.edu.tr)*

**Abstract:** In order to regularize the flow problems, one approach is the time relaxation method. In this study, considers a time relaxation model which consists of adding a term " $\kappa(u-\bar{u})$ " to the NSE, NSE-TLES model, to damp fluctuations exponentially in time, which is explored by Layton, Pruet and Rebholz. First, an implicit time discretization of the model is given. After then, we analyzed its stability and convergence of the algorithm. Numerical experiments for the model are presented.

**Keywords:** Time relaxation; Finite element method; Navier-Stokes equations; Time-filtering regularization.

**Acknowledgments:** This paper has been granted by the Mugla Sıtkı Koçman University Research Projects Coordination Office. Project Grant Number: 16/062 and title "Navier-Stokes Zaman Rahatlama Modelinin Euler Zaman Ayırıklaştırması ile Elde Edilen Sonlu Elemanlar Çözümü Üzerine"

### References:

- [1] P. Moin and K. Mahesh, Direct Numerical Simulation: A Tool in Turbulence Research. Annual Review in Fluid Mech., 30:539--78, 1998.
- [2] Domaradzki J.A., Modeling challenges and approaches in LES for physically complex flows, Proceedings of Euromech Colloquium, 469, Technical University Dresden, Germany, 2005, p. 84.
- [3] T.J.R. Hughes, A.A. Oberai and L. Mazzei, Large eddy simulation of turbulent channel flow by the variational multiscale method, Phys. Fluids 13 (2001) 1784--1799.
- [4] Ph. Rosenau, Extending hydrodynamics via the regularization of the Chapman--Enskog expansion, Phys. Rev. A 40 (1989) 7193.
- [5] S. Schochet and E. Tadmor, The regularized Chapman--Enskog expansion for scalar conservation laws, Arch. Ration. Mech. Anal. 119 (1992) 95.

## INVERSE NODAL PROBLEM FOR p-LAPLACIAN BESSEL EQUATION

Mesut COŞKUN<sup>1</sup>, Hikmet KEMALOĞLU<sup>2</sup>

<sup>1</sup>*Tunceli Vocational School,*

*Tunceli/TURKEY*

[mesutcoskun62@gmail.com](mailto:mesutcoskun62@gmail.com)

<sup>2</sup>*Department of Mathematics, Fırat University, Elazığ/TURKEY*

[hkoyunbakan@gmail.com](mailto:hkoyunbakan@gmail.com)

**Abstract:** In this note, we solve inverse nodal problem for Bessel type  $p$ -Laplacian problem

$$-(y^{(p-1)})' = (p-1)(\lambda - \omega(x))y^{(p-1)}, 1 \leq x \leq a$$

$$y(1) = y(a) = 0$$

on a special interval. We obtain some nodal parameters like nodal points and nodal length. In addition, we reconstructed the potential function by nodal points. Results obtained in this paper are similar to Classical Sturm-Liouville problem. However these type equations are considered with a condition defined at the origin, We solve the problem on an interval  $[1, a]$  that problem is not singular.

**Keywords:** Inverse Nodal Problem, Prüfer Substitution, Bessel Equation

### References:

- [1] Law, CK; Lian, WC and Wang, WC: Inverse nodal problem and the Ambarzumyan problem for the  $p$ -Laplacian, Proc. Roy. Soc. Edinburgh Sect. A Math., 139(6), 1261-1273 (2009)
- [2] Wang, WC; Cheng, YH and Lian, WC: Inverse nodal problems for the  $p$ -Laplacian with eigenparameter dependent boundary conditions, Math. Comput. Modelling, 54 (11-12), 2718-2724 (2011).
- [3] McLeod, JB: The distribution of the eigenvalues for the Hydrogen atom and similar cases, Proc. London Math. Soc., 3(11), 139-158 (1961).

## ON WIJSMAN ASYMPTOTICALLY DEFERRED STATISTICAL EQUIVALENT OF SEQUENCES

Mikail ET

*Department of Mathematics, Firat University 23119, Elazığ/Turkey*  
mikail68@gmail.com

**Abstract:** [3] introduced definitions for asymptotically equivalent sequences and asymptotic regular matrices. Patterson [4] extended these concepts by presenting an asymptotically statistically equivalent analogy of these definitions and natural regularity conditions for nonnegative summability matrices. In this study we introduce the concepts of Wijsmanasymptoticallydeferred statistical equivalent and Wijsmanstrong asymptotically deferred equivalent of sequences. Some relations between Wijsmanasymptotically deferred statistical equivalent and Wijsmanstrong asymptoticallydeferred equivalent of sequences are given.

**Keywords:** Wijsman Statistical Convergence, Asymptotically Statistical Equivalent, Deferred Statistical Convergence ; Deferred CesàroSummability.

### References:

- [1] Fridy, J., On statistical convergence, *Analysis* 5 (1985) 301-313.
- [2] Küçükcaslan, M. and Yılmaztürk, M. On Deferred Statistical Convergence of Sequences (Under Review).
- [3] Marouf, M. Asymptotic equivalence and summability. *Int. J. Math. Math. Sci.*, 16, (1993) 755-762.
- [4] Patterson, R. F. On asymptotically statistical equivalent sequences. *Demonstratio Math.* 36(1) (2003), 149--153.
- [5] Nuray, F. and Rhoades, B. E. 2012. Statistical convergence of sequences of sets. *Fasc. Math.* 49, 87-99.
- [6] Yılmaztürk, M. and Küçükcaslan, M. On strongly deferred Cesàrosummability and deferred statistical convergence of the sequences, *BitlisEren Univ. J. Sci. and Technol.* 3 (2011), 22-25.



## NECESSARY CONDITIONS AND SUFFICIENT CONDITIONS FOR NONEXISTENCE RESULTS TO CERTAIN EVOLUTION EQUATION

Mohamed BERBICHE

*Laboratory of Applied Mathematics, University Mohamed Khider, Po. Box 145  
Biskra (07000) Algeria  
berbichemed@yahoo.fr*

**Abstract:** This work is concerned with establishing necessary or sufficient conditions for the existence of solutions for certain nonlinear evolution equations. We shall see that the existence of solutions depends on the behavior at infinity with both initial data and the coefficient functions. The non global existence is also discussed.

**Keywords:** Fujita critical exponent, non-existence, nonlinear evolution equation.

### References:

- [1] P. Baras and R. Kersner: Local and global solvability of a class of semilinear parabolic equations. *J. Diff. Eqns*, 68 no. 2, (1987), pp. 238-252.
- [2] Fujita, H., On the blowing up of solutions of the Cauchy problem for  $u_t = \Delta u + u^{\alpha+1}$ .
- [3] Hayakawa, K., On nonexistence of global solutions of some semilinear parabolic differential equations, *Proc. Japan Acad.* 49 (1973), pp. 503-505.
- [4] S. Pohozaev and A. Tesei, Blow-up of nonnegative solutions to quasilinear parabolic inequalities. *Rend. Lincei. (9) Mat. Appl.* 11, No. 2, 99-109 (2000).
- [5] A. Samarskii, V. A. Galaktionov, S. Kurdyumov and A. Mikhailov: Blow-up in quasilinear parabolic equations, de Gruyter Expositions of Mathematics, 19. Walter de Gruyter and Co., Berlin (1995).

## ANALYTICAL SOLUTION OF A CLASS OF NONLINEAR VOLTERRA INTEGRAL EQUATIONS USING VARIATIONAL ITERATION METHOD

Mohammed S. MECHEE<sup>1</sup>, RaadM. KADUM<sup>2</sup>

<sup>1,2</sup>*Department of Mathematics, Faculty of Computer Science and Mathematics,  
KufaUniversity, Najaf/IRAQ*

<sup>1</sup>[mohammeds.abed@uokufa.edu.iq](mailto:mohammeds.abed@uokufa.edu.iq)

<sup>2</sup>[raad.muhsen1978@yahoo.com](mailto:raad.muhsen1978@yahoo.com)

**Abstract:** In this paper, one type of volterra integralequations (VIEs) isclassified to be nth-order VIE of fourth-kind. This class ofnth-order VIE usually occurs in many fields of physics andengineering. The nth-order VIE of fourth-kind is converted tonth-order ordinary differential equations (ODEs). This nth-order ODE is then,solved using variational iteration method (VIM). A new iterationtechnique is proposed to solve a class of nonlinear integralequations. It shows that the variational iteration method (VIM) isefficient and powerful tool for dealing with this class ofnonlinear integral equations. Some examples are selectedto illustrate theeffectiveness and simplicity of the method. Thecomparison of the results of VIM with those obtained by classicalmethod reveals that VIM is very effective, convenient and quiteaccurate to both linear and nonlinear problems. It is predictedthat VIM can be widely applied inthe mathematical model of different problems in physics and engineering.

**Keywords:** Integral equations; Voltera integral equation; VIE; nth-order; VIM; systemof ODEs.

### References:

- [1] Cardone, A., Ixaru, L. G., Paternoster, B., Santomauro, G., "Ef-Gaussian direct quadrature methods for Volterra integral equations with periodic solution", *Mathematics and Computers in Simulation*,(2013).
- [2] Chen, H., Zhang, C., "Block boundary value methods for solving Volterra integral and integro-differential equations", *Journal of Computational and Applied Mathematics*, 236(2012), 2822.
- [3] Abbasbandy, S., "Numerical solutions of the integral equations: Homotopy perturbation method and Adomians decomposition method", *Applied Mathematics and Computation*, 173(2006), 493.

## A NOT ON PROPERTIES THAT IMPLY THE FIXED POINT PROPERTY

Mohammad KNEFATI<sup>1</sup> and Vatan KARAKAYA<sup>2</sup>

<sup>1</sup> *Yildiz Technical University, Istanbul TURKEY*

<sup>22</sup> *Department of Mathematical Engineering, Yıldız Technical University, Istanbul/TURKEY*

[mknefati@gmail.com](mailto:mknefati@gmail.com)

[vkaya@yahoo.com](mailto:vkaya@yahoo.com)

**Abstract:** We show that Banach  $c_0(\Gamma)$  with Day's norm space satisfy the weak fixed point property, and prove the relationship between the weakly 2-rotund (W2R) and the fixed point property of Banach spaces under renorming. Moreover distinguish between this property and other geometrical properties that imply the fixed point property.

**Keywords:** Fixed point property; Day's norm; Weakly 2-rotund.

### References:

- [1] K. Goebel, W.A. Kirk, Topics in Metric Fixed Point Theory, Cambridge University press, 1990.
- [2] N. Simsek, E.Savas, V.Karakaya, On Geometrical Properties of Some Banach Spaces .APPLIED MATHEMATICS & INFORMATION SCIENCES, 7(1), 295-300,2013.
- [3] T.D. Benavides, A renorming of some nonseparable Banach spaces with the fixed point property, J. Math.Anal.Appl.350, 525-530, 2009.
- [4] B. Hajek, M.johanis, Characterisation of reflexivity by equivalent renorming J. Msc2000.46B03,46B10,46B20,2003.

## INTEGRAL TYPE ALMOST CONTRACTION MAPPINGS IN METRIC SPACES

M. Abdussamed MALDAR<sup>1</sup>, Vatan KARAKAYA<sup>2</sup>

<sup>1</sup>*Department of Mathematics, Aksaray University,*

*Aksaray/TURKEY*

<sup>2</sup>*Department of Mathematical Engineering, Yıldız Technical University,  
İstanbul/TURKEY*

[mmaldar@aksaray.edu.tr](mailto:mmaldar@aksaray.edu.tr)

[vkaya@yahoo.com](mailto:vkaya@yahoo.com)

**Abstract:** In this presentation, The concept of integral type almost contraction is introduced and then two fixed point theorems for this class of operators in complete metric spaces are proven. Our results extend some fixed point theorems due to Rhoades, Ćirić and many others.

**Keywords:** strong convergence, contractive condition of integral type, metric space.

### References:

- [4] Berinde V., "On the approximation of fixed points of weak contractive mappings", *Carpathian J. Math*, 19(2003), 7-22.
- [5] Berinde V., Pacurar, M., "Fixed points and continuity of almost contractions", *Fixed Point Theory*, 9(2008), 23-34
- [6] Branciari, A., "A fixed point theorem for mappings satisfying a general contractive condition of integral type", *Int. J. Math. Math. Sci.*, no 9, 2002, 521-536.
- [7] Ćirić, Lj.B. "A generalization of Banach's contraction principle", *Proc. Am. Math. Soc.*, 45(1974), 267-273.
- [8] Dogan, K., Karakaya, V., " On the convergence and stability results for a new general iterative process" *Hindawi Publishing Cor. Sci. World Jou.*, 2014(2014), 8.
- [9] Olatinwo, M. O., "Some stability results for Picard and Mann iteration processes using contractive condition of integral type", *creative Math. and inf.*,19(2010).
- [10] Rhoades, B. E., "Two fixed point theorems for mappings satisfying a general contractive condition of integral type", *Int. J. Math. Sci.* 63(2003), 4007-4013.

## MAXIMUM NORM ANALYSIS OF SCHWARZ METHOD FOR ELLIPTIC QUASI-VARIATIONAL INEQUALITIES

Mohammed BEGGAS<sup>1</sup>, Mohamed HAIOUR<sup>2</sup>

<sup>1</sup>*Department of Mathematics, University of Eloued, Eloued 39000, Algeria*  
[beggasmr@yahoo.fr](mailto:beggasmr@yahoo.fr)

<sup>2</sup>*Department of Mathematics, Faculty of Science, University of Annaba, B.P. 12 Annaba 23000, Algeria*  
[haiourm@yahoo.fr](mailto:haiourm@yahoo.fr)

**Abstract:** Schwarz method has been used to solve the stationary or evolutionary boundary value problems on domains which consist of two or more overlapping sub-domains. In this paper we provide a maximum norm analysis of an overlapping Schwarz method on non-matching grids for a quasi-variational inequality generalized where the obstacle and the second member depend on the solution. We proved that the discretization on every sub-domain converges in uniform norm and we give a result of approximation for the method in uniform norm.

**Keywords:** Schwarz method, quasi-variational inequalities,  $L^\infty$ -error estimate.

### References:

- [1] M. Boulbrachene and S. Saadi, "Maximum norm analysis of an overlapping non-matching grids method for the obstacle problem", *Hindawi pub. cop* (2006), 1-10.
- [2] O. M. Haiour and S. Boulaaras, "Overlapping domain decomposition method for elliptic quasi-variational inequalities related to impulse control problem with mixed boundary conditions", *Pro. I. Acad. sci (Math Sci)*, Vol 121, No. 4, 2011, 481-493.
- [3] P.L. Lions, "On the Schwarz alternating method I. First international symposium on domain decomposition methods for partial differential equations", *SLAM*, Philadelphia 1988.

## VARIATION DIMINISHING INTEGRAL OPERATORS OF THE CONVOLUTIONS TYPE ASSOCIATED WITH THE DUNKL OPERATOR ON $\mathbb{R}$

Moncef DZIRI

*Faculty of Sciences of Tunis, Tunisia*  
moncef.dziri@iscae.mu.tn

**Abstract:** Using harmonic analysis associated with Dunkl operator on  $\mathbb{R}$  we give necessary and sufficient conditions such that the number of sign changes of a convolution transforms  $T(f)$  associated with Dunkl operator never exceeds the number of sign changes of the function  $f$ .

## PERTURBED PARTIAL FRACTIONAL ORDER FUNCTIONAL DIFFERENTIAL EQUATIONS WITH INFINITE DELAY IN FRECHET SPACES

Mouffak BENCHOHRA and Mohamed HELLAL

*Laboratoire de Mathematiques, Universite de Sidi Bel-Abbes,  
B.P. 89, 22000, Sidi Bel-Abbes, Algeria*

[benchokra@univ-sba.dz](mailto:benchokra@univ-sba.dz)  
[hellalmohamed@yahoo.fr](mailto:hellalmohamed@yahoo.fr)

**Abstract:** In this paper we investigate the existence of solutions of perturbed partial hyperbolic differential equations of fractional order with finite delay and Caputo's fractional derivative by using a nonlinear alternative of Avramescu on Frechet spaces.

**Key words :** Partial functional differential equation, fractional order, left-sided mixed Riemann-Liouville integral, Caputo fractional-order derivative, finite delay, Frechet space.

### References:

- [1] R. P. Agarwal, M. Belmekki and M. Benchohra, A survey on semilinear differentialequations and inclusions involving Riemann-Liouville fractional derivative. Adv Differ. Equat. 2009(2009) Article ID 981728, 1-47.
- [2] R.P Agarwal, M. Benchohra and S. Hamani, A survey on existence result for boundary value problems of nonlinear fractional differential equation and inclusions, Acta. Appl. Math. 109 (3) (2010), 973-1033.
- [3] C. Avramescu, Some remarks on a fixed point theorem of Krasnoselskii, Electron. J. Qual. Theory Differ. Equ., 5 (2003), 1-15.

## ON SHERMAN'S INEQUALITY

Muhammad Adil KHAN

<sup>1</sup>Department of Mathematics, University of Peshawar

Istanbul/TURKEY

adilswati@gmail.com

**Abstract:** Generalizations of Sherman's inequality for a convex function of higher order are obtained by applying Hermite interpolating polynomials. The results for particular cases, namely, Lagrange, (m; n-m) and two-point Taylor interpolating polynomials are also considered. The Gruss and Ostrowski type inequalities related to these generalizations are given.

## ON GENERALIZED DIFFERENCE SEQUENCES OF FUNCTIONS

Muhammed ÇINAR<sup>1</sup>, Mikail ET<sup>2</sup>

<sup>1</sup>Department of Mathematics, MusAlparslan University,

Mus/TURKEY

[muhammedcinar23@gmail.com](mailto:muhammedcinar23@gmail.com)

<sup>2</sup>Department of Mathematics, Firat University,

Elazığ/TURKEY

[mikaillet@yahoo.com](mailto:mikaillet@yahoo.com)

**Abstract:** In this presentation, we introduce the concepts of pointwise  $\Delta_m^r$ -convergence and uniform  $\Delta_m^r$ -convergence sequences of functions. Furthermore some relations between the spaces of sequences of functions  $c(\Delta_m^r, F(p))$ ,  $c_0(\Delta_m^r, F(p))$ ,  $c(\Delta_m^r, F)$ ,  $c_0(\Delta_m^r, F(u))$  and  $\ell_\infty(\Delta_m^r, F(u))$  are examined.

**Keywords:** Difference sequence, Sequences of functions.

### References:

- [1] B. Altay and F. Başar, On the fine spectrum of the difference operator  $\Delta$  on  $c_0$  and  $c$ , Inform. Sci. 168(1-4) (2004), 217--224.
- [2] H. Kızmaz, On certain sequence spaces, Canad. Math. Bull. 24(2) (1981), 169-176.
- [3] M. Et and R. Colak, On generalized difference sequence spaces, Soochow J. Math. 21(4) (1995), 377-386.
- [4] Ç. A. Bektaş, M. Et, and R. Çolak, Generalized difference sequence spaces and their dual spaces, J. Math. Anal. Appl. 292(2) (2004), 423--432.

## INVERSE SOURCE PROBLEM FOR TIME-FRACTIONAL HEAT EQUATION WITH A GENERALIZED IMPEDANCE BOUNDARY CONDITION

Muhammed ÇIÇEK<sup>1</sup>, Mansur İSGENDEROĞLU (ISMAILOV)<sup>2</sup>

<sup>1</sup>*Department of Mathematics, Bursa Technical University, Bursa/TURKEY*  
[muhammed.cicek@btu.edu.tr](mailto:muhammed.cicek@btu.edu.tr)

<sup>2</sup>*Department of Mathematics, Gebze Technical University, Kocaeli/TURKEY*  
[mismailov@gtu.edu.tr](mailto:mismailov@gtu.edu.tr)

**Abstract:** In this paper, an inverse problem of reconstruction of a time-dependent source term in a one-dimensional time-fractional diffusion equation from the energy measurement and generalized impedance boundary condition is studied. This problem is obtained from a classical diffusion problem by replacing the time derivative with a fractional derivative. The well-posedness of the inverse problem is shown by using the generalized Fourier method.

**Keywords:** Fractional diffusion equation, Generalized Impedance Boundary Condition, Inverse source problem, Generalized Fourier method.

### References:

- [1] R. Metzler, J. Klafter, "The random walk's guide to anomalous diffusion: a fractional dynamics approach", *Physics Reports*, 339(2000), 1-77.
- [2] H. E. Roman, P. A. Alemany, "Continuous-time random walks and the fractional diffusion equation", *Journal of Physics A*, 27(1994), 3407.
- [3] A. Hazanee, D. Lesnic, M. I. Ismailov, N. B. Kerimov, "An inverse time dependent source term for the heat equation with a non-classical boundary condition", *Applied Mathematical Modelling*, 39(2015), 6258-6272.
- [4] M. I. Ismailov, M. Cicek, "Inverse source problem for a time-fractional diffusion equation with nonlocal boundary conditions", *Applied Mathematical Modelling*, 40(2016), 4891-4899.



## A HYBRIDIZABLE DISCONTINUOUS GALERKIN METHOD FOR A CLASS OF FRACTIONAL BOUNDARY VALUE PROBLEM

Mehmet Fatih KARAASLAN<sup>1</sup>, Muhammet KURULAY<sup>2</sup>

<sup>1</sup>*Department of Statistics, Yıldız Technical University,  
Istanbul/TURKEY*  
[mfatih@yildiz.edu.tr](mailto:mfatih@yildiz.edu.tr)

<sup>2</sup>*Department of Mathematical Engineering, Yıldız Technical University,  
Istanbul/TURKEY*  
[mkurulay@yildiz.edu.tr](mailto:mkurulay@yildiz.edu.tr)

**Abstract:** In this work, we present a hybridizable discontinuous Galerkin (HDG) method for solving a class of fractional boundary value problem that involves Caputo derivative with order  $\alpha, \beta > \dots$ . One of the main properties of HDG methods is that they are efficiently implementable since it is possible to eliminate all internal degrees of freedom and obtain a global linear system that only involves unknowns at the element interfaces. Since the global matrix in the linear system is tridiagonal, symmetric and positive definite, the method gives effective and convergent results in the ordinary and partial differential equations. Also, an appropriate choice of the stability parameter has a very important effect on the convergence of the obtained system. Therefore, the HDG method is investigated for the mentioned fractional boundary value problems. We display the results of a series of numerical experiments to ascertain by using MATLAB programme.

**Keywords:** Hybridizable discontinuous Galerkin method, boundary value problem, fractional derivative, fractional calculus.

### References:

- [1] Kilbas, A. A. and Trujillo, J.J., (2002). "Differential equations of fractional order: methods, results and problems. II", *Applicable Analysis*, 81(2):435-493.
- [2] Ervin, V.J. and Roop, J.P., (2006). "Variational formulation for the stationary fractional advection dispersion equation", *Numerical Methods for Partial Differential Equations*, 22(3):558-576.
- [3] Nakhushiev, A.M., (1977). "Sturm-Liouville problem for an ordinary differential equation of second order with fractional derivatives in the lower-order terms", In *Akademiia Nauk SSSR, Doklady*, 234:308-311.

## OSTROWSKI TYPE INEQUALITIES FOR GENERALIZED s-CONVEX FUNCTIONS IN THE SECOND SENSE

Muharrem TOMAR<sup>1,a</sup> and Erhan SET<sup>1,b</sup>

<sup>1</sup>*Department of Mathematics, Ordu University,  
Ordu/TURKEY*

[muharremtomar@gmail.com](mailto:muharremtomar@gmail.com)<sup>a</sup>,

[erhanset@yahoo.com](mailto:erhanset@yahoo.com)<sup>b</sup>

**Abstract:** In this paper, we first obtain a generalized integral identity for twice locally differentiable functions. Then, using functions whose second local derivatives in absolute value at certain powers are generalized s-convex in the second sense, we obtain some new Ostrowski type inequalities.

**Keywords:** Local fractional integral, Hermite-Hadamard inequality, Generalized Convex Functions, Hölder's Inequality, Generalized Ostrowski inequality.

### References:

- [1] X. J. Jang, "Advanced Local Fractional Calculus and Its Applications", World Science Publisher, New York, 2012.
- [2] X. J. Yang, "Local fractional integral equations and their applications", Adv. Comput. Sci. Appl. 1(4)(2012).
- [3] X. J. Yang, "Generalized local fractional Taylor's formula with local fractional derivative", J. ExpertSys. 1(1) (2012) 26-30.
- [4] S. Erden and M. Z. Sarikaya, Generalized Pompeiu type inequalities for local fractional integrals and its applications, Appl. Math. Comput. 274 (2016), 282-291.
- [5] E. Set and M. Tomar, "New inequalities of Hermite-Hadamard type for generalized convex functions with applications", Facta Univ. Ser. Math. Inform. (2016), in press.
- [6] H. Mo and X. Sui, "Generalized s-convex function on fractal sets", arXiv:1405.0652v2 [math.AP].

## ON $I$ -CONVERGENCE OF SEQUENCES OF FUNCTIONS IN 2-NORMED SPACES

Mukaddes ARSLAN and Erdiñ DÜNDAR<sup>1</sup>

<sup>1</sup>*Department of Mathematics, AfyonKocatepe University,  
Afyonkarahisar/TURKEY*

[mukaddes\\_arslan@hotmail.com](mailto:mukaddes_arslan@hotmail.com), [edundar@aku.edu.tr](mailto:edundar@aku.edu.tr)

**Abstract:** In this paper, we study concepts of convergence and ideal convergence of sequence of functions and investigate relationships between them and some properties such as linearity in 2-normed spaces. Also, we prove a decomposition theorem for ideal convergent sequences of functions in 2-normed spaces.

**Keywords:** Ideal, Ideal convergence, Sequence of functions, 2-normed spaces.

## DEFECT-DEFERRED CORRECTION METHOD FOR A FLUID FLOW AT HIGH REYNOLDS NUMBERS

Mustafa AGGUL

**Abstract:** A method is presented, that combines the defect and deferred correction approaches to approximate solutions of Navier-Stokes equations at high Reynolds number. The method is of high accuracy in both space and time, and it allows for the usage of legacy codes – a frequent requirement in the simulation of turbulent flows in complex geometries. The two-step method is considered here; in order to obtain a regularization that is second order accurate in space and time, the method computes a low-order accurate, stable and computationally inexpensive approximation (Backward Euler with artificial viscosity) twice. The results are readily extendable to the higher order accuracy cases by adding more correction steps. Both the theoretical results and the numerical tests provided demonstrate that the computed solution is stable and the accuracy in both space and time is improved after the correction step. We also perform a qualitative test to demonstrate that the method is capable of capturing qualitative features of a turbulent flow, even on a very coarse mesh.

## ALMOST CONVERGENCE METHOD WITH FRACTIONAL ORDER OPERATOR

Murat KİRİŞÇİ<sup>1</sup>

<sup>1</sup>*Department of Mathematical Education, Istanbul University,  
İstanbul/TURKEY*

[mkirisci@hotmail.com](mailto:mkirisci@hotmail.com), [murat.kirisci@istanbul.edu.tr](mailto:murat.kirisci@istanbul.edu.tr)

**Abstract:** The purpose of this paper is twofold. First, basic concepts such as Gamma function, almost convergence, fractional order difference operator and sequence spaces are given as a survey character. Thus, the current knowledge about those concepts are presented. Second, we construct the almost convergent spaces with fractional order difference operator and compute dual spaces which are help us in the characterization of matrix mappings. After we characterize to the matrix transformations, we give some examples. In this paper, the notation  $\Gamma(n)$  will be shown the Gamma function. For  $n \notin \{0, -1, -2, \dots\}$ , Gamma function defined by an improper integral  $\Gamma(n) = \int_0^{\infty} e^{-t} t_{n-1} dt$ .

**Keywords:** Gamma Function, almost convergence, fractional order operator, matrix domain

### References:

- [1] B. Altay, F. Başar "Certain topological properties and duals of the domain of a triangle matrix in a sequence spaces", J. Math. Anal. Appl., 336, (2007), 632-645.
- [2] P. Baliarsingh, "Some new difference sequence spaces of fractional order and their dual space", Appl. Math. Comput., 219, (2013), 9737.
- [3] P. Baliarsingh, "On the classes of fractional order difference sequence spaces and their matrix transformations", Appl. Math. Comput., 250, (2015), 635.
- [4] U. Kadak, P. Baliarsingh "On certain Euler difference sequence spaces of fractional order and related dual properties", J. Nonlinear Sci. Appl., 8 (2015), 997.
- [5] M. Kirişçi, "Almost convergence and generalized difference matrix", Comp. Math. Appl., 61 (2011), 602.

**ON SOME FIXED POINT THEOREMS WITH  
GENERALIZED CONTRACTIONS IN COMPLETE CONE  
METRIC SPACE SENDOWED WITH A PARTIAL ORDER  
AND INVOLVING A GRAPH**

Murat CANSAN<sup>1</sup>

<sup>1</sup>*Department of Mathematics, YuzuncuYil University,  
Van/TURKEY  
[mcancan@yyu.edu.tr](mailto:mcancan@yyu.edu.tr)*

**Abstract:** The aim of this presentation is to present some fixed point theorems for generalized contractions by altering distance functions in a complete cone metric spaces endowed with a partial order and involving a graph.

**Keywords:** Complete cone metric space, fixed point theorem, generalized contraction, graph.

**References:**

- [1] J. Harjani, K. Sadarangani, "Generalized contractions in partially ordered metric spaces and applications to ordinary differential equations. (English summary)", *Nonlinear Anal.*, 72(2010), no. 3-4, 1188–1197.
- [2] J. Jachymski, "The contraction principle for mappings on a metric space with a graph. (English summary)", *Proc. Amer. Math. Soc.*, 136(2008), no. 4, 1359–1373.
- [3] M. Asadi, H. Soleimani, "Some fixed point results for generalized contractions in partially ordered cone metric spaces. (English summary)", *J. Nonlinear Anal. Optim.*, 6(2015), no. 1, 53–60.
- [4] S. M. A. Aleomraninejad, Sh. Rezapour, N. Shahzad, "Some fixed point results on a metric space with a graph. (English summary)", *Topology Appl.*, 159(2012), no. 3, 659–663.

## DISCUSSION ON ADVECTION-DIFFUSION EQUATION THROUGH FINITE DIFFERENCE SCHEMES

Murat SARI, Lamia J.M. Al-MASHHADANI, Arshed A. AHMAD

*Department of Mathematics, Yıldız Technical University, Istanbul, TURKEY*

[sarim@yildiz.edu.tr](mailto:sarim@yildiz.edu.tr)

**Abstract:**The aim of this presentation is to numerically discuss physical behavior of the advection diffusion equation. To achieve this, fundamental finite difference schemes are used both in time and in space. In order to realize properly the physical behavior of the model, the produced solutions have been discussed in terms of advection-diffusion relation. The current schemes seem to be trustworthy and moderate alternative to understand numerical thinking for these kinds of models.

**Keywords:**Advection diffusion equation, finite difference scheme, numerical modelling, physical behavior.

### References:

- [1] M. Sari, G. Gürarlan, A. Zeytinoğlu, "High-order finite difference schemes for solving the advection-diffusion equation", *Mathematical and Computational Applications*, 15(3)(2010) 449-460.
- [2] T.-L. Tsai, J.-C. Yang, L.-H. Huang, "Characteristics method using cubic-spline interpolation for advection-diffusion equation", *Journal of Hydraulic Engineering ASCE*, 130(6)(2004),580-585.
- [3] R. Szymkiewicz, "Solution of the advection-diffusion equation using the spline function and finite elements", *Communications in Numerical Methods in Engineering*, 9(1993), 197-206.

## THE GENERATING FUNCTIONS FOR THE FAMILY OF THE GENERALIZED BERNOULLI POLYNOMIALS

Mustafa ALKAN

Akdeniz University, Faculty of Science,  
Department of Mathematics,  
07058 Antalya, Turkey  
alkan@akdeniz.edu.tr

**Abstract:** We study the generalization Bernoulli numbers and polynomials attached to a periodic group homomorphism. By using a fixed periodic group homomorphism, we obtain not only multiplication formulas, but also some new identities for the generalized Bernoulli polynomials.

## TWO NEW PROOFS OF GENERALIZED BIPERIODIC FIBONACCI IDENTITY IN TERMS OF THE DETERMINANTS OF TRIDIAGONAL MATRIX

Yasin YAZLIK, Musa BAŞBÜK

<sup>1</sup>Department of Mathematics, Nevşehir Hacı Bektaş Veli University,  
Nevşehir / TURKEY

[yyazlik@nevsehir.edu.tr](mailto:yyazlik@nevsehir.edu.tr), [mbasbuk@gmail.com](mailto:mbasbuk@gmail.com)

**Abstract:** In this study, we present two new proofs of generalized Fibonacci identity  $q_{m+n-1} = q_m q_n a^{\xi(mn+n-m)-1} b^{1-\xi(mn+n-m)} + q_{m-1} q_{n-1} a^{-\xi(mn)} b^{\xi(mn)}$  via the determinants of  $nxn$  tridiagonal matrix evaluating by Laplace expansion method and constructing  $2x2$  square matrices, where  $m, n$  are any two positive integers,  $\{q_n\}_{n=0}^{\infty}$  is the generalized Fibonacci sequence and  $\xi(n) = \begin{cases} 0 & \text{if } n \text{ is even,} \\ 1 & \text{if } n \text{ is odd,} \end{cases}$  is the parity function.

**Keywords:** Generalized Fibonacci sequence, Tridiagonal matrix, Laplace expansion method.

### References:

- [1] M. Edson, O. "Yayenie, A new generalization of Fibonacci sequences and extended Binets formula", *Integers* 9(A48) (2009), 639-654.
- [2] Y. Yazlik, N. Taskara, "A note on generalized k-Horadam squence", *Computers and Mathematics with Applications* 63 (2012), 36-41.
- [3] O. Yayanie, "A note on generalized Fibonacci squence", *Applied Mathematics and Computation* 217 (2011), 5603-5611.
- [4] Y. Yazlik, N. Yilmaz, N. Taskara, "On the Determinant of Tridiagonal Matrices via some Special Numbers", *Selcuk Journal of Applied Mathematics* 13(2) (2012), 25-30.

## SOME NOTES ON THE SEQUENCE SPACES $l_p^\lambda(G^m)$ AND $l_\infty^\lambda(G^m)$

Mustafa Cemil BİŞGİN<sup>1</sup>, Abdulkabbar SÖNMEZ<sup>2</sup>

<sup>1</sup>Department of Mathematics, Recep Tayyip Erdoğan University,  
Rize/TURKEY

[mustafa.bisgin@erdogan.edu.tr](mailto:mustafa.bisgin@erdogan.edu.tr)

<sup>2</sup>Department of Mathematics, Erciyes University,  
Kayseri/TURKEY

[sonmez@erciyes.edu.tr](mailto:sonmez@erciyes.edu.tr)

**Abstract:** In this work, we introduce the sequence spaces  $l_p^\lambda(G^m)$  and  $l_\infty^\lambda(G^m)$  derived by the domain of the composition of  $m$ -th order generalized difference matrix and lambda matrix. Moreover, we determine some topological properties and examine inclusion relations related to those spaces. Furthermore, we give Schauder basis for the space  $l_p^\lambda(G^m)$ . Finally, we determine  $\alpha$ -,  $\beta$ - and  $\gamma$ -duals of the spaces  $l_p^\lambda(G^m)$  and  $l_\infty^\lambda(G^m)$ .

**Keywords:** Sequence Space, Matrix Transformation, Matrix Domain, Schauder Basis, Duals, Topological Property.

### References:

- [1] F. Başar, A. Karaisa, "Some New Generalized Difference Spaces Of Nonabsolute Type Derived From The Spaces  $l_p$  and  $l_\infty$ ", The Scientific World Journal, (2013), Article ID 349346, 15 Pages.
- [2] M. Başarır, M. Kayıkçı, "On Generalized  $B^m$ -Riesz Difference Sequence Space And  $\beta$ -Property", J. Inequal. Appl., (2009), Article ID 385029, 18 Pages.
- [3] M. Mursaleen, A. K. Noman, "On Some New Sequence Spaces Of Nonabsolute Type Related To The Spaces  $l_p$  and  $l_\infty$  I", Filomat, 2(2011), 33-51.
- [4] M. Mursaleen, A. K. Noman, "On Some New Sequence Spaces Of Nonabsolute Type Related To The Spaces  $l_p$  and  $l_\infty$  II", Math. Commun., 16(2011), 383-398.



## A PARAMETERIZED SINGULARLY PERTURBED BOUNDARY VALUE PROBLEM

Mustafa KUDU<sup>1</sup>, Gabil M. AMIRALIYEV <sup>2</sup>

<sup>1</sup>*Department of Mathematics, Erzincan University,  
Erzincan/TURKEY*

[muskud28@yahoo.com](mailto:muskud28@yahoo.com)

<sup>2</sup>*Department of Mathematics, Erzincan University,  
Erzincan/TURKEY*

[gabilamirali@yahoo.com](mailto:gabilamirali@yahoo.com)

**Abstract:** This article is concerned with the parameterized second order boundary value problem with layer behavior. Asymptotic estimates for the solution and its first and second derivatives have been established. The obtained results are important for construction and analysis of appropriate approximate methods. The illustrative examples are given.

**Keywords:** Depending on a parameter, Asymptotic bounds, Singular perturbation, Boundary layer.

### References:

- [1] G.M., Amiraliyev, Kudu M. and H.Duru, Uniform difference method for a parameterized singular perturbation problem, *Appl. Math. Comput.*, 175(2006), 89-100.
- [2] M. Fěćkan, Parametrized singularly perturbed boundary value problems, *J.Math. Anal. Appl.* 188(1994), 426--435.
- [3] T. Jankowski, Generalization of the method of quasilinearization for differential problems with a parameter, *Dyn. Syst. Appl.* 8(1999), 53—72
- [4] M. Kudu, Asymptotic Estimates for Second-Order Parameterized Singularly Perturbed Problem, *Appl. Math.* 5(13)(2014),1988-1992.
- [5] M. Kudu and I. Amirali, A Priori Estimates of Solution of Parametrized Singularly Perturbed Problem, *J.Appl. Math. Phys.* 4(1)(2016), 73-78.

## **$p$ -ADIC GIBBS MEASURES FOR THE ISING-VANNIMENUS MODEL ON CAYLEY TREE OF ORDER THREE**

Mutlay DOGAN<sup>1</sup>, Hasan AKIN<sup>2</sup>

<sup>1</sup>*Department of Mathematics, Faculty of Education, Zirve University, 27260 Gaziantep/TURKEY*

[mutlay.dogan@zirve.edu.tr](mailto:mutlay.dogan@zirve.edu.tr)

<sup>2</sup>*Department of Mathematics, Faculty of Education, Zirve University, 27260 Gaziantep, Turkey*

[hasan.akin@zirve.edu.tr](mailto:hasan.akin@zirve.edu.tr)

### **Abstract:**

**Keywords:** Cayley tree,  $p$ -adic Gibbs measure,  $p$ -adic Ising-Vannimenus model, Dynamics Systems.

### **References:**

- [1] Akin, H., "Using New Approaches to obtain Gibbs Measures of Vannimenus model on a Cayley tree", Chinese J. of Phys, to appear, 2016, [arXiv:1510.08405](https://arxiv.org/abs/1510.08405)
- [2] Vannimenus, J., "Modulated phase of an Ising system with competing interactions", Zeit. f. Phys. B Con. Mat. Mod. Phys., 43 (1981) 141-148.
- [3] Mukhamedov, F.M., Omirov, B. A., "On cubic equations over  $p$ -adic fields", Int. Journal of Num. Theory, 10, (2014) 1171-1100.
- [4] Mukhamedov, F.M., Dogan, M. and Akin, H., "Phase transition for  $p$ -adic Ising-Vannimenus Model on a Cayley tree", J. Stat. Mech., P10031, (2014), 1-21.

## AN EXISTENCE THEOREM FOR ANALYTIC SOLUTION OF A FRACTIONAL DIFFERENTIAL EQUATION WITH CAPUTO DERIVATIVE

Müfit ŞAN

*Department of Mathematics, ÇankırıKaratekin University,  
Çankırı/TURKEY  
[mufitsan@hotmail.com](mailto:mufitsan@hotmail.com)*

**Abstract:** In this work, we investigate the existence of analytic solution of an initial value problem for the nonlinear fractional differential equation with Caputo derivative by using Schauder fixed point theorem and a new technique related to Schwarz Lemma for analytic functions of several variables.

**Keywords:** Fractional differential equation, existence and uniqueness, fixed point theorem, Schwarz's lemma.

### References:

- [1] D. Baleanu and O.G. Mustafa, "On the global existence of solutions to a class of fractional differential equations." *Computers&Mathematics with Applications* 59.5 (2010): 1835-1841.
- [2] D. Delbosco and L. Rodino, Existence and uniqueness for a nonlinear fractional differential equation, *J. Math. Anal. Appl.*, 204 (1996), 609-625.
- [3] M. Şan,, and K. N. Soltanov. "The New Existence and Uniqueness Results for Complex Nonlinear Fractional Differential Equation." *arXiv preprint arXiv:1512.04780* (2015).
- [4] S.G. Samko, A.A. Kilbas and O.I. Marichev, *Fractional Integrals and Derivatives: Theory and Applications*, Gordon and Breach, Yverdon, Switzerland, 1993.
- [5] T.W., Gamelin, *Complex Analysis*, Springer Verlag, 2003.

## SOME CONVERGENCE AND DATA DEPENDENCE RESULTS IN A GENERAL CLASS OF CONTRACTIVE TYPE OPERATORS

Müzeyyen ERTÜRK<sup>1</sup>, Vatan KARAKAYA<sup>2</sup>

Faik GÜRSOY<sup>3</sup>

<sup>1,3</sup>*Department of Mathematics, Adiyaman University,  
Adiyaman/TURKEY*

<sup>1</sup>[merturk3263@gmail.com](mailto:merturk3263@gmail.com)

<sup>3</sup>[faikgursoy02@hotmail.com](mailto:faikgursoy02@hotmail.com)

<sup>2</sup>*Department of Mathematical Engineering, Yıldız Technical University,  
İstanbul/TURKEY*

[vkaya@yahoo.com](mailto:vkaya@yahoo.com)

**Abstract:** In this presentation, we study convergence and data dependence results of the iteration method, which was introduced by Thianwan and Suantai in [1], for a general class of operators. Also, we support our results with examples. Our study generalizes some results in the literature.

**Keywords:** Iterative schemes, convergence, data dependence

### References:

- [1] Thianwan, Sornsak, and SuthepSuntai. "Convergence criteria of a new three-step iteration with errors for nonexpansive nonself-mappings." *Computers and Mathematics with Applications* 52.6-7 (2006): 1107-1118.
- [2] Soltuz, S. M., "Data dependence for strongly pseudocontractive operators." *Advances in Nonlinear Variational Inequalities* 13 1 (2010): 19-27.

## INTEGRABLE SOLUTIONS OF A NONLINEAR INTEGRAL EQUATION VIA SCHAEFER-KRASNOSELSKII FIXED POINT THEOREM

N. ABADA and L. AITKAKI

*Laboratoire de Mathématiques Appliquées et Didactique ,  
Ecole Normale Supérieure, Constantine, Algerie*

**Abstract:** We study the existence of solutions of nonlinear volterra equation in the space  $L^1([0, +\infty[)$ . With the help of Schaefer-Krasnoselskii fixed point theorem and the theory of measure of weak noncompactness, we prove an existence result for a functional integral equation. An example is given to support our results.

**Keywords:** Krasnoselskii fixed point theorem, measure of noncompactness, nonlinear integral equation.

## A FIXED POINT PROOF OF THE CONVERGENCE OF A NEWTON-LIKE METHOD OBTAINED BY THE NORMAL S- ITERATION PROCESS

Nazli KARACA<sup>1</sup>, Isa YILDIRIM<sup>2</sup>

<sup>1</sup>*Department of Mathematics, Ataturk University,  
Erzurum/TURKEY*

[nazli.kadioglu@atauni.edu.tr](mailto:nazli.kadioglu@atauni.edu.tr)

<sup>2</sup>*Department of Mathematics, Ataturk University,  
Erzurum/TURKEY*

[isayildirim@atauni.edu.tr](mailto:isayildirim@atauni.edu.tr)

**Abstract:** In this paper, we indicate a new Newton-type iterative method in  $\mathbb{R}$ . It is shown that this process converges to the unique solution of the scalar nonlinear equation  $f(x) = 0$ , under some conditions, involving only  $f$  and  $f'$ . Finally, we present numerical examples to support the analytic result proved herein.

**Keywords:** Fixed point, Newton's method, nonlinear operator.

### References:

- [1] V. Berinde, "Conditions for the convergence of the Newton method", An. Şt.Univ. Ovidius Constanta, 3(1995), No. 1, 22-28.
- [2] V. Berinde, M. Pacurar, "A fixed point proof of the convergence of a Newton-type method", Fixed Point Theory, 7 (2006), No. 2, 235-244.
- [3] D. R. Sahu, "Applications of the S-iteration process to constrained minimization problems and split feasibility problems", Fixed Point Theory, 12(2011), 187-204.

## A REARRANGEMENT ESTIMATE FOR THE GENERALIZED MULTILINEAR ANISOTROPIC FRACTIONAL INTEGRALS

Nezrin GADIROVA

*Institute of Mathematics and Mechanics,  
Baku, AZERBAIJAN*

[gadirovanezrin@gmail.com](mailto:gadirovanezrin@gmail.com)

**Abstract:** In this report, author studies  $L_{p_1} \times L_{p_2} \times \dots \times L_{p_k}$  boundedness of the generalized multilinear anisotropic fractional integral operators. O'Neil type inequality for the generalized multilinear fractional integral is proved. Was given a new proof of the Hardy-Littlewood-Sobolev multilinear anisotropic fractional integration theorem, based on a pointwise estimate of the rearrangement multilinear anisotropic fractional type integral.

## CALSESSES OF I-CONVERGENTDOUBLE SEQUENCES OVER N-NORMED SPACES

Nazneen KHAN

*<sup>1</sup>Department of Mathematics, Taibah University,  
Madina/SAUDI ARABIA  
[nazneen4maths@gmail.com](mailto:nazneen4maths@gmail.com)*

**Abstract:**In this article, I introduce some new classes of I-convergent double sequence spaces over n-normed space using the concept of sequence of moduli and double lacunary sequence space. I have studied and proved their algebraic and topological properties and some inclusion relations. Some useful examples have been constructed to understand new terms defined in this article. By varying different parameters used in the definition of these spaces, a case study of changes in their behavior has been shown.

**Keywords:** I-convergence, lacunary sequence space, n-norm, double sequence.

### References:

- [1] P.Das, P.Kostyrko, P.Malik, W.Wilczynski, "I and I<sup>\*</sup>-Convergence of Double Sequences", Math. Slovaca, 58(2008), 605-620.
- [2] M. Mursaleen, S.A. Mohiuddine, "On ideal convergence of double sequences in probabilistic normed spaces", Math. Rep., 12(62) (2010), 359-371.
- [3] E. Savaş, R.F.Patterson, "On some double almost lacunary sequences defined by Orlicz function", Filomat, 19(2005), 35-44.

## ON SOME GEOMETRICAL PROPERTIES

Necip ŞİMŞEK<sup>1</sup>, Zhamile ASKEROVA<sup>2</sup>

<sup>1</sup>*Department of Mathematics, İstanbul Commerce University,  
İstanbul/TURKEY*

[necsimsek@yahoo.com](mailto:necsimsek@yahoo.com)

<sup>2</sup>*Department of Mathematics, Institute of Science, İstanbul Commerce University,  
İstanbul/TURKEY*

[cemile05@mail.ru](mailto:cemile05@mail.ru)

**Abstract:** In this paper, we study some geometric properties in some Banach spaces. We construct tensor product of some Banach spaces and investigate of some geometric properties.

**Keywords:** Tensor products, geometrical properties, Banach space.

### References:

- [1] A. Arias, J.D. Farmer, "On the structure of tensor products of  $\ell_p$  spaces", Pacific Journal of Math, 175(1), 1996.
- [2] Q. Bu, Y. Li, "Copies of  $\ell_1$  in positive tensor products of Orlicz sequence spaces", Quaestiones Mathematicae, 34(2011), 407-415.
- [3] Şimşek, N., Karakaya V., On some geometrical properties of generalized modular spaces of Cesaro type defined by weighted mean, Journal of Inequalities and Applications , Vol. 2009, Issue 932734, pp. 1-13, (2009).
- [4] Şimşek N, Savaş E., Karakaya, V., Some geometric and topological properties of a new sequence space defined by de la vale pousson means, Journal of Computational Analysis and Applications , Vol. 12, Issue 4, pp. 768-779, (2010)

## AVERAGE VECTOR FIELD METHOD AND CAPUTO FRACTIONAL DERIVATIVE DEFINITION FOR LINEAR FRACTIONAL SCHRÖDINGER EQUATION

Neslihan Fatma Er, Canan Akkoyunlu, Hikmet Çağlar

*Istanbul Kültür University, Mathematics-Computer Department, 34156  
İstanbul/TURKEY  
nf.er@iku.edu.tr  
c.kaya@iku.edu.tr  
s.caglar@iku.edu.tr*

**Abstract:** In this study, linear fractional Schrödinger equation with its initial and boundary conditions is studied by using Average Field Vector (AVF) method. Caputo fractional derivative definition is applied to the fractional part of the equation to express it with integer order of derivatives. In the solution of the problem, finite differences discretization along the spatial coordinate and AVF method along the time coordinate have been applied. Dispersion analysis is applied to ensure consistency and convergency of the method used. The result shows that the applied method in this study is an applicable technique.

**Keywords:** Linear fractional Schrödinger equation, Caputo fractional derivative definition, average vector field method, dispersion analysis.

### References:

- [1] Egen, T., Karaszen, B., Poisson Integrators for Volterra-Lattice Equations, 165 Applied Numerical Mathematics, (2006), 56, 879-887.
- [2] Cellodoni, E., Grimm, V., McLachlan, D.I., O'Neale, D.R.J., Quispel, G.R.W., Preserving Energy Resp. Dissipation in Numerical PDEs, Using the Average Vector Field Method, Journal of Computational Physics, (2009), 6770-6789.
- [3] Cieslinski, J.L., Improving the Accuracy of the AVF Method, Journal of Computational and Applied Mathematics, (2014), 259, 233-243.
- [4] Egen, T., Karaszen, B., Poisson Integrators for Volterra-Lattice Equations, 165 Applied Numerical Mathematics, (2006), 56, 879-887



## SOME CONTRACTIONS AND FIXED POINT THEOREMS IN MODULAR METRIC SPACES

Duran TÜRKOĞLU<sup>1</sup>, Nesrin MANAV<sup>2</sup>

<sup>1</sup>Department of Mathematics, Gazi University,  
Ankara/TURKEY

[dturkoglu@gazi.edu.tr](mailto:dturkoglu@gazi.edu.tr)

<sup>2</sup>Department of Mathematics, Erzincan University,  
Erzincan/TURKEY

[nesrinmanav2@gmail.com](mailto:nesrinmanav2@gmail.com)

**Abstract:** We introduce some properties in modular metric spaces, then show that some contractions and fixed point theorems in this modular metric spaces. Moreover, we show that type of modular metric spaces are useful. Finally, some given examples will be helpful to understand this construction.

**Keywords:** modular metric spaces, fixed point theorem, contractions.

### References:

- [1] Abdou, Afrah A. N.; Khamsi, Mohamed A. On common fixed points in modular vector spaces, *Fixed Point Theory Appl.* 2015, 2015:229, 9 pp.
- [2] Chistyakov, V. V. Fixed points of modular contractive mappings. (Russian) *Dokl. Akad. Nauk* 445 (2012), no. 3, 274--277; translation in *Dokl. Math.* 86 (2012), no. 1, 515--518
- [3] Chistyakov, V. V. Metric modulars and their application. (Russian) *Dokl. Akad. Nauk* 406 (2006), no. 2, 165--168.
- [4] Cho, Yeol J. E.; Saadati, Reza; Sadeghi, Ghadir, Quasi-contractive mappings in modular metric spaces. *J. Appl. Math.* 2012, Art. ID 907951, 5 pp.
- [5] Khamsi, M. A. Generalized metric spaces: a survey. *J. Fixed Point Theory Appl.* 17 (2015), no. 3, 455--475.
- [6] Jleli, Mohamed; Samet, Bessem, A generalized metric space and related fixed point theorems. *Fixed Point Theory Appl.* 2015, 2015:61, 14 pp.

## ALGORITHM FOR ZEROS OF MAXIMAL MONOTONE MAPPINGS IN CLASSICAL BANACH SPACES

A. H. ADOUM, O. DIOP, M. SENE AND N. DJITTE

*Department of Mathematics, Gaston Berger University,  
St Louis/Senegal*  
[ngalla.djitte@ugb.edu.sn](mailto:ngalla.djitte@ugb.edu.sn)

**Abstract:** In this presentation, we introduce a new iteration process and show that this iteration process converges strongly to a zeros of a bounded maximal monotone operator defined in a 2-uniformly convex and q-uniformly smooth or p-uniformly convex and 2-uniformly smooth real Banach space. Using this result, we deal with the convex minimization problem. Our theorems improve and unify most of the results that have been proved in this direction for this important class of nonlinear mappings. Furthermore, our new technique of proof is of independent interest.

**Keywords:** monotone mappings, zeros, iteration process

### References:

- [1] C.E. Chidume, N. Djitte, M sene, terative algorithm for zeros of multivaluedaccretive operators in certain Banach spaces, Afr. Mat. 26 (2015), no. 3-4, 357-368.
- [2] S. Kamimura and W. Takahashi, Approximating solutions of maximal monotone operators in Hilbert spaces, Journal of ApproximationTheory, vol. 106 (2000), no. 2, pp. 226-240.
- [3] H. Zegeye, Strong convergence theorems for maximal monotone mappings in Banach spaces, J. Math. Anal. Appl.,343 (2008) 663-671.

## SPECTRAL ANALYSIS OF MATRIX STURM-LIOUVILLE OPERATORS

Nihal YOKUS<sup>1</sup>, Nimet COSKUN<sup>2</sup>

<sup>1</sup>*Department of Mathematics, Karamanoglu Mehmetbey University,  
Karaman/TURKEY  
[nyokus@kmu.edu.tr](mailto:nyokus@kmu.edu.tr)*

<sup>2</sup>*Department of Mathematics, Karamanoglu Mehmetbey University,  
Karaman/TURKEY  
[cannimet@kmu.edu.tr](mailto:cannimet@kmu.edu.tr)*

**Abstract:** In this presentation, we introduce a boundary value problem (BVP) consisting of a second order non-selfadjoint matrix Sturm-Liouville equation and boundary conditions that depend on quadratic eigenvalue parameter.

**Keywords:** Eigenvalues, spectral singularities, spectral analysis, Sturm-Liouville operator.

### References:

- [1] M. A. Naimark, Investigation of the spectrum and the expansion in eigenfunctions of a non-selfadjoint operator of second order on a semi-axis, AMS Transl., 2 (16) (1960), 103-193.
- [2] F. Gesztesy, A. Kiselev and K.A. Makarov, Uniqueness results for matrix-valued Schrödinger, Jacobi and Dirac-type operators, Math. Nachr., 239 (2002) 103-145.
- [3] E. Bairamov and N. Yokus, Spectral singularities of Sturm-Liouville problems with eigenvalue-dependent boundary conditions, Abstract and Applied Analysis, 2009 (2009) 1-8.
- [4] T. Koprubasi and N. Yokus, Quadratic eigenparameter dependent discrete Sturm-Liouville equations with spectral singularities, Appl. Math. Comput., 244 (2014) 57-62..

## NEW RESULTS ON GRAPH PRODUCT OF SPECIAL SEMIGROUPS

Nihat AKGÜNEŞ

*Department of Mathematics-Computer Sciences, Necmettin Erbakan University,  
Meram, Konya/Turkey*  
[nakgunes@konya.edu.tr](mailto:nakgunes@konya.edu.tr)

**Abstract:** In this presentation, we introduce a new results for a important graph product over special semigroups. In detail, we will investigate some graph parameters and some graph numbers for that product of any two monogenic semigroup graphs  $\Gamma_1(S_M)$  and  $\Gamma_2(S_M)$ .

**Keywords:** Graphs, Graph product, Monogenic semigroup graph.

### References:

- [1] K. C. Das, N. Akgunes, A. S. Cevik, "On a graph of monogenic semigroup", Journal of Inequalities and Applications. 2013:44, 2013.
- [2] N. Akgunes, K. Ch. Das, A. S. Cevik, "Topological indices on a graph of monogenic semigroups", Topics in Chemical Graph Theory. Topics in Chemical Graph Theory, Mathematical Chemistry Monographs, University of Kragujevac and Faculty of Science Kragujevac, Kragujevac, (2014), No.16a, 1-21..

## PRINCIPAL FUNCTIONS OF DISCRETE STURM-LIOUVILLE EQUATIONS WITH HYPERBOLIC EIGENPARAMETER

Nihal YOKUS<sup>1</sup>, Nimet COSKUN<sup>2</sup>

<sup>1</sup>*Department of Mathematics, Karamanoglu Mehmetbey University,  
Karaman/TURKEY*

[nyokus@kmu.edu.tr](mailto:nyokus@kmu.edu.tr)

<sup>2</sup>*Department of Mathematics, Karamanoglu Mehmetbey University,  
Karaman/TURKEY*

[cannimet@kmu.edu.tr](mailto:cannimet@kmu.edu.tr)

**Abstract:** In this study, we take under investigation principal functions corresponding to the eigenvalues and the spectral singularities of the boundary value problem (BVP)  $a_{n-1}y_{n-1} + b_n y_n + a_n y_{n+1} = \lambda y_n, n \in \mathbb{N}$  and  $(\gamma_0 + \gamma_1 \lambda)y_1 + (\beta_0 + \beta_1 \lambda)y_0 = 0$  where  $(a_n)$  and  $(b_n)$  are complex sequences,  $\lambda$  is a hyperbolic eigenparameter and  $\gamma_i, \beta_i \in \mathbb{C}$ , for  $i = 0, 1$ .

**Keywords:** Spectral analysis, spectral singularities, eigenvalues, discrete equations.

### References:

- [1] M. Adıvar, E. Bairamov "Spectral properties of non-selfadjoint difference operators", J. Math. Anal. Appl., 261 (2014), 461-478.
- [2] M. A. Naimark, "Linear differential operators 2", Ungar, New York, (1968).
- [3] M. Olgun, T. Koprubasi, Y. Aygar, "Principle functions of non-selfadjoint difference operator with spectral parameter in boundary conditions", Abstract and Applied Analysis, Article ID 608329 (2011).
- [4] G. S. Guseinov, "The inverse problem of scattering theory for a second order difference equation on the whole axis", Doklady Akademii Nauk SSSR, 17(1976), 1684-1688.

## WIJSMAN $I$ -INVARIANT CONVERGENCE OF SEQUENCES OF SETS

Nimet PANCAROĞLU AKIN<sup>1</sup>, Erdiñ DÜNDAR<sup>1</sup> and Fatih NURAY<sup>1</sup>

<sup>1</sup>*Department of Mathematics, AfyonKocatepe University,  
Afyonkarahisar/TURKEY*

[npancaroglu@aku.edu.tr](mailto:npancaroglu@aku.edu.tr), [edundar@aku.edu.tr](mailto:edundar@aku.edu.tr), [fnuray@aku.edu.tr](mailto:fnuray@aku.edu.tr)

**Abstract:** In this paper, we study the concepts of Wijsman/ $I$ -invariant convergence ( $I_\sigma^W$ ), Wijsman  $I^*$ -invariant convergence ( $I_\sigma^{*W}$ ), Wijsman  $p$ -strongly invariant convergence ( $[WV_\sigma]_p$ ) and investigate the relationships among Wijsman invariant convergence, ( $[WV_\sigma]_p$ ), ( $I_\sigma^W$ ) and ( $I_\sigma^{*W}$ ). Also, we introduce the concepts of ( $I_\sigma^W$ )-Cauchy sequence and ( $I_\sigma^{*W}$ )-Cauchy sequence of sets.

**Keywords:** Invariant,  $I$ -convergence, Wijsman convergence.

## ON NEW FIXED POINTS THEOREMS FOR SET CONTRACTION MULTIVALUED MAPPINGS AND APPLICATIONS TO DIFFERENTIAL INCLUSIONS

Nour El Houda BOUZARA<sup>1</sup>, Vatan KARAKAYA<sup>2</sup>

<sup>1</sup>*Department of Mathematics, Yıldız Technical University,  
Istanbul/TURKEY*

[bzr.nour@gmail.com](mailto:bzr.nour@gmail.com)

<sup>2</sup>*Department of Mathematical Engineering, Yıldız Technical University,  
Istanbul/TURKEY*

[vkkaya@yahoo.com](mailto:vkkaya@yahoo.com)

**Abstract:** In this work, combining the concept of measure of noncompactness with fixed point theory for multivalued mappings, we present new existence theorems for different type of set contraction multivalued maps. We also introduce a new class of mappings which are general than Meir-Keeler mappings. Finally, we use these results are then used to investigate the existence of mild solutions for a nonlocal evolution differential inclusion without the compactness assumption.

**Keywords:** Multivalued mappings; Measure of noncompactness; fixed points; evolution differential inclusion.

### References:

- [1] C. Dhage, Some Generalizations of Mult-Valued Version of Schauder's Fixed Point Theorem with Applications, CUBO, Vol.12, No 03, 139.151 (2010)

## APPLYING POWELL'S SYMMETRICAL TECHNIQUE TO CONJUGATE GRADIENT METHODS WITH THE GENERALIZED CONJUGACY CONDITION

Noureddine BENRABIA

noureddinebenrabia@yahoo.fr

**Abstract:** A new conjugate gradient method for unconstrained optimization, is proposed by applying the Powell symmetrical technique in a sense to be defined. Using the Wolfe line search conditions, the global convergence property of the method is also obtained, on the basis of the spectral analysis of the conjugate gradient iteration matrix and the Zoutendijk's condition for steepest descent methods. Preliminary numerical results for a set of 86 unconstrained optimization test problems, verify the performance of the algorithm and show that the GDSHS1 algorithm is competitive with the FR and  $\square+$  algorithms.

**Keywords:** Conjugate gradient method, symmetrical technique, Generalized conjugacy condition, spectral analysis, global convergence.

### References:

- [1] M. Adivar, E. Bairamov "Spectral properties of non-selfadjoint difference operators", J. Math. Anal. Appl., 261 (2014), 461-478.
- [2] Al-Baali, M., *Descent property and global convergence of the FletcherReeves method with inexact line-search*, IMA J. Numer. Anal. 5, 121-124 (1985).
- [3] Liu, D., Xu, G., *Applying Powells symmetrical technique to conjugate gradient methods*, C1007/s10589-009-9302-1. (2009).omputational Optimization and Applications, DOI
- [4] Perry, A., *A modified conjugate gradient algorithm*, Oper. Res. Tech.Notes 26(6), 1073–1078 (1978).
- [5] Hestenes, M. R., Stiefel, E., *Methods of conjugate gradients for solving linear systems*, J. Res. Nat. Bur. Stand. 49(6), 409-439 (1952).
- [6] Dai, Y.H., Liao, L. Z., *An efficient hybrid conjugate gradient method for unconstrained optimization*, Ann. Oper. Res., 103 (2001) 33-47.

## CONVERGENCE OF SPLIT-STEP FOURIER COLLOCATION METHOD FOR BENJAMIN-BONA- MAHONY TYPE EQUATIONS

Nurcan GÜCÜYENEN

nurcangucuyenen@gmail.com

**Abstract:** In this paper, we study stability, consistency and the convergence analysis of fully discretized Benjamin-Bona-Mahony (BBM) equations of the type  $u_t - \partial_x^2 u_t = Au + \frac{1}{2} \partial_x (u^2)$ , where  $A$  is an unbounded linear differential operator. In paper [1], a third order local and a second order global error bounds for the same problem is obtained in time using Strang splitting. Here, we study on fully discretized solution with Strang splitting in time and Fourier collocation in space under suitable regularity assumptions on exact solution. First we prove stability and construct a local error bound via Fourier interpolation operator and time discretization error. Then with the help of Lady Windermere's fan argument, we obtained a fully discretized global error bound. Finally the results are tested on a numerical example.

**Keywords:** Operator splitting method, Fourier collocation method, Nonlinear Partial differential equation, KdV-BBM equation, error bound.

### References:

- [1] N. Gücüyenen, "Strang splitting method to Benjamin Bona Mahony type equations: Analysis and application", Journal of Computational and Applied Mathematics, DOI:10.1016/j.cam.2015.11.015.
- [2] L. Gauckler, "Convergence of a split Hermite method for the Gross-Pitaevskii equation", IMA journal of Numerical Analysis, 31(2011), 396-415.
- [3] E. Faou, "Geometric numerical integration and Schrödinger Equations", European Mathematical Society, (2012).
- [4] C. Lubich, "From quantum to classical molecular dynamics: Reduced models and numerical analysis", European Mathematical Society, (2008).



## HERMIT-HADAMARD TYPE INEQUALITIES FOR CO-ORDINATES LOG-CONVEX STOCHASTIC PROCESSES

Nurgül OKUR BEKAR

*Department of Statistics, Giresun University,  
Giresun/TURKEY  
[nrgokur@gmail.com](mailto:nrgokur@gmail.com)*

**Abstract:** The main aim of the present is to introduce co-ordinated log-convex stochastic processes. Moreover, we prove Hermit-Hadamard type inequalities for co-ordinated log-convex stochastic processes and obtain some important results for these processes.

**Keywords:** Hermit-Hadamard inequality, co-ordinated log-convex function, log-convex stochastic processes, co-ordinated log-convex stochastic processes

### References:

- [1] K. Nikodem, "On convex stochastic processes", *Aequationes Mathematicae*, 20(1980), 184-197.
- [2] M. Alomari, M. Darus. "On the Hadamard's inequality for log-convex functions on the coordinates." *Journal of Inequalities and Applications* 2009.1 (2009), 1-13.
- [3] M. Tomar, E. Set and N. O. Bekar, "On Hermite-Hadamard Type inequality for strongly log-convex stochastic processes", *Journal of Global Engineering Studies*, 1 (2) (2014), 53-61.
- [4] M. Tomar, E. Set and S. Maden, "On Hermite-Hadamard Type inequality log-convex stochastic processes", *New Theory*, 2 (2015), 23-32.
- [5] S.S. Dragomir, Refinements of the Hermite-Hadamard integral inequality for log-convex functions, *RGMI Res. Rep. Collect.* 3 (4) (2000), 527-533.

## A NEW SMOOTHING APPROXIMATION TO PIECEWISE SMOOTH FUNCTIONS AND APPLICATIONS

Nurullah YILMAZ<sup>1</sup>, Ahmet ŞAHİNER<sup>1</sup>

<sup>1</sup>*Department of Mathematics, SuleymanDemirelUniversity,  
Isparta/TURKEY*

[nurullahyilmaz@sdu.edu.tr](mailto:nurullahyilmaz@sdu.edu.tr), [ahmetnur32@gmail.com](mailto:ahmetnur32@gmail.com)

**Abstract:** In this study, we introduce smoothing approximations for piecewise smooth functions. First, we give a new definition for piecewise smooth functions. Second, present a new local smoothing approximation for both one dimensional and n-dimensional piecewise functions. Third, we apply our smoothing approach three important area such as optimization, data modeling and geometric design. We give some numerical examples in order to illustrate the efficiency of our method.

**Keywords:** Piecewise smooth function, Smoothing approximation, Optimization,

### References:

- [1] L. Qi, P. Tseng, On almost smooth functions and piecewise smooth functions, *Nonlinear Anal.* (2007) 67: 773--794.
- [2] R.T. Rockafellar, A property of piecewise smooth functions, *Comput. Optim. Appl.* (2003) 25: 247--250.
- [3] H. Wu, P. Zhang, G.-H. Lin, Smoothing approximations for some piecewise smooth functions, *J. Oper. Res. Soc. China* (2015) 3:317--329.
- [4] X. Chen, Smoothing Methods for nonsmooth, nonconvex minimization, *Math. Program. Serie B*, (2012) 134:71--99.
- [5] A. Mozroui, D. Sbibi, A. Tijini, A simple method for smoothing functions and compressing hermite data, *Adv. Comput. Math.* (2005) 23: 279--297.
- [6] J. Cheng, X-S. Gao, Constructing blending surfaces for two arbitrary surfaces, *MM Research Preprints*, (2003) 22: 14:28.

## ON THE A FAMILY SAVING MODEL

Olgun CABRİ<sup>1</sup>, Khanlar R. MAMEDOV<sup>2</sup>

<sup>1</sup>*Department of Business Administration, Artvin Çoruh University,  
Artvin/TURKEY*  
[olguncabri@artvin.edu.tr](mailto:olguncabri@artvin.edu.tr)

<sup>2</sup>*Department of Mathematics, Mersin University,  
Mersin/TURKEY*  
[hanlarm@yahoo.com](mailto:hanlarm@yahoo.com)

**Abstract:** In this study, we are interested in the family saving model for a family sets which is given by Kolmogorov equation

$$\frac{\partial u}{\partial t} = -\frac{\partial}{\partial x}(Cu) + \frac{1}{2} \frac{\partial^2}{\partial x^2}(bu) + f$$

where  $u = u(x, t)$  is density distribution of family saving. Nonlocal boundary conditions which describes total family saving and number of families on the definite interval are considered for the model. By the Fourier method, solution of the problem is examined. In addition, Method of Lines method and Crank Nicolson method are applied to family saving model with integral boundary conditions. Errors of numerical methods are presented.

**Keywords:** Sturm-Liouville problem, nonlocal boundary conditions, family saving model, method of lines, Crank Nicolson method

### References:

- [1] Cannon.J.R, "The solution of the heat equation subject to specification of energy", Quarterly of Applied Mathematics, 21(1963),155-160
- [2] Ionkin. N.I, "Solution of a boundary value problem in heat conduction with a nonclassical boundary condition", Differential Equations, 13(1977),204-211

## CONVERGENCE ANALYSIS OF DIFFERENCE METHOD FOR VOLTERRA DELAY-INTEGRO-DIFFERENTIAL EQUATION

Gabil M. AMIRALIYEV<sup>1</sup>, Ömer YAPMAN<sup>2</sup>

<sup>1</sup>*Department of Mathematics, Faculty of Arts and Sciences, Erzincan University,  
Erzincan/TURKEY*

[gabilamirali@yahoo.com](mailto:gabilamirali@yahoo.com)

<sup>2</sup>*Department of Mathematics, Faculty of Arts and Sciences, Erzincan University,  
Erzincan/TURKEY*

[yapmanomer@gmail.com](mailto:yapmanomer@gmail.com)

**Abstract:** This study is concerned with the finite-difference solution of singularly perturbed initial value problem for a linear first order Volterra integro-differential equation with delay. The method is based on the method of integral identities with the use of exponential basis functions and interpolating quadrature rules with the weight and remainder terms in integral form. The emphasis is on the convergence of numerical method. It is shown that the method displays uniform convergence in respect to the perturbation parameter. Numerical results are also given.

**Keywords:** Delay-integro-differential, delay difference scheme, uniform convergence, singular perturbation.

**MSC:** 65L11, 65L12, 65L20, 65R05, 65R20.

### References:

- [1] G. Amiraliyev, B. Yilmaz, "Fitted Difference Method for a Singularly Perturbed Initial Value Problem", *International Journal of Mathematics and Computation*, 22(2014), 1-10.

## A GENERALIZATION OF THE EXPONENTIAL AND LINDLEY DISTRIBUTIONS VIA THE KUMARASWAMY-G FAMILY

OrhanMazlum YAZAR<sup>1</sup>, Mustafa Ç. KORKMAZ<sup>2</sup>

<sup>1</sup>Science InstituteMSc.,RecepTayyipErdoğanUniversity,  
Rize/TURKEY

[o.m.yazar@artvin.edu.tr](mailto:o.m.yazar@artvin.edu.tr)

<sup>2</sup>Department of Educational Sciences,ArtvinÇoruh University,Artvin/TURKEY

[mcagatay@artvin.edu.tr](mailto:mcagatay@artvin.edu.tr)

**Abstract:** In this study, we introduce a new generalization of the exponential and Lindley distribution via Kumaraswamy-G family of the distribution. The new distribution has the following cumulative distribution function,

$$F(x, a, b, \alpha, \beta) = 1 - \left( 1 - \left[ 1 - \frac{(\alpha + \beta + \alpha\beta x)e^{-\alpha x}}{\alpha + \beta} \right]^a \right)^b, x > 0,$$

where  $a, b, \alpha, \beta > 0$ . Furthermore, we obtain several properties of this new distribution such as special cases and its density shapes, hazard rate function, moments, maximum likelihood estimations. Finally we end the paper with data analysis and conclusions.

**Keywords:** extended exponential distribution, Lindley distribution, Kumaraswamy-G family, generalized distribution.

### References:

- [1] G.M. Cordeiro, M. de Castro, "A new family of generalized distributions", Journal of Stat. Comput. and Simul., 81(2011), 883–893.
- [2] S. Çakmakyapan, G. Ö. Kadılar, "A New Customer Lifetime Duration Distribution: The Kumaraswamy Lindley Distribution", Inter. J. Trade, Economics and Finance, 5(2014), 441-444.
- [3] Y. M. Gomez, H. Bolfarine, H.W. Gomez, "A New Extension of the Exponential Distribution", Revista Colombiana de Estadística, 37(2014), 25-34.

## CONVERGENCE THEOREMS FOR A FAMILY OF MULTIVALUED NONEXPANSIVE MAPPINGS IN HYPERBOLIC SPACES

Osman ALAGÖZ<sup>1</sup>, Birol GÜNDÜZ<sup>2</sup>, Sezgin AKBULUT<sup>3</sup>

<sup>1</sup>*Department of Mathematics, BilecikŞeyhEdebali University,  
Bilecik/TURKEY*

[osman.alagoz@bilecik.edu.tr](mailto:osman.alagoz@bilecik.edu.tr)

<sup>2</sup>*Department of Mathematics, Erzincan University,  
Erzincan/TURKEY*

[birolgndz@gmail.com](mailto:birolgndz@gmail.com)

<sup>3</sup>*Department of Mathematics, Atatürk University,  
Erzurum/TURKEY*

[sezginakbulut@gmail.com](mailto:sezginakbulut@gmail.com)

**Abstract:** In this article we introduce a new iteration process inspired by the iteration [1] to prove strong convergence and  $\Delta$ -convergence for a finite family of nonexpansive multivalued mappings in hyperbolic spaces. The results presented here extend some existing results in the literature.

**Keywords:** Hyperbolic spaces,  $\Delta$ -convergence, nonexpansive multivalued mapping.

### References:

- [1] B. Gunduz and S. Akbulut, Strong convergence of an explicit iteration process for a finite family of asymptotically quasi-nonexpansive mappings in convex metric spaces, *Miskolc Mathematical Notes*, Vol. 14 (2013), No. 3, pp. 905-913
- [2] A. Kettapun et al. A new approximation method for common fixed points of a finite family of asymptotically quasi-nonexpansive mappings in Banach spaces, *Computers and Mathematics with Applications* 60 (2010) 1430-1439.

## COMPLETE ABSTRACT DIFFERENTIAL EQUATIONS OF ELLIPTIC TYPE WITH ROBIN'S CONDITION IN A NON-COMMUTATIVE FRAMEWORK

Ould Melha KHELLAF<sup>1</sup>, Mustapha CHEGGAG<sup>2</sup>, Stéphane MAINGOT<sup>3</sup> and Rabah LABBAS<sup>3</sup>.

<sup>1</sup>*Department of Mathematics, Chlef University.  
ould\_melha\_khel@yahoo.fr*

<sup>2</sup>*Department of Mathematics and Computer Sciences,  
Polytechnic National School of Oran, Algeria  
mustapha.cheggag@enp-oran.dz*

<sup>3</sup>*Laboratoire de Mathématiques Appliquées, Université du Havre, France.  
[Stephane.maingot@univ-lehavre.fr](mailto:Stephane.maingot@univ-lehavre.fr), [rabah.labbas@univ-lehavre.fr](mailto:rabah.labbas@univ-lehavre.fr)*

**Abstract:** In this work we give some new results on Robin abstract problem of second order differential equations of elliptic type with coefficient-operator in a non-commutative framework. We study the case  $f \in L_p(0,1;X)$ ,  $1 < p < \infty$  with  $X$  is UMD Banach spaces, using the representation formula of the solution given in M. Cheggag et al. [4]. Necessary and sufficient conditions of compatibility are established to obtain a strict solution. This work completes the ones studied by M. Cheggag et al. [4] and [5].

**Keywords:** Abstract differential equations, Robin boundary conditions, fractional powers of operators, bounded imaginary powers, analytic semigroups theory, UMD space, non-commutativity.

### References:

- [1] M. Cheggag, A. Favini, R. Labbas, S. Maingot, A. Medeghri. Sturm-Liouville Problems for an Abstract Differential Equation of Elliptic Type in UMD Spaces, *Differential and Integral Equations*, Vol. 21, 9-10, (2008), 981-1000.
- [2] M. Cheggag, A. Favini, R. Labbas, S. Maingot, A. Medeghri. Complete Abstract Differential Equations of Elliptic Type with General Robin Boundary Conditions in UMD Spaces, *DCDS-S*, 4, no. 3 (2011), 1-16.
- [3] M. Cheggag, A. Favini, R. Labbas, S. Maingot, M. Medeghri: Elliptic Problems with Robin Boundary Coefficient-Operator Conditions in General  $L_p$  Sobolev Spaces and Applications. *Bulletin of the South Ural State University. Ser. Mathematical Modelling, Programming & Computer Software (Bulletin SUSU MMCS)*, 2015, vol. 8, no. 3, pp. 56-77.

## EXTREMAL FUNCTIONS FOR STARLIKE FUNCTIONS AND CONVEX FUNCTIONS

İsmet YILDIZ<sup>1</sup>, Neslihan ZORLU<sup>2</sup>, Oya MERT<sup>3</sup>

<sup>1</sup>*Department of Mathematics, Düzce University,  
Düzce/TURKEY*

[ismetyildiz@duzce.edu.tr](mailto:ismetyildiz@duzce.edu.tr)

<sup>2</sup>*Department of Mathematics, Düzce University,  
Düzce/TURKEY*

[neslihn.zrl@gmail.com](mailto:neslihn.zrl@gmail.com)

<sup>3</sup>*Department of Mechanical Engineering, Kemerburgaz University,  
İstanbul/TURKEY*

[oya.mert@kemerburgaz.edu.tr](mailto:oya.mert@kemerburgaz.edu.tr)

**Abstract:** In this paper, we obtain new extremal functions for starlike functions and convex functions on the range  $0 \leq \alpha \leq \frac{1}{2r+1}$ , defined on the unit disk using analytic and univalent functions.

**Keywords:** Starlike functions, convex functions, analytic functions, extremal function.

### References:

- [1] M. Nunokawa, M. Aydoğan, K. Kuroki, I. Yildiz, S. Owa, "On the order of close-to-convexity of convex functions of order alpha", *Journal of Inequalities and Applications* 2012, 2012:245 doi:10.1186/1029-242X-2012-245.
- [2] C. Carathéodory, *Mathematische Annalen*, - Springer., 64(1907), 95-115.
- [3] P. L. Duren., 1. *Univalent Functions.*, I. Title., II Series. QA331.D96 1983 515.9
- [4] K. Kuroki, S. Owa and I. Yildiz "On starlikeness of confluent hypergeometric functions" *International Journal of Applied Mathematics*, Volume 25 No. 4 2012, 583-589.
- [5] M.S. Robertson, "On the Theory of Univalent Functions", *Ann. of Math.*, 37(1936), 374-408.



## DYNAMIC SEMI-DISCRETE SURFACES OF REVOLUTION

Sibel PAŞALI ATMACA<sup>1</sup>, Ömer AKGÜLLER<sup>2</sup>, Emel KARACA<sup>3</sup>

<sup>1,2,3</sup>*Department of Mathematics, Muğla Sıtkı Koçman University,  
Muğla/TURKEY*

[sibela@mu.edu.tr](mailto:sibela@mu.edu.tr), [oakguller@mu.edu.tr](mailto:oakguller@mu.edu.tr), [emelkcaraca@gmail.com](mailto:emelkcaraca@gmail.com)

**Abstract:** Discrete Differential Geometry considers all kinds of discrete objects such as polygons, polyhedral surfaces etc. and has a long range of applications in many areas. One kind of manifolds arise from this subject are bivariate function of one discrete and one continuous variable, so called semi-discrete surfaces. Such mixed continuous-discrete objects can be seen as a limit case of purely discrete surfaces, or as a semi-discretization of smooth surfaces. Rather than the constant step discretization methods, Time Scales Calculus can also be effective to discretize smooth surfaces, since they directly converge to smooth part of the underlying manifold. Besides, with the chosen of discrete and continuous time scale, it is also possible to obtain local dynamic semi-discretization of smooth surface. In this study we briefly introduce such semi-discretization of smooth surfaces by using time scales calculus. Also semi-discrete surfaces are included and can be looked at in different ways- on the one hand as a discrete (or smooth) evolution of a curve from the point of view of transformations of curves, and on the other hand as approximation of a surface by a sequence of merged strips. The present study mainly investigates semi-discrete surfaces of revolution. We give some definitions of dynamic semi-discrete surface by using the Trigonometric functions on time scales. Also, we discuss basic theorems about the study.

**Keywords:** Semi-Discrete Surface, Discrete Differential Geometry, Time Scales Calculus, Mimetic Discretization

### References:

- [1] Atmaca, Sibel Paşalı, and Ömer Akgüller. "Surfaces on time scales and their metric properties." *Advances in Difference Equations* 2013, no. 1 (2013): 1-10.
- [2] Atmaca, Sibel Paşalı, and Ömer Akgüller. "Curvature of curves parameterized by a time scale." *Advances in Difference Equations* 2015, no. 1 (2015): 1-7.

## ON SOME PROPERTIES OF POISSON AND CAUCHY TYPE INTEGRALS IN WEIGHTED MORREY TYPE SPACES

Şeyma ÇETİN, Yusuf ZEREN

<sup>1</sup>Department of Mathematics, Yıldız Technical University,  
İstanbul/TURKEY

[seyymacetin@gmail.com](mailto:seyymacetin@gmail.com)

[yusufzeren@hotmail.com](mailto:yusufzeren@hotmail.com)

**Abstract:** In this work, we consider weighted form of Morrey-type spaces and some properties of shift operator in weighted Morrey-type spaces. We established some analogues of classical results in this case.

**Keywords:** Morrey-type spaces, weighted Morrey-type spaces, Poisson Integral, Cauchy Integral

### References:

- [1] Peetre J. On the theory of  $L^{p,\lambda}$  spaces, J. Funct. Anal., 1964, 4, pp.71-87
- [2] Zorko C.T. Morrey space, Proc. of the Amer. Math. Society, 1986, v.98, is.4, pp. 586-592
- [3] Samko N. Weight Hardy and singular operators in Morrey spaces, Journal of Mathematical Analysis and Application, 2009, 35(1), pp.183-188
- [4] Bilalov B.T., Guliyeva A.A. On basicity of exponential systems in Morrey type spaces, International Journal of Mathematics, Vol. 25, No. 6 (2014), pp.1-10
- [5] Bilal Bilalov, Telman Gasymov, Aida Guliyeva On Solvability of Riemann boundary value problem in Morrey-Hardy classes
- [6] Israfilov D.M., Tozman N.P. Approximation by polynomials in Morrey-Smirnov classes, East J. Approx., 2008, v.14(3), pp.255-269

## ON $I_2$ -ASYMPTOTICALLY $\lambda^2$ -STATISTICAL EQUIVALENT DOUBLE SET SEQUENCES

Ömer KİŞİ, Semra SARAÇOĞLU ÇELİK, Erhan GÜLER

*Faculty of Science, Department of Mathematics,  
Bartın, Turkey*

[okisi@bartin.edu.tr](mailto:okisi@bartin.edu.tr), [ssaracoglu@bartin.edu.tr](mailto:ssaracoglu@bartin.edu.tr), [erqler@gmail.com](mailto:erqler@gmail.com)

**Abstract:** In this paper, we introduce the concept of  $I_2$ -asymptotically  $\lambda^2$ -statistically equivalence of multiple  $L$  for the double sequences  $\{A_{\{k,l\}}\}$  and  $\{B_{\{k,l\}}\}$  Also we give some inclusion relations.

**Keywords:**  $I_2$ -convergence,  $\lambda^2$ -convergence, asymptotically equivalence, double sequences, set sequences.

### References:

- [1] M. Baronti, P. Papini, "Convergence of sequences of sets", In: Proceedings of methods of functional analysis in approximation theory, ISNM 76, Birkhauser, Basel, pp. 133-155 (1986).
- [2] G. Beer, "On convergence of closed sets in a metric space and distance", Bull Aust Math Soc 31:421-432 (1985).
- [3] Ö. Kişi, F. Nuray, "New convergence definitions for sequence of sets", Abstractand Applied Analysis Volume 2013, Article ID 852796 6 pages, (2013).
- [4] F. Nuray, B. E. Rhoades, "Statistical convergence of sequences of Sets", Fasciculi Mathematici 49, 87-99, (2012).

## ON THE ALMOST EVERYWHERE STATISTICAL CONVERGENCE OF SEQUENCES OF FUZZY NUMBERS

Özer TALO

*Department of Mathematics, Celal Bayar Universty,  
Manisa/TURKEY*

[ozertalo@cbu.edu.tr](mailto:ozertalo@cbu.edu.tr)

**Abstract:** In this paper, we define the concept of almost everywhere statistical convergence of a sequence of fuzzy numbers and prove that a sequence of fuzzy numbers is almost everywhere statistically convergent if and only if its statistical limit inferior and limit superior are equal. To achieve this result, new representations for statistical limit inferior and limit superior of a sequence of fuzzy numbers are obtained and we show that some properties of statistical limit inferior and limit superior can be easily derived using these representations.

**Keywords:** Sequence of fuzzy numbers, almost everywhere statistical convergence, statistical limit inferior, statistical limit superior.

## DYNAMICS OF A DISCRETE-TIME HOST PARASITOID

Özlem AK GÜMÜŞ

<sup>1</sup>*Department of Mathematics, Adiyaman University,  
Adiyaman/TURKEY  
[akgumus@adiyaman.edu.tr](mailto:akgumus@adiyaman.edu.tr)*

**Abstract:** In this presentation, we investigate the stability of the coexistence fixed point of a host parasitoid model with certain parameters.

**Keywords:** Host parasitoid model, stability analysis, fixed point.

### References:

- [1] A. Nicholson and V. Bailey, "The balance of animal population, 3, Proc. Zool. Soc. Lond.", 1935.
- [2] U. Ufuktepe, S. Kapçak, "Stability analysis of a host parasite model, Advances of Difference Equations", 79(2013), 2-7.
- [3] J.C. Misra, A. Mitra, "Instabilities in single-species and host-parasite systems: period-doubling bifurcations and chaos", Comput. Math. Appl. 52(2006), 525-538.
- [4] M.P. Hassell, H.N. Comins, "Discrete-time models for two species competition. Theor. Popul. Biol.", 9, (1976), 202-221.
- [5] J.R. Beddington, C. A. Free and J. H. Lawton, "Dynamic complexity in predator-prey models framed in difference equation", Nature 255(1975), 58-60.

## STABILITY BEHAVIOR OF A MODIFIED NICHOLSON-BAILEY MODEL

Özlem AK GÜMÜŞ

<sup>1</sup>*Department of Mathematics, Adiyaman University,  
Adiyaman/TURKEY*

[akgumus@adiyaman.edu.tr](mailto:akgumus@adiyaman.edu.tr)

**Abstract:** This study presents the dynamical results of the model by obtaining the fixed points existing in the host-parasitoid model. Also, the results are confirmed by the examples.

**Keywords:** Discrete-time system, Nicholson Bailey model, stability analysis, fixed point.

### References:

- [1] A. Nicholson and V. Bailey, "The balance of animal population", 3, Proc.Zool. Soc. Lond.", (1935).
- [2] Ö. Ak Gümüş, "Dynamical Consequences and Stability Analysis of a New Host-Parasitoid Model", General Mathematical Notes, No. 1, 27(2015),9-15.
- [3] L.J.S. Allen, "An Introduction to Mathematical Biology", Pearson, New Jersey", (2007).
- [4] Ö. Ak Gümüş, F. Kangalgil, "Allee effect and stability in a discrete-time host-parasitoid model", Journal of Advanced research in Applied Mathematics, Issue 1, 7(2015), 94 -99.
- [5] C. J. Pennycuik, R.M. Compton and A. Beckingham, "A Computer Model for Simulating the Growth of a Population, or of Two Interacting Populations", Journal of Theoretical Biology, 18(1968), 316-329.
- [6] U. Ufuktepe, S. Kapçak, "Stability analysis of a host parasite model, Advances of Difference Equations", 79(2013), 2-7.

## ON $p$ -ADIC GAMMA FUNCTION

Özge ÇOLAKOĞLU HAVARE, Hamza MENKEN

*Department of Mathematics, Mersin University,  
Mersin/TURKEY*

[ozgecolakoglu@mersin.edu.tr](mailto:ozgecolakoglu@mersin.edu.tr)

[hmenken@mersin.edu.tr](mailto:hmenken@mersin.edu.tr)

**Abstract:** In the present work, we consider  $p$ -adic gamma function. We obtain the derivative of the  $p$ -adic gamma function and Volkenborn integral of derivative of  $p$ -adic gamma function is obtained. Also, we compute value of the Volkenborn integral for Mahler base.

**Keywords:** Volkenborn integral,  $p$ -adic gamma function, Mahler coefficients.

### References:

- [1] A. Volkenborn, "Ein  $p$ -adisches Integral und seine Anwendunge I", *Manuscripta Math.*, 7-4(1972), 341-373.
- [2] A. Volkenborn, "Ein  $p$ -adisches Integral und seine Anwendunge II", *Manuscripta Math.*, 12(1974), 17-46.
- [3] D. Barsky, "On Morita's  $p$ -adic gamma function", *Grouped'Etuded'AnalyseUltramétrique*, 5e année (1977/78), *Secrétariat Math.*, Paris, Exp. No. 3(1978),6.
- [4] Y. Morita, "A  $p$ -adic analogue of the  $\Gamma$ -function", *J. Fac. Science Univ.*, Tokyo, 22(1975), 225-266.

## APPROXIMATION PROPERTIES OF KING TYPE(p,q)- BERNSTEIN OPERATORS

Özge DALMANOĞLU, Mediha ÖRKÇÜ

<sup>1</sup>*Department of Mathematics Education, Baskent University,  
Ankara/TURKEY*

*[ozgedalmanoglu@gmail.com](mailto:ozgedalmanoglu@gmail.com)*

<sup>2</sup>*Department of Mathematics, Gazi University, Ankara/TURKEY  
[medihaakcay@gazi.edu.tr](mailto:medihaakcay@gazi.edu.tr)*

**Abstract:** In this presentation we deal with a King type modification of (p,q)-Bernstein operators. We investigate the Korovkin type approximation of both (p,q)-Bernstein and King type (p,q)-Bernstein operators under different conditions from the previous works. We prove that the error estimation of King type of the operator is better than that of the classical one whenever  $0 \leq x \leq \frac{1}{3}$ .

**Keywords:** Korovkin theorem, (p,q) integers, (p,q)-Bernstein operators, King type operators, rate of convergence.

### References:

- [1] M. Mursaleen, K. J. Ansari, Asif Khan, On (p,q)-analogue of Bernstein operators, *Appl. Math. Comput.* 266 (2015) 874-882.
- [2] M. Mursaleen, Khursheed J. Ansari, Asif Khan, Erratum to "On (p,q) analogue of Bernstein Operators" [*Appl. Math. Comput.* 266 (2015) 874–882], *Appl. Math. Comput.* 278 (2016) 70–71.
- [3] Mursaleen, M., Khursheed J. Ansari, and Asif Khan. "Some approximation results by (p,q)-analogue of Bernstein--Stancu operators." *Applied Mathematics and Computation* 264 (2015): 392-402. [Corrigendum: *Appl. Math. Comput.* 269 (2015),744-746 ]
- [4] King, J. P., Positive Linear Operators which preserve  $x^2$ , *Acta Math. Hungari*, 99, (2003) 203-208.
- [5] Gupta, Vijay and Ali Aral "Bernstein Durrmeyer Operators Based on Two Parameters." *FactaUniversitatis, Series: Mathematics and Informatics* 31.1 (2016): 79-95.

## ON THE NUMERICAL SOLUTION OF THE KLEIN-GORDON EQUATION BY EXPONENTIAL B-SPLINE COLLOCATION METHOD

Özlem ERSOY HEPSON<sup>1</sup>, Alper KORKMAZ<sup>2</sup>, İdris DAĞ<sup>1</sup>

<sup>1</sup>*Department of Mathematics-Computer, EskişehirOsmangaziUniversity, Eskişehir/TURKEY*

[ozersoy@ogu.edu.tr](mailto:ozersoy@ogu.edu.tr)

<sup>2</sup>*Department of Mathematics, ÇankırıKaratekin University, Çankırı/TURKEY*

[akorkmaz@karatekin.edu.tr](mailto:akorkmaz@karatekin.edu.tr)

<sup>1</sup>*Department of Computer Engineering, EskişehirOsmangaziUniversity, Eskişehir/TURKEY*

[idağ@ogu.edu.tr](mailto:idağ@ogu.edu.tr)

**Abstract:** A finite element collocation method based on exponential-type cubic B-spline functions is formulated for the numerical solutions some initial boundary value problems constructed on the Klein-Gordon equation. The time order of the equation is reduced to convert the equation to a coupled system of equations of order one in time. The time discretization of the resultant system is accomplished by the Crank-Nicolson method. Then, following the linearization of the nonlinear terms, the space discretization is completed using exponential cubic B-spline collocation method. Finally, balancing the initial state makes the iteration algorithm ready to run. Some problems are solved by using the proposed algorithm. The error between the exact and approximate solutions is measured by using various discrete norms in some distinct steps. The plots of the obtained numerical solutions are also depicted to examine the motion.

**Keywords:** Finite element method, collocation method, Klein-Gordon equation, Exponential cubic B-spline.

### References:

- [1] B. J. McCartin, "Theory of Exponential Splines", Journal of Approximation Theory, 66(1991), 1.
- [2] O. Ersoy, İ. Dağ, "Numerical solutions of the reaction diffusion system by using exponential cubic B-spline collocation algorithms", Open Physics, 13 (2015), 414
- [3] İ. Dağ, O. Ersoy, "The exponential cubic B-Spline algorithm for Fisher equation", Chaos Solitons&Fractals, 86(2016), 101.



## SOLVING LINEAR FRACTIONAL EQUATIONS WITH CONSTANT COEFFICIENTS USING LAPLACE TRANSFORM METHOD UNDER CTIT TRANSFORMATION

Özlem ÖZTÜRK MIZRAK<sup>1</sup>, Nuri ÖZALP<sup>2</sup>

<sup>1</sup>*Department of Mathematics, Ankara University,  
Ankara/TURKEY*

[oomizrak@ankara.edu.tr](mailto:oomizrak@ankara.edu.tr)

<sup>2</sup>*Department of Mathematics, Ankara University, Ankara/TURKEY*  
[nozalp@science.ankara.edu.tr](mailto:nozalp@science.ankara.edu.tr)

**Abstract:** We propose an adapted Laplace transform method using cosmic time-individual time (CTIT) transformation which enables to reduce the problem of finding a solution for a linear fractional differential equation in fractional domain to a problem in ordinary domain and provide estimates for accuracy of the computations with comparative graphs showing the behaviour of the solutions.

**Keywords:** Laplace transform, CTIT transformation, linear fractional differential equation, fractional domain, ordinary domain.

### References:

- [1] I. Podlubny, Geometric and physical interpretation of fractional integration and fractional differentiation, *Fractional Calculus and Applied Analysis* 5 (4) (2002) 367–386.
- [2] E. Demirci, N. Özalp, A method for solving differential equations of fractional order, *J. Comput. Appl. Math.* 236, 2754-2762 (2012).
- [3] A.A. Kilbas, H.M. Srivastava, J.J. Trujillo, *Theory and Applications of Fractional Differential Equations*, Elsevier, Amsterdam, 2006.

**THE SPACE  $W(L^{p(\cdot),q(\cdot)}, L^r_\omega)$  AND BOUNDEDNESS OF THE  
HARDY-LITTLEWOOD MAXIMAL FUNCTION ON  
 $W(L^{p(\cdot),q(\cdot)}, L^r_\omega)$**

Öznur KULAK<sup>1</sup>, A. TuranGÜRKANLI<sup>2</sup>

<sup>1</sup>*Department of Banking and Finance, Giresun University,  
GiresunTURKEY*

[oznur.kulak@giresun.edu.tr](mailto:oznur.kulak@giresun.edu.tr)

<sup>2</sup>*Department of Mathematics and computer Sciences, İstanbul Arel University,  
İstanbul/TURKEY*

[turangurkanli@arel.edu.tr](mailto:turangurkanli@arel.edu.tr)

**Abstract:** In this paper, we define a new weighted variable exponent Wiener amalgam space  $W(L^{p(\cdot),q(\cdot)}, L^r_\omega)$  whose local component is variable exponent Lorentz space and the global component is weighted Lebesgue space. We give some characterizations of this space. At the end of the paper we discuss boundedness and unboundedness of the Hardy-Littlewood maximal function on  $W(L^{p(\cdot),q(\cdot)}, L^r_\omega)$ .

**Keywords:** Variable exponent Lorentz space, Hardy-Littlewood maximal function, Wiener amalgam space.

**References:**

- [1] A. T. Gürkanlı, "The Amalgam Spaces  $W(L^{p(x)}, l^{\{p_n\}})$  and boundedness of Hardy-Littlewood Maximal operators", *Current Trends in Analysis and Its Applications*, Springer International Publishing Switzerland, (2015).
- [2] I. Aydın, A. T. Gürkanlı, "Weighted variable exponent amalgam spaces  $W(L^{p(x)}, L^q_\omega)$ ", *GlasnikMatematički*, 47(67), (2012), 165-174.
- [3] L. Ephremidze, V. Kokilashvili, S. Samko, "Fractional, maximal and singular operators in variable exponent Lorentz spaces", *Fract. Calc. Appl. Anal.*, 11(4), (2008), 1-14.
- [4] O. Kulak, "The inclusion theorems for variable exponent Lorentz spaces", *Türkish Journal of Mathematics*, 40(2016).

## ON THE GROWTH RATE OF ALGEBRAIC POLYNOMIALS THROUGH THEIR NORM IN BERGMAN SPACE

Pelin ÖZKARTEPE<sup>1</sup>, Fahreddin ABDULLAYEV<sup>2</sup>

<sup>1</sup>Mersin/TURKEY

[pelinozkartepe@gmail.com](mailto:pelinozkartepe@gmail.com)

<sup>2</sup>Department of Mathematics, Mersin University

Mersin/TURKEY

[fabdul@mersin.edu.tr](mailto:fabdul@mersin.edu.tr)

---

**Abstract:** In many areas of research in mathematics (in approximation theory, embedding theory and etc.), one can be faced with two important problems given in the following: a) Determining how to undergo a change of (semi)norm of the holomorphic function when the given region expands; b) Determining the relationships between different (semi)norms of analytic functions in a given finite Jordan region on the complex plane in the various (semi)normed space [2]. We will consider these problems for algebraic polynomials of complex variables in the well known Bergman space. We will investigate the following problems: evaluating the increase of the modulus of polynomials in the exterior of the given region with respect to the norm of the polynomial in this region [3,4]; determining a change of (semi)norm of polynomials for the given region.

**Keywords:** Algebraic polynomials, Quasiconformal mapping, Quasidisk.

### References:

- [1] J.L. Walsh, Interpolation and Approximation by Rational Functions in the Complex Domain, AMS, 1960.
- [2] F.G. Abdullayev, U. Deger, On the orthogonal polynomials with weight having singularity on the boundary of regions of the complex plane, Bull. Belg. Math. Soc., 2009, Vol 16, No:2, pp.235-250.
- [3] N. Stylianopoulos, Strong asymptotics for Bergman polynomials over domains with corners and applications, Const. Approx., 33, 2013, 59-100.
- [4] F.G. Abdullayev, P. Özkartepe, Uniform and pointwise Bernstein-Walsh-type inequalities on a quasidisk in the complex plane, Bulletin of Belg. Math. Soc. Simon Stevin 23, No:2, 2016, pp. 285–310.2015 , pp.699-725.

## DELAY DIFFERENTIAL OPERATORS AND SOME SOLVABLE MODELS IN LIFE SCIENCES

Pembe İPEK<sup>1</sup>, Bülent YILMAZ<sup>2</sup>

Zameddin. İSMAİLOV<sup>1</sup>

<sup>1</sup>*Institute of Natural Sciences, Karadeniz Technical University,  
Trabzon/TURKEY*

[ipekpebbe@gmail.com](mailto:ipekpebbe@gmail.com)

[zameddin.ismailov@gmail.com](mailto:zameddin.ismailov@gmail.com)

<sup>2</sup>*Department of Mathematics, Marmara University,  
Istanbul/TURKEY*

[bulentyilmaz@marmara.edu.tr](mailto:bulentyilmaz@marmara.edu.tr)

**Abstract:** Using the methods of spectral theory of differential operators in Hilbert space  $L^2$  – solvability of some models arising in life sciences is investigated. Particularly, concrete solvable models are given.

**Keywords:** Hilbert space and direct sum of Hilbert spaces; delay differential operator; bounded and boundedly solvable operators; extension of an operator; Hutchinson's, Houseflies, Drug-free and medical models.

### References:

- [1] M.I. Vishik, "On General Boundary Problems for Elliptic Differential Equations", Amer. Math. Soc. Transl. II, 24(1963), 107-172.
- [2] L. Edelstein-Keshet, "Mathematical Models in Biology", McGraw-Hill, New York, (1988).
- [3] V. Karakaya, M. Altun, "Fine Spectra of Upper Triangular Double-Band Matrices", J. Comp. Appl. Math., 234(2010), 1387-1394.
- [4] S. Ruan, "Delay Differential Equations in Single Species Dynamics. In: Delay Differential Equations and Applications", Springer, Berlin, (2006).
- [5] M. Villasana, A. Radunskaya, "A Delay Differential Equation Model for Tumor Growth", J. Math. Biol., 47(2003), 270-294.

## STATISTICALLY RELATIVELY A-SUMMABILITY OF CONVERGENCE OF DOUBLE SEQUENCES OF POSITIVE LINEAR OPERATORS

Pınar OKÇU<sup>1</sup>, Fadime DİRİK<sup>2</sup>

<sup>1</sup>*Department of Mathematics, Sinop University,  
Sinop/TURKEY*

[okcupinar@gmail.com](mailto:okcupinar@gmail.com)

<sup>2</sup>*Department of Mathematics, Sinop University,  
Sinop/TURKEY*

[fdirik@sinop.edu.tr](mailto:fdirik@sinop.edu.tr)

**Abstract:** In this presentation, we introduce the concept of statistically relatively A-summability. Based upon this definition and A-statistically relatively uniform convergence for double sequences of functions, we prove a Korovkin-type approximation theorem. Also, we present a strong application.

**Keywords:** A-statistically relatively uniform convergence, statistically A-summability, positive linear operator, Korovkin theorem.

### References:

- [1] A.D. Gadjiev, C. Orhan, "Some approximation theorems via statistical convergence", *Rocky Mount. J. Math.*,32(2002),129-138.
- [2] F.Dirik, K. Demirci, "Korovkin-Type approximation theorem for functions of two variables in statistical sense", *Turk. J. Math.*,34(2010), 73-83.
- [3] H.Steinhaus, "Sur la convergence ordinaire et la convergence asymptotique", *Colloq Math.*,2(1951),73-74.
- [4] K.Demirci, S. Karakuş, "Korovkin-Type approximation theorem for double sequences of positive linear operators via A-Summability", *Results. Math.*, 63(2013),1-13.
- [5] K.Demirci, S. Orhan, "Statistically relatively uniform convergence of positive linear operators", *Results. Math.*, DOI 10.1007/s00025-015-0484-9(2015).

## SOME SPECTRAL PROPERTIES OF LINEAR OPERATORS ON EXOTIC BANACH SPACES

Rabah DEBBAR

<sup>1</sup>*Department of Mathematics, University of Guelma,  
Box 401, 24000 Guelma/Algeria  
[rabah.debbbar@yahoo.fr](mailto:rabah.debbbar@yahoo.fr)*

**Abstract:** In this work, we present some results concerning the operators defined on various classes of exotic Banach spaces, containing in particular those studied respectively by V. Ferenczi [7, 8] and T. Gowers with B. Maurey [14, 15]. We show that, on hereditarily indecomposable or quotient hereditarily indecomposable Banach space  $X$ , the set of bounded Fredholm operators is dense in  $L(X)$ , this gives that the boundary of bounded Fredholm operators is nothing else but the ideal of strictly singular operators if  $X$  is hereditarily indecomposable Banach space (resp. the ideal of strictly cosingular operators if  $X$  is quotient hereditarily indecomposable Banach space). On the other hand, a comparison between sufficiently rich and exotic Banach spaces is given via some properties of the two maps spectra and Wolf essential spectra.

**Keywords:**

Fredholm perturbation, semi-Fredholm operator, Fredholm operator, hereditarily indecomposable Banach space, essential spectrum.

**References:**

- [1] G. Androulakis and Th. Schlumprecht, *J. London. Math., Soc.*(2) 64 (3), 655 (2001)
- [2] H. Brezis, *Analyse Fonctionnelle, Theorie et Applications* (Masson, 1983).
- [3] S. R. Caradus, W. E. Pfaffenberger, and B. Yood, *Calkin Algebras and Algebras of Operators on Banach Spaces* (Marcel Dekker, New York, 1974).

## SUPPORT VECTOR MACHINES SVM

Rachid BELGACEM<sup>1</sup>, Abdessamad AMIR<sup>2</sup>

<sup>1</sup>*Department of Mathematics, Hassiba Ben bouali University,  
Chlef/ALGERIA*

*belgacemrachid02@yahoo.fr*

<sup>2</sup>*Department of Mathematical, Abdelhamid ibn badis University,  
Mostaganem/ALGERIA*

*amirabdessamad@yahoo.fr*

**Abstract:** The support vector machines or wide margin separators SVM are a class of algorithms based on the search for the optimal hyperplane margin, where possible, classroom or properly separated data. The principle is to find from a training set a classifier, or a classificatory function, the generalization ability (quality forecast) is the largest possible. SVM were developed in the 1990s based on theoretical considerations of Vladimir Vapnik on the development of statistical learning theory. SVM were quickly adopted for their ability to work with large data, the small number of hyper parameters, their theoretical guarantees, and good results in practice. SVMs have been applied to numerous fields (bioinformatics, information retrieval, computer vision, finance ...)

**Keywords:** Classification, Support vector machines.

### References:

- [1] Bradley PS, Mangasarian OL (1998) Feature selection via concave minimization and support vector machines. In: Shavlik J, (ed) Machine learning proceedings of the 15th international conference (ICML '98). San Francisco, California, Morgan Kaufmann.
- [2] Fung G, Mangasarian OL, A feature selection newton method for support vector machine classification. Computational Optimization and Applications, 28, 185--202 (2004).
- [3] Nocedal, J. & Wright, S. J. (2006), Numerical Optimization, second ed., Springer-Verlag, NewYork.

## CHARACTERIZATION OF MIXED MODULUS OF SMOOTHNESS IN WEIGHTED $L_p$ SPACES

Ramazan AKGÜN

*Department of Mathematics, Faculty of Arts and Sciences, Balikesir University,  
Balikesir/TURKEY  
[rakgun@balikesir.edu.tr](mailto:rakgun@balikesir.edu.tr)*

**Abstract:** In this work we consider the mixed modulus of smoothness of fractional order in the Lebesgue spaces with Muckenhoupt weights on two dimensional torus. We obtain a characterization class for the mixed modulus of smoothness of fractional order. Also direct and inverse estimates of angular trigonometric approximation of functions in these spaces. An equivalence between the mixed modulus of smoothness and K-functional and realization functional are established.

**Keywords:** Mixed modulus of smoothness, Muckenhoupt weight, weighted Lebesgue space, characterization class for modulus of smoothness.

### References:

- [1] R. Akgün, "Mixed modulus of continuity in Lebesgue spaces with Muckenhoupt weights", Turk. J. Math., 40(2016).
- [2] C. Cottin, "Mixed K-functionals: a measure of smoothness for blending-type approximation". Math Z 204(1990), 69-83.
- [3] M. K. Potapov, "Approximation by "angle"", In Russian, Proceedings of the Conference on the Constructive Theory of Functions and Approximation Theory, Budapest, 1969, Akadémiai Kiadó, 1972, 371-399.
- [4] M. K. Potapov, B.V. Simonov, S.Y. Tikhonov, "Mixed moduli of smoothness in  $L_p, 1 < p < \infty$ : A survey". Surv. Approx. Theory., 8(2013), 1-57.
- [5] K. V. Runovski, "Several questions of approximation theory", PhD, Disser Cand Nauk, Moscow State University MGU, Moscow, Russia, 1989.



## SOME DIRECT APPROXIMATION THEOREMS IN WEIGHTED ORLICZ SPACES

Ramazan ÇETİNTAŞ<sup>1</sup>, Yunus Emre YILDIRIR<sup>2</sup>

*Balikesir University, Faculty of Art and Science, Department of  
Mathematics,*

*10145, Balikesir, Turkey*

[cetintas\\_ramazan@mynet.com](mailto:cetintas_ramazan@mynet.com)

*Balikesir University, Faculty of Education, Department of Mathematics,*

*10145, Balikesir, Turkey*

[yildirir@balikesir.edu.tr](mailto:yildirir@balikesir.edu.tr)

**Abstract:** In 1963, Chen [10] generalized the definition of Orlicz spaces saving almost all known properties of them. In this definition, the generating Young function of Orlicz spaces is not necessary to be convex. The definition and application to approximation theory Orlicz spaces with Muckenhoupt weights in the sense of Chen was given by AKGUN [11]. In this work, using this definition, we generalize the results obtained in the papers [2, 3, 4] to the weighted Orlicz spaces having generating Young functions not necessary to be convex. We obtained some direct theorems of approximation theorems in these spaces.

### References:

- [1] Ponomarenko, V. G., *Approximation of periodic functions in Orlicz spaces*, Translated from *Sibirskii Matematicheskii Zhurnal*, Vo. 7, No. 6, (1966), 1337-1346.
- [2] Y. E. Yildirir, *Approximation of periodic functions in weighted Orlicz spaces*, *Glasnik Matematički*, 47(67)(2012), 401-413.
- [3] Y. E. Yildirir, R. Cetintas, *Approximation theorems in weighted Orlicz spaces*, *J. Math. Sci. Adv. Appl.*, V. 14, No. 1, (2012), 35-49.
- [4] Y. M. Chen, *On two-functional spaces*, *Studia Math.* 24 (1964), 61-88.
- [5] R. Akgun, *Some inequalities of trigonometric approximation in weighted Orlicz spaces*, *Math. Slovaca*, 66(1), 1-18, (2016).

## UNCONDITIONALLY CAUCHY SERIES AND ZEWIER MATRIX METHOD

Ramazan KAMA<sup>1</sup>, Bilal ALTAY<sup>2</sup>

<sup>1</sup>*Department of Mathematics, Siirt University,  
Siirt/TURKEY*

[ra.kama12@gmail.com](mailto:ra.kama12@gmail.com)

<sup>2</sup>*Faculty of Education, Inonu University,  
Malatya/TURKEY*

[bilal.altay@inonu.edu.tr](mailto:bilal.altay@inonu.edu.tr)

**Abstract:** In this paper, we give some results about completeness of the spaces by means of Zewier matrix method. Also, we characterize continuity of the operators  $T_x: S \rightarrow X$  by weakly unconditionally Cauchy series.

**Keywords:** Zewier matrix, completeness, unconditionally Cauchy series.

### References:

- [1] A. Aizpuru and F. J. Prez-Fernandez, Spaces of S-bounded multiplier convergent series, *Acta Math. Hungar.*, 87 (2000), 103–114.
- [2] F. Albiac and N. J. Kalton, *Topics in Banach Spaces Theory*, Springer Inc., 2006.
- [3] M. Q. Bu and C. Wu, Unconditionally convergent series of operators on Banach spaces, *Math. Anal. Appl.*, 207 (1997), 291–299.
- [4] C. Bessaga and A. Pelczynski, On bases and unconditional convergence of series in Banach spaces, *Stud. Math.*, 17 (1958), 151–164.
- [5] J. Diestel, *Sequences and Series in Banach Spaces*, Springer-Verlag, New York, 1984.
- [6] C. W. McArthur, On relationships amongst certain spaces of sequences in an arbitrary Banach space, *Canad. J. Math.*, 8 (1956), 192–197.

**TAUBERIAN CONDITIONS FOR DOUBLE SEQUENCES  
WHICH ARE STATISTICALLY SUMMABLE (C,1,1) IN  
FUZZY NUMBER SPACE**

Reha YAPALI<sup>1</sup>, Ozer TALO<sup>2</sup>

<sup>1</sup>*Department of Mathematics, Celal Bayar University, Manisa/TURKEY*  
[rehayapali@gmail.com](mailto:rehayapali@gmail.com)

<sup>2</sup>*Department of Mathematics, Celal Bayar University, Manisa/TURKEY*  
[ozertalo@cbu.edu.tr](mailto:ozertalo@cbu.edu.tr)

**Abstract:** In this presentation, we introduce the concept of statistically summability (C,1,1) for double sequences in fuzzy number space  $E^n$  and also we give some tauberian conditions for double sequences of fuzzy numbers that are statistically summable (C,1,1).

**Keywords:** Double sequences; statistical convergence; statistical summability (C,1,1); fuzzy number space

ICAA-2016

## THE REALIZATION OF THE FEEDBACK AMPLIFIER DESIGN WITH USING ARTIFICIAL NEURAL NETWORK

Remzi TUNTAS

*Faculty of business, Department of business administration, YuzuncuYil University,  
Van/TURKEY*  
[rtuntas@hotmail.com](mailto:rtuntas@hotmail.com)

**Abstract:**Operational amplifiers (op-amps) are the most widely used type of linear integrated circuits. There are many advantages to using back in a system design as increase the bandwidth of the amplifier and improve stability. The design of a non-inverting feedback amplifier circuit using Artificial Neural Network (ANN) in this study was performed. The developed ANN model has been trained by Levenberg Marquardt algorithm for design feedback amplifier circuit. After the input and output parameters of proposed ANN model were determined, the most suitable ANN architecture and training parameters were selected. Finally, trained network was tested and it was used for design feedback amplifier circuit.

**Keywords:** Non-inverting feedback amplifier, Artificial Neural Network.

### References:

- [1] R. Jafarnejad, A. Jannesari, A. Nabavi, A. Sahafi, "A low power low noise amplifier employing negative feedback and current reuse techniques", *Microelectronics Journal*, 49(2016), 49-56.
- [2] S. Kargarrazi, L. Lanni, C. Zetterling, "A study on positive-feedback configuration of a bipolar SiC high temperature operational amplifier", *Solid-State Electronics*, 116(2016), 33-37.
- [3] A. Kumar, A. Singh, "Transistor level fault diagnosis in digital circuits using artificial neural network", *Measurement*, 82(2016), 384-390.
- [4] T. Hamdalla, "Theoretical and artificial neural network modeling for the output power of irradiated erbium doped fiber amplifier", *Optics & Laser Technology*, 49(2013), 264-267.

## PREDICTION OF HARDNESS VALUES OF COLD WORKED Al/SiC<sub>p</sub> COMPOSITE AT DIFFERENT REDUCTION RATIO BY ADAPTIVE NEURO-FUZZY INFERENCE SYSTEM

Remzi TUNTAS and Burak DİKİCİ

*Department of Business Administration, Yuzuncu Yil University, Van/TURKEY*  
[rtuntas@yyu.edu.tr](mailto:rtuntas@yyu.edu.tr)

*Department of Mechanical Engineering, Yuzuncu Yil University, Van/TURKEY*  
[burakdikici@yyu.edu.tr](mailto:burakdikici@yyu.edu.tr)

**Abstract:** Aluminum alloys are used widely in the aerospace and, more recently, in the automotive industry as well as in defense industry. The production and potential applications of metal matrix composites have been dramatically increased with technological developments. In this theoretical study, hardness values of the metal matrix composites (MMCs) reinforced with SiC particles has been predicted using by Adaptive Neuro-Fuzzy Inference System (ANFIS) after cold working process at different reduction ratio. To evaluate prediction capabilities of the proposed ANFIS model, the obtained results were compared with experimental data in terms of statistical values used in the literature. It was shown that there are very good correlation between the predicted and the experimental values. The other results have been discussed in details.

**Keywords:** Three step iteration, strong convergence, rate of convergence, data dependence integral equation.

### References:

- [1] J.S.R. Jang, "ANFIS Adaptive-Network-Based Fuzzy Inference Systems," IEEE Trans, Syst. Man Cybernet, 23(1993), 665.
- [2] R. Tuntas, B. Dikici, "An investigation on the aging responses and corrosion behaviour of A356/SiC composites by neural network: The effect of cold working ratio", J Compos Mater, 50(2016), 2323.
- [3] B. Dikici, C. Tekmen, "A comparative study: The combined effect of the cold working and age hardening processes on pitting behaviour of Al/SiC metal matrix composites under saline environment", J Compos Mater, 50(2016), 471.

## DIFFERENCE SEQUENCE SPACES AND MATRIX TRANSFORMATIONS OF SOME BILATERAL SEQUENCES

Rıdvan Cem DEMİRKOL<sup>1</sup>, Harun POLAT<sup>2</sup>

<sup>1</sup>*Department of Mathematics, MuşAlparslan University,  
Muş/TURKEY*

[rc.demirkol@alparslan.edu.tr](mailto:rc.demirkol@alparslan.edu.tr)

<sup>2</sup>*Department of Mathematics, MuşAlparslan University,  
Muş/TURKEY*

[h.polat@alparslan.edu.tr](mailto:h.polat@alparslan.edu.tr)

**Abstract:** In this study, we introduce difference sequence spaces of some bilateral sequences  $X(\Delta, \mathbb{Z})$ , where  $X$  denotes one of the sequence spaces of  $l_\infty$ ,  $c$ , or  $c_0$ . For instance  $l_\infty(\Delta, \mathbb{Z}) = \{x = (x_k)_{k \in \mathbb{Z}} : \Delta x \in l_\infty(\mathbb{Z})\}$ . Besides we compute continuous  $\alpha$ ,  $\beta$ , and  $\gamma$  duals of these spaces  $X(\Delta, \mathbb{Z})$ . Finally we characterize some matrix transformations between these bilateral sequence spaces.

**Keywords:** Bilateral sequences, difference sequence spaces, duals, matrix transformations.

### References:

- [1] H. Kızmaz, "On Certain Sequence Spaces", *Canad. Math. Bull.* 24(1981), 169-176
- [2] R. Agrawal, JK. Srivastava, "Banach Space Valued Bilateral Sequence Space", *British Journal of Mathematics and Computer Science*, 3(2013), 44-51.
- [3] R. Agrawal, JK. Srivastava, "Continuous duals of  $ac_0(\mathbb{Z}, X, \bar{\lambda}, \bar{p})$  and  $c(\mathbb{Z}, X, \bar{\lambda}, \bar{p})$ ", *Methods of Functional Analysis and Topology*, 20(2014), 92-100.
- [4] A. Taheri, "Function Spaces and Partial Differential Equations Volume 1- Classical Analysis", *Oxford Lecture Series in Mathematics and Its Applications*, (2015).

## TWO-WEIGHTED INEQUALITIES FOR MULTIDIMENSIONAL HARDY OPERATOR IN VARIABLE WEIGHTED LEBESGUE SPACES WITH MIXED NORM

R. A. BANDALIYEV<sup>1</sup>, S. G. HASANOV<sup>2</sup>

<sup>1</sup>*Institute of Mathematics and Mechanics of NAS of Azerbaijan,  
Baku/AZERBAIJAN*

[bandaliyev.rovshan@math.ab.az](mailto:bandaliyev.rovshan@math.ab.az)

<sup>2</sup>*Institute of Mathematics and Mechanics of NAS of Azerbaijan,  
Baku/AZERBAIJAN*

[sabirhasanov@gmail.com](mailto:sabirhasanov@gmail.com)

**Abstract:** In this report, a two-weight boundedness of multidimensional Hardy operator and its dual operator acting from weighted Lebesgue spaces with mixed norm into weighted variable Lebesgue spaces with mixed norm spaces is given. In particular, a new type two-weight criterion of multidimensional Hardy operator is obtained.

The research of R. Bandaliyev was partially supported by the grant of Science Development Foundation under the President of the Republic of Azerbaijan, Grant EIF-2013-9(15)-46/10/1 and by the grant of Presidium of Azerbaijan National Academy of Science 2015.

## GROWTH OF SOLUTIONS OF LINEAR DIFFERENTIAL EQUATIONS AROUND AN ISOLATED ESSENTIAL SINGULARITY

Saada HAMOUDA

*Department of Mathematics, Abdelhamid Ibn Badis University,  
Mostaganem/ALGERIA  
[hamouda\\_saada@yahoo.fr](mailto:hamouda_saada@yahoo.fr)*

**Abstract:** In this paper we study the growth of solutions of certain class of linear differential equations around an isolated essential singularity point. For that we transform by making use a conformal mapping certain results from the complex plane to a neighborhood of a singular point. We will see that there are large similarities between the complex plane results and this investigation.

**Keywords:** Linear differential equations, local growth of solutions, essential isolated singularity.

### References:

- [1] S. Hamouda, Properties of solutions to linear differential equations with analytic coefficients in the unit disc, *Electron. J. Differential. Equ.* Vol 2012 (2012), No. 177, pp. 1-9.
- [2] S. Hamouda, Iterated order of solutions of linear differential equations in the unit disc, *Comput. Methods Funct. Theory*, 13 (2013) No. 4, 545-555.
- [3] W.K. Hayman, *Meromorphic functions*, Clarendon Press, Oxford, 1964.
- [4] R. Korhonen, Nevanlinna theory in an annulus, in: *Value Distribution Theory and Related Topics*, in: *Adv. Complex Anal. Appl.*, vol. 3, Kluwer Acad. Publ., Boston, MA, 2004, pp. 167-179.



## ALGEBRAIC PROPERTIES OF JOIN AND CORONA PRODUCT OF GRAPHS

Sadık DELEN, Ismail Naci CANGUL

*Department of Mathematics, Uludag University,  
Gorukle, Bursa, Turkey  
[matesadik@gmail.com](mailto:matesadik@gmail.com),  
[cangul@uludag.edu.tr](mailto:cangul@uludag.edu.tr)*

**Abstract:** Given any two graphs, it is possible to obtain a new graph from them using some certain operation. There are several operations on graphs. Two of them are join and Corona product. In this talk, we determine the abstract algebraic structure of the set of simple connected graphs according to join and Corona product of two given graphs. Also some new properties are obtained.

**Keywords:** Graph theory, graph operation, join, Corona product

### References:

[1] Das, K. Ch., Xu, K., Cangul, I. N., Cevik, A. S., Graovac, A., On the Harary Index of Graph Operations, Journal of Inequalities and Applications, SI: Recent Advances in General Inequalities, DOI: 10.1186/1029-242X-2013-339, 2013, 1-16

[2] Das, K. Ch., Yurttas, A., Togan, M., Cangul, I. N., Cevik, A. S., The Multiplicative Zagreb Indices of Graph Operations, Journal of Inequalities and Applications, 90, doi:10.1186/1029-242X-2013-90, 2013, 1-14

[3] Khalifeh, M. H., Azari, H. Y., Ashrafi, A. R.: The hyper-Wiener index of graph operations, Computers and Mathematics with Appl., 56 (2008), 1402-1407

## COMMON FIXEDPOINT THEOREMS FOR WEAKLY SUBSEQUENTIALLY CONTINUOUS MAPS IN MODIFIED INTUITIONISTIC METRIC SPACES

Said BELOUL

*Department of Mathematics, EL-Oued University,  
ALGERIA  
[beloulsaid@gmail.com](mailto:beloulsaid@gmail.com)*

**Abstract:** The aim of this work is to prove common fixed point theorems for two weakly subsequentially continuous and compatible of type (E) pairs of self mappings which satisfying implicit relation in modified intuitionistic fuzzy metric spaces, an example is given to illustrate our results, our results improve and generalize some previous results.

**Keywords:** Common fixed point, weakly subsequentially continuous, compatible of (E), implicit relation, modified intuitionistic fuzzy metric space.

### References:

- [1] A. T. Atanassov, Intuitionistic fuzzy sets, *Fuzzy Sets Syst.* 20 (1986), 87-96
- [2] C. Alaca, D. Turkoglu and C. Yildiz, Fixed points in Intuitionistic fuzzy metric spaces, *Chaos Solitons and Fractals*, 29 (2006), 1073-1078.
- [3] S. Beloul, Common fixed point theorems for weakly subsequentially continuous generalized contractions with applications, *Appl. Maths. E-Notes*, 15 (2015), 173-186.
- [4] S. Chauhan, M. Imdad and B. Samet, Coincidence and common fixed point theorems in modified intuitionistic fuzzy metric spaces, *Math. Comput. Model* 58 (2013), 892-900.
- [5] M. Imdad, J. Ali and M. Hasan, Common fixed point theorems in modified intuitionistic fuzzy metric spaces *Iranian Journal of Fuzzy Systems* Vol. 9, No. 5, (2012) pp. 77-92.

## EXPONENTIAL STABILITY OF SOME NEURAL NETWORK SYSTEMS OF COHEN-GROSSBERG TYPE

Said MAZOUZI

*Laboratory of Applied Mathematics, Badji Mokhtar-Annaba University,  
P.O.Box 12, 23000 Annaba, Algeria.*

*Co-author Nassereddine TATAR, Department of Mathematics,  
KFUPM, Dahrn, Saudi Arabia.*

**Abstract:** Our main concern in the expected oral talk is the study of some neural network systems of Cohen-Grossberg type which are extensively applied in various areas of science and technology such as in neurobiology, image processing and so on. Time delays are introduced in the system because of the finite switching speed of the signal transmission and amplification time. To the knowledge of the reader time delays could cause instability and even oscillation of a given model, and so appropriate assumptions are really needed to avoid chaos, divergence or bifurcation states. We will first establish the existence of a unique equilibrium point for such a system, and then, by using Halanay inequality, we prove that the obtained unique equilibrium is exponentially asymptotically stable.

**Keywords:** Cohen-Grossberg neural network systems; equilibrium point; Halanay inequality; exponential stability.

### References:

- [1] M. A. Cohen and S. Grossberg, Absolute stability of global pattern formation and parallel memory storage by competitive neural networks, *IEEE Trans. Systems Man Cybernet.* 13 (1983), 815-826.
- [2] R. D. Driver, *Ordinary and delay differential equations*, Springer-Verlag, N.Y., 1977, 389-390.
- [3] C. Feng and R. Plamondon, On the stability analysis of delayed neural network systems, *Neural Network* 14 (2001), 1181-1188.
- [4] H. Wu, F. Tao, L. Qin, R. Shi and L. He, Robust exponential stability for interval neural networks with delays and non-Lipschitz activation functions, *Nonlinear Dyn.* 66 (2011), 479-487.
- [5] J. Zhou, S. Y. Li and Z. G. Yang, Global exponential stability of Hopfield neural networks with distributed delays, *Appl. Math. Model.* 33 (2009), 1513-152.

## EXACT SOLUTIONS AND CONSERVATION LAWS OF 3+1 DIMENSIONAL YTSF EQUATION

Sait SAN

<sup>1</sup>*Department of Mathematics-Computer  
Eskisehir Osmangazi University, Eskisehir/TURKEY  
ssan@ogu.edu.tr*

**Abstract:** In this study, we derive exact traveling wave solution of the (3+1) dimensional potential-YTSF equation by a generalized Kudryashov method. Moreover, conservation laws are derived for the underlying equation by employing the multiplier method with the first order multipliers.

**Keywords:** Exact solution, Conservation laws, Multiplier method.

### References:

- [1] Demiray, S. Tuluce, Yusuf Pandir, and Hasan Bulut. "The investigation of exact solutions of nonlinear time-fractional Klein-Gordon equation by using generalized Kudryashov method." *AIP Conference Proceedings*. Vol. 1637. 2014
- [2] Song, M., & Ge, Y. (2010). Application of the-expansion method to (3+ 1)-dimensional nonlinear evolution equations. *Computers & Mathematics with Applications*, 60(5), 1220-1227.
- [3] Cheviakov, A. F. (2007). GeM software package for computation of symmetries and conservation laws of differential equations. *Computer physics communications*, 176(1), 48-61.
- [4] Adem, A. R., &Khalique, C. M. (2012). Symmetry reductions, exact solutions and conservation laws of a new coupled KdV system. *Communications in Nonlinear Science and Numerical Simulation*, 17(9), 3465-3475.

## GENERALIZED RESULT OF GLOBAL SOLUTIONS TO A CLASS OF A REACTION-DIFFUSION SYSTEM

Salah BADRAOUI

*University 8 mai 1945 Guelma, Department of Mathematics*

*BP.401, Guelma 24000, Algeria*

salah.badraoui@gmail.com

**Abstract:** We prove in this work a generalized result of global classical solutions in time to a class of a reaction diffusion system defined on a bounded domain in  $\mathbb{R}^n$ .

**Keywords:** Reaction-diffusion equations, positivity of solutions, global existence, uniform boundedness, continuous semigroups, Lyapunov functional.

### References:

- [1] S. Badraoui; Existence of global solutions for systems of reaction-diffusion equations on unbounded domains, *EJDE*, Vol. 2002, No. 74, 1-10.
- [2] A. Haraux and M. Kirane; Estimations  $C^1$  pour des problèmes paraboliques semi-linéaires, *Ann. Fac. Sci. Toulouse Math.* 5 (1983), 265-280.
- [3] J. I. Kanel and M. Kirane; Global existence and large time behavior of positive solutions to a reaction-diffusion system, *Differ Integral Equ*, Volume 13 (1-3) (2000), 255-264.
- [4] J. I. Kanel and M. Kirane; Global solutions of reaction-diffusion systems with a balance law and nonlinearities of exponential growth, *J. Differential Equations* 165 (2000), 24-41.

## A MODIFIED REGULARIZATION METHOD FOR A NON-LINEAR ABSTRACT PARABOLIC EQUATION

Salah DJEZZAR<sup>1</sup>, Roumaïssa BENMARAÏ<sup>2</sup>

<sup>1</sup>*Department of Mathematics, FreresMentouriUniversity,  
Constantine/ALGERIA  
salah.djezzar@gmail.com*

<sup>2</sup>*Department of Mathematics, FreresMentouriUniversity,  
Constantine/ALGERIA  
romiben6@gmail.com*

**Abstract:** In this work, we study the abstract backward parabolic problem. This problem is known to be severely ill posed. We regularize this problem, using a new modified regularization method to obtain a family of approximate well posed problems. We also give the error estimate between the regularized solution and the exact solution (when it exists). Moreover, some other convergence results are also established.

**Keywords:** Ill-posed problem, nonlinear backward problem, quasi-reversibility value methods, quasi-boundary value-methods.

### References:

- [1] G.W. Clark, S.F. Oppenheimer, Quasi-reversibility methods for non-well posed problems, *Electron. J. Differential Equations* 1994 (8) (1994) 1\_9.
- [2] R. Lattès, J.L. Lions, *Méthode de Quasi-réversibilité et Applications*, Dunod, Paris, 1967.
- [3] S. Djezzar and N. Teniou, "Improved regularization method for backward Cauchy problems associated with continuous spectrum operator " *International Journal of Differential Equations*, Volume 2011, Article ID 93125, 11pages.
- [4] T.N. HUY, M. KIRANE, L.D. LE, T.V.NGUYENV, "On the approximation of fixed points of weak contractive filter regularization for an inverse parabolic problem in several variables" *Electronic Journal of Differential Equations*, Vol. 2016 (2016), No. 24, pp. 1-13.

## ASYMPTOTIC BEHAVIOR OF WEAKLY COUPLED THERMOELASTIC WAVE MODEL

Salem NAFIRI

**Abstract:** This paper has two objectives. First, we propose a system of partial differential equations describing the behavior of a one-dimensional thermoelastic structure occupying a bounded interval of  $\mathbb{R}$ . For an initial-boundary value problem associated with this system, we prove a global well-posedness result in a certain topology under appropriate regularity

conditions on the data. Further, we show that under particular classes of 'natural' boundary conditions, the energy associated to the system decays polynomially to zero. Secondly, we consider the case where the domain is unbounded and we study conditions under which stability estimates still holds.

**Keywords:** thermoelastic structure, contraction semigroups, polynomial decay.

## ON THE CONVERGENCE FOR A SEQUENCE OF INTERVALS OF FUZZY NUMBERS

Salih AY TAR

*Department of Mathematics, SüleymanDemirelUniversity,  
Isparta/TURKEY  
[salihaytar@sdu.edu.tr](mailto:salihaytar@sdu.edu.tr)*

**Abstract:** In this study, we show that, if the  $n$ th term of a sequence  $X = \{[X_n, Y_n]\}$  of intervals of fuzzy numbers contains the  $n$ th term of such another sequence  $Z = \{[Z_n, W_n]\}$  for each positive integer  $n$ , then the limit of  $X$  contains the limit of  $Z$ , provided that these limits exist. Moreover, we show that this situation may not hold in the context of rough convergence. Furthermore, we demonstrate how to construct a convergent/rough convergent sequence of fuzzy numbers from a convergent/rough convergent sequence of intervals of fuzzy numbers.

**Keywords:** Rough convergence; Sequence of intervals of fuzzy numbers.

### References:

- [1] F.G. Akçay, S. Ay tar (2015), Rough convergence of a sequence of fuzzy numbers, Bulletin of Mathematical Analysis and Applications, 7(4): 17-23.
- [2] S. Ay tar (2015), Order intervals in the metric space of fuzzy numbers, Iranian Journal of Fuzzy Systems, 12(5): 139-147
- [3] H.X. Phu (2001), Rough convergence in normed linear spaces, Numer. Funct. Anal. and Optimiz., 22:201-224.

## SOME INEQUALITIES FOR DOUBLE INTEGRALS AND APPLICATIONS FOR CUBATURE FORMULA

Samet ERDEN<sup>1</sup>, M. Zeki SARIKAYA<sup>2</sup>

<sup>1</sup>*Department of Mathematics, Bartın University,  
Bartın/TURKEY  
[erdensmt@gmail.com](mailto:erdensmt@gmail.com)*

<sup>2</sup>*Department of Mathematics, Düzce University,  
Düzce/TURKEY  
[sarikayamz@gmail.com](mailto:sarikayamz@gmail.com)*

**Abstract:** We establish an Ostrowski type inequality for double integrals of second order partial derivative functions which are bounded. Then, we deduce some inequalities of Hermite-Hadamard type for double integrals of functions whose partial derivatives in absolute value are convex on the co-ordinates on rectangle from the plane. Finally, some applications in Numerical Analysis in connection with cubature formula are given.

**Keywords:** Ostrowski inequality, Hermite-Hadamard inequality, co-ordinated convex mapping, cubature formula.

### References:

- [1] N.S. Barnett, S.S. Dragomir, "An Ostrowski type inequality for double integrals and applications for cubature formulae", *Soochow J. Math.*, 27 (1) (2001), 109-114
- [2] S.S. Dragomir, "Some perturbed Ostrowski type inequalities for absolutely continuous functions (I)", *Acta Universitatis Matthiae Belii*, series Mathematics, 23 (2015), 71-86.
- [3] M.A. Latif, S.S. Dragomir, "On some new inequalities for differentiable co-ordinated convex functions", *Journal of Inequalities and Applications*, 2012, 2012:28.
- [4] S. Erden, M.Z. Sarikaya, "An Ostrowski Type Inequality for Twice Differentiable Mappings and Applications", *Mathematical Modelling and Analysis*, in press.



## SOME PERTURBED INEQUALITIES OF OSTROWSKI TYPE FOR TWICE DIFFERENTIABLE FUNCTIONS

Samet ERDEN<sup>1</sup>, Hüseyin BUDAK<sup>2</sup>, M. Zeki SARIKAYA<sup>2</sup>

<sup>1</sup>*Department of Mathematics, Bartın University,  
Bartın/TURKEY  
[erdensmt@gmail.com](mailto:erdensmt@gmail.com)*

<sup>2</sup>*Department of Mathematics, Düzce University,  
Düzce/TURKEY  
[hsyn.budak@gmail.com](mailto:hsyn.budak@gmail.com)  
[sarikayamz@gmail.com](mailto:sarikayamz@gmail.com)*

**Abstract:** We establish new perturbed Ostrowski type inequalities for functions whose second derivatives are of bounded variation. In addition, we obtain some integral inequalities for absolutely continuous mappings. Finally, some inequalities related to Lipschitzian derivatives are given.

**Keywords:** Function of bounded variation, Perturbed Ostrowski type inequalities.

### References:

- [1] S.S. Dragomir, "Some perturbed Ostrowski type inequalities for functions of bounded variation", *Asian-European Journal of Mathematics*, 8(4) (2015), 14 pages.
- [2] S.S. Dragomir, "*Some perturbed Ostrowski type inequalities for absolutely continuous functions (I)*", *Acta Universitatis Matthiae Belii, series Mathematics*, 23 (2015), 71-86.
- [3] S.S. Dragomir, "*Some perturbed Ostrowski type inequalities for absolutely continuous functions (II)*", *RGMA Research Report Collection*, 16 (2013), Article 93, 16 pp.
- [4] S.S. Dragomir, "*Some perturbed Ostrowski type inequalities for absolutely continuous functions (III)*", *TJMM*, 7(1) (2015), 31-43.
- [5] H. Budak, M. Z. Sarikaya, "*Some perturbed Ostrowski type inequality for functions whose first derivatives are of bounded variation*", *RGMA Research Report Collection*, 19 (2016), Article 54, 13 pp.

## ON THE PALINDROMICS CONTINUED FRACTIONS IN THE FIELD $F_q((X^{-1}))$

Sana DRISS

*Faculte des Sciences de Sfax, Tunisia*  
sana\_driss@yahoo.fr

**Abstract:** In 2007 B. Adamczewski and Y. Bugeaud have proved that if the continued fractions expansion of a non quadratic real  $x$  begin with sufficiently large palindrome then  $x$  is transcendental. In this paper we study the same problem in the fields of formal power series over a finite fields. We recall that Schmidt's theorem is not valuable in this case.

## CONVERGENCE THEOREMS FOR EQUILIBRIUM PROBLEMS AND GENERALIZED HYBRID MAPPINGS

Sattar ALIZADEH<sup>1</sup>, Fridoun MORADLOU<sup>2</sup>

<sup>1</sup>*Department of Mathematics, Marand Branch, Islamic Azad University,  
Marand/IRAN*

salizadeh@marandiau.ac.ir

<sup>2</sup>*Department of Mathematics, Sahand University of Technology,  
Tabriz/IRAN*

moradlou@sut.ac.ir

**Abstract:** In this presentation, we introduce a new modified Ishikawa iteration process for finding a common element of the solutions set of an equilibrium problem and the set of fixed points of generalized hybrid mappings in a Hilbert space. Our results generalize and improve some existing results in the literature. A numerical example is given to illustrate the usability of our results.

**Keywords:** Equilibrium problem, Fixed point, Hybrid method, Hilbert space, Weak convergence, Strong convergence.

### References:

- [1] S. Alizadeh and F. Moradlou, A strong convergence theorem for equilibrium problems and generalized hybrid mappings *Mediterr. J. Math.* **13** (2016), 379-390.
- [2] E. Blum and W. Oettli, From optimization and variational inequalities to equilibrium problems, *Mathematics Students*, **63** (1994), 123-145.
- [3] C. E. Chidume and S. A. Mutangadura, An example on the Mann iteration method for Lipschitz pseudocontractions, *Proc. Am. Math. Soc.* **129** (2001) 2359-2363.
- [4] P. L. Combettes and S. A. Hirstoaga, Equilibrium programming in Hilbert spaces, *J. Nonlinear Convex Anal.* **6** (2005) 117-136.

## HYERS-ULAM-RASSIAS STABILITY OF A VOLTERRA INTEGRO-DIFFERENTIAL EQUATION

Sebaheddin ŞEVGİN

*Department of Mathematics, YüzüncüYılUniversity,  
Van/TURKEY*

[ssevgin@yahoo.com](mailto:ssevgin@yahoo.com)

**Abstract:** In this presentation, by applying the fixed point alternative method, we give a necessary and sufficient condition in order that a Volterra integro-differential equation has the Hyers-Ulam-Rassias stability under some additional conditions.

**Keywords:** Fixed point method, integro-differential equation, Hyers-Ulam-Rassias stability.

### References:

- [1] Bojor, Florin. "Note on the stability of first order linear differential equations." *Opuscula Mathematica* 32.1 (2012): 67-74.
- [2] Alqifiary, QusuayHatim. "Note on the stability for linear systems of differential equations." *International Journal of Applied Mathematical Research* 3.1 (2013): 15-22.
- [3] Sevgin, Sebaheddin, and HamdullahSevli. "Stability of a nonlinear Volterra integro-differential equation via a fixed point approach." *Journal of Nonlinear Sciences and Applications* 9.1 (2016): 200-207.

## APPROXIMATION PROPERTIES OF ANALYTIC FUNCTIONS BY THE SEQUENCES OF $k$ -POSITIVE LINEAR OPERATORS IN SOME SUBSPACE OF ANALYTIC FUNCTIONS

Tülin COŞKUN<sup>1</sup>, Seda KARATEKE<sup>2</sup>

<sup>1</sup>Department of Mathematics, Bülent Ecevit University,  
Zonguldak/TURKEY

[tcoskun@beun.edu.tr](mailto:tcoskun@beun.edu.tr)

<sup>2</sup>Department of Mathematics and Computer, Istanbul Arel University,  
Istanbul/TURKEY

[sedakarateke34@gmail.com](mailto:sedakarateke34@gmail.com)

**Abstract:** It is known that Korovkin type theorem is not valid in the space of analytic functions. In this presentation, we put in evidence that Korovkin type theorem is true for the space  $A_g$ , the space  $A_g$  consists of analytic functions whose coefficients satisfy the inequality  $|f_k| \leq M_f g(k)$  such that  $g(k) = 1 + k^2$ . The theorem is proved by choosing the test functions as  $g_\vartheta(z) = \sum_{k=0}^{\infty} k^\vartheta z^k$ ,  $\vartheta = 0, 1, 2$  and finally, an example is given.

**Keywords:** Korovkin type theorem,  $k$ -positive linear operators, analytic functions

### References:

- [1] A. D. Gadjiev, H. Hacısalihoğlu, "Lineer Pozitif Operatörler Dizilerinin Yakınsaklığı", 1. Basım A.Ü.F.F Döner Sermaye İşletmesi Yayınları:31, Ankara, (1995), s. 78-100.
- [2] P. P. Korovkin, "Linear Operators and Approximation Theory", Hindustan Publishing, (1960), pp. 1-100
- [3] M. A. Evgrafov, "Analytic Functions", W. B. Saunders Company, Philadelphia and London, (1966), pp. 24-46.
- [4] T. Başkan, "Kompleks Fonksiyonlar Teorisi", 5. Basım Nobel Yayınları, Ankara, (2003), s. 26-200.
- [5] E. Freitag, R. Busam, "Complex Analysis", Springer-Verlag Berlin Heidelberg, New York, (2005), pp.9-244.

## HERMITE-HADAMARD AND SIMPSON-LIKE TYPE INEQUALITIES FOR DIFFERENTIABLE $p$ -QUASI- CONVEX FUNCTIONS

İmdat İŞCAN<sup>1</sup>, Sercan TURHAN<sup>2</sup>, Selahattin MADEN<sup>3</sup>

<sup>1</sup> *Department of Mathematics, Giresun University, Giresun/TURKEY,*  
[imdati@yahoo.com](mailto:imdati@yahoo.com)

<sup>2</sup> *Dereli Vocational High School, Giresun University,*  
*Giresun/TURKEY,*[sercanturhan28@gmail.com](mailto:sercanturhan28@gmail.com)

<sup>3</sup> *Department of Mathematics Ordu University, Ordu/TURKEY,*  
[maden55@mynet.com](mailto:maden55@mynet.com)

**Abstract:** In this paper, we give a new concept which is a generalization of the concepts quasi-convexity and harmonically quasi-convexity and establish a new identity. A consequence of the identity is that we obtain some new general inequalities containing all of the Hermite-Hadamard and Simpson-like type for functions whose derivatives in absolute value at certain power are  $p$ -quasi-convex. Some applications to special means of real numbers are also given.

**Keywords.**  $p$ -Quasi-convex functions, Hermite-Hadamard type inequality, Simpson inequality.

### References:

- [1] Alomari, M. W., Darus, M., Kirmaci, U. S, Refinements of Hadamard-type inequalities for quasi-convex functions with applications to trapezoidal formula and to special means, *Computers and Mathematics with Appl.*, 59(2010), 225-232.
- [2] Alomari, M., Hussain, S., Two inequalities of Simpson type for quasi-convex functions and applications, *Applied Mathematics E-Notes*, 11(2011), 110-117.

## ON SOME EQUALITIES OF ORDINARY LEAST SQUARES AND BEST LINEAR UNBIASED ESTIMATORS UNDER A GENERAL PARTITIONED LINEAR MODEL

Selahattin MADEN

Department of Mathematics, Ordu University, Ordu/TURKEY  
[maden55@myynet.com](mailto:maden55@myynet.com)

**Abstract:** Estimations of partial coefficients in a general regression models involve some complicated operations of matrices and their generalized inverses. In this presentation, we consider a general partitioned linear model  $\mathcal{M} = \{y, X_1\beta_1 + X_2\beta_2, \sigma^2\Sigma\}$  and its stochastically restricted model without any rank assumptions. We give necessary and sufficient conditions for the equalities of the ordinary least squares estimators (OLSEs) and best linear unbiased estimators (BLUEs) of  $X\beta$ . Also, we give an example for the equality of BLUEs of  $X\beta$  under a general linear model and its stochastically restricted model.

**Keywords:** General linear model, stochastically restricted model, partitioned linear model, OLSE, BLUE.

### References:

- [1] C. Lu, S. Gan, Y. Tian, "Some remarks on general linear model with new regressors", Stat. and Prob. Letters 97(2015), 16-24.
- [2] H. Yang, J. Wu, "Estimation in singular linear models with stochastic linear restrictions and linear equality restriction", Communications Statistics-Theory and Methods, 40(2011), 4364-4371.
- [3] X. Ren, "On the equivalence of the BLUEs under a general linear model and its restricted and stochastically restricted model", Stat. and Prob. Letters, 90(2014), 1-10.
- [4] Y. Tian, B. Jiang, "Equalities for estimators of partial parameters under linear model with restrictions", Journal of Multivariate Analysis 143(2016), 299-313.
- [5] Y. Tian, J. Zhang, "Some equalities for estimations of partial coefficients under a general linear regression model", Stat. Papers 52(2011), 911-920.

## SOME RESULTS ON THE GENERALIZED MELLIN TRANSFORMS AND APPLICATIONS

Selcan KOCABAŞ<sup>1</sup>, Ezgi ERDOĞAN<sup>2</sup>, A. Neşe DERNEK<sup>3</sup>

<sup>1</sup>*Department of Mathematics, University of Marmara, Istanbul/TURKEY*

*[selcan.kocabas@gmail.com](mailto:selcan.kocabas@gmail.com)*

<sup>2</sup>*Department of Mathematics, University of Marmara, Istanbul/TURKEY*

*[ezgi.erdogan@marmara.edu.tr](mailto:ezgi.erdogan@marmara.edu.tr)*

<sup>3</sup>*Department of Mathematics, University of Marmara, Istanbul/TURKEY*

*[ndernek@marmara.edu.tr](mailto:ndernek@marmara.edu.tr)*

**Abstract:** This presentation discusses the generalized Mellin transform and its properties with examples and applications to integral and partial differential equations. Several simple lemmas and theorems dealing with general properties of the generalized Mellin transform are proved. The main focus of this study is to develop the method of the generalized Mellin transform to solve partial differential equations and integral equations in applied mathematics.

**Keywords:** Fourier transform, Mellin transform, generalized Mellin transform, integral and partial differential equations.

### References:

- [1] D. Brown, N. Dernek, O. Yürekli, "Identities for the  $\varepsilon_{2,1}$  Transform and Their Applications", *Appl. Math. Comput.*, 187(2007), 1557-1566.
- [2] L. Debnath, D. Bhatta, "Integral Transforms and Their Applications", Second Edition, Chapman&Hall, (2006).
- [3] N. Dernek, F. Aylıkçı, O. Yürekli, "New Identities on the Generalized Exponential and Mellin Integral Transformations and Their Applications"(to appear)
- [4] N. Dernek, F. Aylıkçı, S. Kıvrak, "An Alternative Technique for Solving Ordinary Differential Equations", *Konuralp J. Math.* Vol 4:1,2016, 68-79.
- [5] A. Erdelyi, W. Magnus, F. Oberhettinger, and F.G. Tricomi, "Tables of Integral Transforms", Vol. I, Vol II, New York: McGraw Hill, 1954.
- [6] N. Lebedev, *Special Functions and Their Applications*, Prentice Hall, 1965.

## APPROXIMATE SOLUTION FOR SOLVING THE SINE-GORDON EQUATION BY REDUCED DIFFERENTIAL TRANSFORM METHOD WITH FIXED GRID SIZE

Sema SERVİ<sup>1</sup>, Yıldırım KESKİN<sup>2</sup>, Galip OTURANÇ<sup>2</sup>

<sup>1</sup>*Vocational School of Technical Sciences, Selcuk University,  
Konya/TURKEY*

[semaservi@selcuk.edu.tr](mailto:semaservi@selcuk.edu.tr)

<sup>2</sup>*Department of Mathematics, Science Faculty, Selcuk University,  
Konya/TURKEY*

[ykeskin@selcuk.edu.tr](mailto:ykeskin@selcuk.edu.tr), [goturanc@selcuk.edu.tr](mailto:goturanc@selcuk.edu.tr)

**Abstract:** In this study, we applied relatively, a new algorithm to the reduced transformation method [3] for solving sine-Gordon equation and RDTM with fixed grid size was formed [1-2]. This method is an effective method for solving partial differentiable equations in literature. To present the RDTM with fixed grid size's effectiveness an example is given [4-5]. In the application part, we compare numerical results with the exact solutions and solutions of the variational iteration method (VIM).

**Keywords:** Reduced differential transform method, Variational iteration method, sine-Gordon equations.

### References:

- [1] M. Jang, C. Chen, Y. Liy, On solving the initial-value problems using the differential transformation method, *Applied Mathematics and Computation*, 115 (2000) 145-160.
- [2] Kurnaz, Aydin, and Galip Oturanç. "The differential transform approximation for the system of ordinary differential equations." *International Journal of Computer Mathematics* 82.6 (2005): 709-719.
- [3] Keskin Y. Oturanç G., "Reduced differential transform method for partial differential equations", *International Journal of Nonlinear Sciences and Numerical Simulation*, 10,6, 741-750, 2009
- [4] Batiha, B., Mohd Salmi Md Noorani, and Ishak Hashim. "Numerical solution of sine-Gordon equation by variational iteration method." *Physics Letters A* 370.5 (2007): 437-440.
- [5] Keskin, Yıldırım, İbrahim Çağlar, and Ayşe Betül Koç. "Numerical Solution of Sine-Gordon Equation by Reduced Differential Transform Method." *Proceedings of the World Congress on Engineering*. Vol. 1. 2011.



## EULER SPIRALS

Semra SARAÇOĞLU ÇELİK, Erhan GÜLER, Ömer KİŞİ

*Bartın University, Faculty of Science, Department of Mathematics, 74100,*

*Bartın, Turkey*

*ssaracoglu@bartin.edu.tr ,*

*eguler@bartin.edu.tr ,*

*okisi@bartin.edu.tr*

**Abstract:** In this talk, we give some characterizations of Euler spirals. We show the relations between Euler spirals and Bertrand curves. Moreover, many different approaches about Euler spirals are presented in three dimensional Euclidean space and Minkowski space.

**Keywords:** Euler spirals, Bertrand curves, curvature.

## SIMPLE EQUATION METHOD FOR TRAVELING WAVESOLUTIONS OF SOME NONLINEAR PARTIAL DIFFERENTIAL EQUATIONS

Serbay DURAN<sup>1</sup>, Ibrahim E. INAN<sup>2</sup>, Yavuz UĞURLU<sup>3</sup>

*<sup>1</sup>Faculty of Education, Adıyaman University,  
Adıyaman/TURKEY*

*[serbayduran@hotmail.com](mailto:serbayduran@hotmail.com)*

*<sup>2</sup>Faculty of Education, Firat University,  
Elazığ/TURKEY*

*[ieinan@yahoo.com](mailto:ieinan@yahoo.com)*

*<sup>3</sup>Department of Mathematics, Firat University,  
Elazığ/TURKEY*

*[matematikci\\_23@yahoo.com.tr](mailto:matematikci_23@yahoo.com.tr)*

**Abstract:** In this study, we study simple equation method for traveling wavesolutions of the Dodd-Bullough-Mikhailov (DBM) equation, the Liouville equation and fifth order KdV equation.

**Keywords:**Traveling wavesolutions, simple equation method, Dodd-Bullough-Mikhailov (DBM) equation, Liouville equation, fifth order KdV equation.

### References:

- [1] L. Debnath, Nonlinear Partial Differential Equations for Scientist and Engineers, Birkhauser, Boston, MA, 1997.
- [2] N.A. Kudryashov, "Simple equation method to look for exact solutions of nonlinear differential equations", Chaos, Solitons& Fractals, 24 (2005), 1217–1231
- [3] A.M. Wazwaz, "A study of nonlinear dispersive equations with solitary-wave solutions having compact support", Mathematics and Computers in Simulation, 56 (2001), 269-276.

## ENTROPY CONVERGENCE FOR SEQUENCES OF FUZZY NUMBERS

Sevda ATPINAR<sup>1</sup>, Mehmet ŞENGÖNÜL<sup>2</sup>

<sup>1,2</sup>*Department of Mathematics, Nevşehir H. B. V University*

*Nevşehir/TURKEY*

[sevdaatpinar@nevsehir.edu.tr](mailto:sevdaatpinar@nevsehir.edu.tr)

<sup>2</sup>*Department of Mathematics, Nevşehir H. B. V University*

*Nevşehir/TURKEY*

[msengonul@yahoo.com](mailto:msengonul@yahoo.com)

**Abstract:**In this presentation, we have introduced entropy convergence (E-convergence) for sequence of fuzzy numbers and proved some theorems about entropy convergent sequences spaces.

**Keywords:** Entropy, fuzzy numbers, sequence of fuzzy numbers.

### References:

- [1] M.Şengönül, "An Application of Fuzzy Sets to Veterinary Medicine", *Theory and Applications of Mathematics & Computer Science* 6 (1) (2016) 1–12.
- [2] T. C. Chin, "The entropy difference of triangular fuzzy numbers with arithmetic operations", *Journal of "ir.lib.kuas.edu.tw"* (1), 53–75.
- [3] E. Czogala and J. Leski, "Entropy and Energy Measures of Fuzziness ECG Signal Processing", *Fuzzy Systems in Medicine*. Springer-Verlag Berlin Heidelberg, (2000).
- [4] A. de Luca and S. Termini, "A Definiton of a Nonprobabilistic Entropy in the Setting of Fuzzy Sets Theory", *Information and Control* 20(1), 301–312.

## ENTROPY VALUE OF QRS COMPLEX IN THE ELECTROCARDIOGRAPHY

Sevda ATPINAR, Mehmet ŞENOL

*Department of Mathematics, Nevşehir H. B. V University,  
Nevşehir/TURKEY*

[sevdaatpinar@nevsehir.edu.tr](mailto:sevdaatpinar@nevsehir.edu.tr)  
[msenol@nevsehir.edu.tr](mailto:msenol@nevsehir.edu.tr)

**Abstract:** In this presentation, we introduce entropy concept in fuzzy sets to QRS complex in ECG. QRS complex is maybe the most prominent component of ECG and mostly related to myocardial infarction (MI) state. Negative and positive deflections in QRS complex employed as a fuzzy set and entropies of QRS complex belong patients with cardiac diseases compared with control group and some results acquired.

**Keywords:** Entropy, QRS complex, ECG, Fuzzy numbers, Fuzzy sets

### References:

- [1] M.Şengönül, "An Application of Fuzzy Sets to Veterinary Medicine", *Theory and Applications of Mathematics & Computer Science* 6 (1) (2016) 1–12.
- [2] T. C. Chin, "The entropy difference of triangular fuzzy numbers with arithmetic operations", *Journal of "ir.lib.kuas.edu.tw"* (1), 53–75.
- [3] E. Czogala and J. Leski, "Entropy and Energy Measures of Fuzziness ECG Signal Processing", *Fuzzy Systems in Medicine*. Springer-Verlag Berlin Heidelberg, (2000).
- [4] A. de Luca and S. Termini, "A Definition of a Nonprobabilistic Entropy in the Setting of Fuzzy Sets Theory", *Information and Control* 20(1), 301–312.

## OPTIMIZATION OF HIGHER ORDER POLYHEDRAL DISCRETE AND DIFFERENTIAL INCLUSIONS

Sevilay DEMİR<sup>1</sup>, Elimhan MAHMUDOĞ<sup>2</sup>

<sup>1</sup>*Department of Mathematics, İstanbul University,  
İstanbul/TURKEY*

[sevilay.demir@istanbul.edu.tr](mailto:sevilay.demir@istanbul.edu.tr)

<sup>2</sup>*Department of Mathematical Engineering, İstanbul Technical University,  
İstanbul/TURKEY*

[elimhan22@yahoo.com](mailto:elimhan22@yahoo.com)

**Abstract:** In this presentation, we concern with one of the difficult and interesting fields-higher order polyhedral optimization described by ordinary discrete and differential inclusions. The optimality problem for higher order discrete inclusions are reduced to the problem with finite number of geometric constraints. By using higher order difference operators with problem for higher order differential inclusions, we associate the discrete-approximation problem, approximating it. The derivation of sufficient conditions for optimality of higher order differential inclusions is implemented by passing to the formal limit as the discrete steps tend to zero. Finally we prove the sufficient conditions of optimality for higher order polyhedral differential inclusions with boundary value constraint.

**Keywords:** Polyhedral, differential inclusions, Euler-Lagrange inclusion.

### References:

- [1] J.-P. Aubin, A. Cellina, "Differential Inclusions", Springer-Verlag, Grundlehren der Math.Wiss, (1984).
- [2] E.N. Mahmudov, "Approximation and Optimization of Discrete and Differential inclusions", Elsevier, (2011).
- [3] B.S. Mordukhovich, "Variational Analysis and Generalized Differentiation Vols.I and II", Springer-Verlag Berlin Heidelberg (2006).
- [4] R.T. Rockafellar, "Variational Analysis and Its Applications", Preface to a special issue of Set-Valued Analysis, 12(2002), 1-4.

## WEIGHTED APPROXIMATION BY NONLINEAR DOUBLE SINGULAR INTEGRAL OPERATORS

Gumrah UYSAL<sup>1</sup>, Sevilay KIRCI SERENBAY<sup>2</sup> and Ertan İBIKLİ<sup>3</sup>

<sup>1</sup>*Department of Mathematics, Karabük University,  
Karabük/TURKEY*

[guysal@karabuk.edu.tr](mailto:guysal@karabuk.edu.tr)

<sup>2</sup>*Department of Mathematical Education, Başkent University,  
Ankara/TURKEY*

[sevilaykirci@gmail.com](mailto:sevilaykirci@gmail.com)

<sup>3</sup>*Department of Mathematics, Ankara University,  
Ankara/TURKEY*

[Ertan.Ibikli@ankara.edu.tr](mailto:Ertan.Ibikli@ankara.edu.tr)

**Abstract:** In this work, we present some theorems on pointwise convergence of nonlinear double singular integral operators depending on three parameters in weighted sense.

**Keywords:** Pointwise Convergence, degree of pointwise convergence, nonlinear double singular integral operator.

### References:

- [1] R. Taberski, "Singular integrals depending on two parameters", *Roczniki Polskiego Towarzystwa Matematycznego, Seria I. Prace Matematyczne*, VII, 1962.
- [2] R. Taberski, "On double integrals and Fourier Series", *Ann. Polon. Math.* 15 (1964) 97-115.
- [3] J. Musielak, "On Some Approximation Problems in Modular Spaces, In Constructive Function Theory 1981 (Proc. Int. Conf. Varna, June 1-5, 1981)", *Publ. House Bulgarian Acad. Sci., Sofia* (1983) 455-461.
- [4] T. Swiderski and E. Wachnicki, "Nonlinear Singular Integrals depending on two parameters", *Comment. Math. XL*, (2000) 181-189.

## ON STATISTICAL CONVERGENCE OF SEQUENCES OF FUNCTIONS IN 2-NORMED SPACES

Sevim YEGÜL and Erdiñ DÜNDAR

*Department of Mathematics, AfyonKocatepe University,  
Afyonkarahisar/TURKEY  
[sevimyegull@gmail.com](mailto:sevimyegull@gmail.com), [edundar@aku.edu.tr](mailto:edundar@aku.edu.tr)*

**Abstract:** Statistical convergence and statistical Cauchy sequence in 2-normed spaces were studied by Gürdal and Pehlivan [M. Gürdal, S. Pehlivan, Statistical convergence in 2-normed spaces, Southeast Asian Bulletin of Mathematics, (33) (2009), 257-264]. In this paper, we get analogous results of statistical convergence and statistical Cauchy sequence of functions and investigate some properties and relationships between them in 2-normed spaces.

**Keywords:** Statistical convergence, Sequence of functions, Statistical Cauchy sequence, 2-normed spaces.

### References:

- [1] M. Gürdal, S. Pehlivan, Statistical convergence in 2-normed spaces, Southeast Asian Bulletin of Mathematics, (33) (2009), 257-264.
- [2] M. Gürdal, S. Pehlivan, The statistical convergence in 2-Banach spaces, Thai. J. Math., 2(1) (2004), 107-113.

## SOME DOUBLE SEQUENCE SPACES OF INTERVAL NUMBERS

Sibel YASEMİN GÖLBOL<sup>1</sup>, UğurDEĞER<sup>2</sup>, Ayhan ESI<sup>3</sup>

<sup>1,2</sup>Department of Mathematics, Mersin University,  
Mersin/TURKEY

[sibelyasemin@mersin.edu.tr](mailto:sibelyasemin@mersin.edu.tr), [degpar@hotmail.com](mailto:degpar@hotmail.com)

<sup>3</sup>Department of Mathematics, Adiyaman University,  
Adiyaman/TURKEY  
[aesi23@hotmail.com](mailto:aesi23@hotmail.com)

**Abstract:** Interval arithmetic was first suggested by Dwyer in [3]. In [2], Chiao introduced the sequences of interval numbers and defined usual convergence of sequences of interval number. Esi and Yasemin in [1] defined the metric spaces  $\bar{c}_0(f, p, s)$ ,  $\bar{c}(f, p, s)$ ,  $\bar{l}_\infty(f, p, s)$  and  $\bar{l}_p(f, p, s)$  of sequences of interval numbers by a modulus function. In this study, we consider a generalization for double sequences of these metric spaces by taking a  $\psi$  function, satisfying the following conditions, instead of  $s$  parameter. For this aim, let  $\psi(k, l)$  be a positive function for all  $k, l \in \mathbb{N}$  such that (i)  $\lim_{k, l \rightarrow \infty} \psi(k, l) = 0$  and (ii)  $\Delta_2 \psi(k, l) = \psi(k-1, l-1) - 2\psi(k, l) + \psi(k+1, l+1) \geq 0$  or  $\psi(k, l) = 1$ .

Therefore, according to class of functions which satisfying the conditions (i) and (ii) we deal with the metric spaces  $\bar{c}_0^2(f, p, \psi)$ ,  $\bar{c}^2(f, p, \psi)$ ,  $\bar{l}_\infty^2(f, p, \psi)$  and  $\bar{l}_p^2(f, p, \psi)$  of double sequences of interval numbers defined by a modulus function and state some topological theorems and inclusions related to these spaces.

**Keywords:** Interval numbers, complete metric spaces, modulus function.

### References:

- [1] A.Esi, S. Yasemin Gölbol, "Some spaces of sequences of interval numbers defined by a modulus function", Global Journal of Mathematical Analysis, **2**, (1)(2014), 11-16.
- [2] K. P. Chiao, "Fundamental properties of interval vector max-norm", Tamsui Oxford Journal of Mathematics, **18**, (2)(2002), 219-233.
- [3] P. S. Dwyer, Linear Computation, Wiley, New York, 1951. equations, *Global Jour. Math. Anal.* 1 (1-2) (2007), 91-108.

## APPROXIMATING SOLUTIONS OF NONLINEAR ABSTRACT MEASURE DIFFERENTIAL EQUATIONS

Sidheshwar BELLALE<sup>1</sup>, Bapurao DHAGE<sup>2</sup>

<sup>1</sup>Department of Mathematics, Dayanand Science College, Latur  
Maharashtra, INDIA  
[sidhesh.bellale@gmail.com](mailto:sidhesh.bellale@gmail.com)

<sup>2</sup>Kasubai, Gurukul Colony, Ahmedpur, Dist: Latur  
Maharashtra, INDIA  
[bcdhage@gmail.com](mailto:bcdhage@gmail.com)

**Abstract:** In this paper the existence theorem as well as approximations of the solutions of initial value problems of first order nonlinear abstract measure differential equations is proved under the mixed generalized Lipschitz and Caratheodory conditions. We rely our results on a hybrid fixed point theorem of Dhage in partially ordered normed linear spaces. The abstract measure differential equations in which ordinary derivative is replaced by the derivative of set functions, namely, the Radon-Nokodym derivative of a measure with respect to another measure.

$$\frac{dp}{d\mu} = f(x, p(\overline{S_x})) + g(x, p(\overline{S_x})) \quad (1)$$
$$P(E) = q(E), E \in M_0. \text{ a.e. } [\mu] \text{ on } \overline{x_0 z}$$
$$\mu, f, g : S_z \times R \rightarrow R$$

The existence of the solutions to (1) is proved by Dhage and Bellale by using a new nonlinear alternative of Leray-Schauder type developed in this paper. Also we apply a approximation solution Dhage's hybrid fixed point theory for nonlinear mapping in partially ordered metric spaces.

**Keywords:** Approximating solution, Abstract Measure differential equation, Initial value Problems, Hybrid fixed point theorem

### References:

- [1] J. Banas , K. Goebel, Measures of non compactness in Banach space, in: *Lecture Notes in pure and Applied Mathematics* , Vol 60 , Dekker, New York, 1980.
- [2] P. C. Das and R. R. Sharma, Existence and stability of measur differential equations, *Zech. Math. J.*, 22 (1972), 145 -158.
- [3] B. C. Dhage, Hybrid fixed point thory in ordrd normed linear spaces and applications to the functional integral equations, *Differ. Equ Appl.* 5(2013), 155-184.
- [4] S. S Bellale and B. C. Dhage Abstract measure integro-differential equations, *Global Jour. Math. Anal.* 1 (1-2) (2007), 91-108



## ON $\lambda$ -CONVERGENCE OF SECOND ORDER ANDNEW BANACH SPACES

Sinan ERCAN<sup>1</sup>, Çiğdem A. BEKTAŞ<sup>2</sup>

<sup>1</sup>*Department of Mathematics, Firat University,  
Elazığ/TURKEY*

[sinanercan45@gmail.com](mailto:sinanercan45@gmail.com)

<sup>2</sup>*Department of Mathematics, Firat University,  
Elazığ/TURKEY*

[cbektas@firat.edu.tr](mailto:cbektas@firat.edu.tr)

**Abstract:** The notion of  $\lambda$ -convergence and  $\lambda$ -boundedness were given by Mursaleen and Noman in [4]. In this presentation we introduce the  $\lambda$ -convergence and  $\lambda$ -boundedness of second order. We examine the relation between of the ordinary convergence and  $\lambda$ -convergence of second order. Then we define new BK-spaces of non-absolute type. We investigate some topological properties and establish some inclusion relations concerning with those spaces.

**Keywords:** BK-spaces, Difference sequence spaces.

### References:

- [1] F. Moricz, On  $\Lambda$ -strong convergence of numerical sequences and Fourier series, *Acta Math. Hung.*, 54(3-4), 1989, 319-327.
- [2] N. L. Braha, F. Başar, On the domain of the triangle  $A(\lambda)$  on the spaces of null, convergent and bounded sequences, *Abstr. Appl. Anal.*, Volume 2013, Article ID 476363.
- [3] I. J. Maddox, *Elements of Functional Analysis*, 2nd ed., The University Press, Cambridge, 1988.
- [4] M. Mursaleen, A. K. Noman, On the spaces of  $\lambda$ -convergent sequences and bounded sequences, *Thai J. Math*, Volume 8, Number 2, 2010, 311-329.
- [5] M. Mursaleen, A. K. Noman, On some new difference sequence spaces of non-absolute type, *Math. Comput. Mod.*, 52 (2010), 603-617.

## COMPARISON OF SOME SET OPEN AND UNIFORM TOPOLOGIES ON $C(X,Y)$

Smail KELAIAIA<sup>1</sup>, LamiaHARKAT<sup>2</sup>

<sup>1</sup>*Department of Mathematics, Annaba University,  
Annaba/ALGERIA*

[kelaiaiasmail@yahoo.fr](mailto:kelaiaiasmail@yahoo.fr)

<sup>2</sup>*Department of Mathematical Engineering, Souk-Ahras University,  
Souk-Ahras/ALGERIA*

[Harkat\\_lamia@yahoo.fr](mailto:Harkat_lamia@yahoo.fr)

**Abstract:** Let  $X, Y$  be topological spaces and  $C(X, Y)$  be the set of all continuous functions from  $X$  to  $Y$ . The set  $C(X, Y)$  can be endowed with set open or uniform topologies on particular families of subsets of  $X$ . We give here a comparison between some of these topologies and give a criterion for their coincidence.

**Keywords:** Function spaces, set open topology, uniform topology,  $Y$ -compact sets.

### References:

- [1] A. Bouchair, S. Kelaiaia, "Some results on  $C(X)$  with set open topology", *Math. Reports*, 17(67), 2(2015), 167-182.
- [2] A. Bouchair, S. Kelaiaia, "Comparison of some set open topologies on  $C(X, Y)$ ", *Top. Appl.* 178(2014), 352-359.
- [3] S. E. Nokhrin, A. V. Osipov, "On the coincidence of the set open and uniform topologies", *Proc. Steklov. Inst. Supp.* 3(2009), 184-181.
- [4] S. Onal, C. Vural, "Some cardinal invariants on the space  $C(X, Y)$ ", *Top. Appl.* 150(2005), 255-265.

## SOLUTION OF A LINEAR MULTIOBJECTIVE PROBLEM BY THE ADAPTIVE METHOD

Zohra Sabrina DELHOUM<sup>1</sup>, Sonia RADJEF<sup>2</sup> and Fatima BOUDAOU<sup>3</sup>

<sup>1,3</sup>*Department of Mathematics, Faculty of Sciences, Mathematics et Applications  
Laboratory, University Oran 1 Ahmed Ben Bella, Oran, Algeria,*

<sup>1</sup>[delhoum.zahra@yahoo.fr](mailto:delhoum.zahra@yahoo.fr)<sup>3</sup>[boudaoud@yahoo.fr](mailto:boudaoud@yahoo.fr)

*Department of Mathematics, Faculty of*

*Mathematics and Computer Science, University USTOMB, Oran 31000, Algeria  
[soniaradjef@yahoo.fr](mailto:soniaradjef@yahoo.fr)*

**Abstract:** In this presentation, we introduce a new method to solve a linear multiobjective programming problem with bounded variables using the principle of the adaptive method.

We propose a procedure for finding an initial efficient point without having to calculate a feasible point, and we develop a method to find efficient points, weakly efficient points, and subefficient points.

Then we give a detailed algorithm for computing all efficient. A numerical example is utilized to illustrate the applicability of the proposed method.

**Keywords:** Linear program, multiobjective linear programming, bounded variables, suboptimality criterion, adaptive method, efficient points, subefficient points.

### References:

- [1] R. Gabasov, "Adaptive method of linear programming", Preprints of the university of Karlsruhe, Germany (1993).
- [2] Sonia Radjef and M.O Bibi, "A New Algorithm for Linear Multiobjective Programming Problems with Bounded Variables", Arabian Journal of Mathematics (2014), DOI 10.1007/s40065-013-0094-x.
- [3] Sonia Radjef and M.O Bibi, "An effective Generalization of the Direct Support Method", Mathematical Problems of Engineering 2011; Article ID 374390, 18 pages, doi:10.1155/2011/374390.
- [4] J.G. Ecker and I.A. Kouada, "Finding all efficient extreme points for multiple objective linear programs", Mathematical Programming 14(1978), 249-261.

## GROUPS WHOSE PROPER SUBGROUPS ARE HYPERCENTRAL

SouadAZRA and Nadir TRABELSI

**Abstract:** Let  $X$  be a class of groups. A group is said to be minimal non- $X$  if it is not an  $X$ -group, while all its proper subgroups belong to  $X$ . We will denote minimal non  $X$ -groups by MNX-groups. Many results have been obtained on MNX-groups, for various choices of  $X$  ( see [1], [2], [3], [4]). In particular, in [2] a complete description infinitely generated MNN groups, where  $N$  denotes the class of nilpotent groups. Xu [3] has described the structure of infinitely generated MNFN-groups.

To ease the discussion we also introduce some abbreviations. A group  $G$  is said to be MNZA-group if all its proper subgroups are hypercentral, but  $G$  itself is not. Here we proved if  $G$  is a finitely generated MNZA-group is a perfect group which has no proper subgroup of finite index and such that  $G/\text{Frat}(G)$  is an infinite simple group, where  $\text{Frat}(G)$  stands for Frattini subgroup of  $G$ . In section 2; we discuss infinitely generated MNZA-groups. The following results are obtained.

**Keywords:** Hypercentral groups, Minimal non-nilpotent groups.

### References:

- [1] A.Badis and N.Trabelsi, Groups with few non-(locally finite)-by-Baer) subgroups. Note Math. 30(2010)no.2.107-111
- [2] M.F.Newman and J.Wiegold, Groups with many nilpotent subgroups, Archiv der Math 15(1964),241-250..
- [3] M.Xu, Groups whose proper subgroups are finite-by-nilpotent, Arch. Math. 66(1996),353-359..

## SOLUTION OF FRACTIONAL ORDER ORDINARY DIFFERENTIAL EQUATION: A NUMERICAL APPROACH

Soumen SHAW

*Department of Mathematics,  
Indian Institute of Engineering Science and Technology, Shibpur. India.*

**Abstract:** In this article a fractional order ordinary differential equation (FDE) is attempted to solve applying a new geometrical approach. We establish some new criteria to obtain the solution of a fractional order differential equation with integer order initial condition. Based on the geometrical interpretation of the fractional derivatives, the solution curve is approximated numerically. Two special phenomena are employed for concave upward and downward curves.

**Keywords:** Fractional order ordinary differential equation; geometrical interpretation; numerical solution.

## ERROR ANALYSIS FOR EXTENDED DISCONTINUOUS GALERKIN(XDG) METHODS

Suayip TOPRAKSEVEN

*Department of Computer Engineering, ArtvinCoruh University,  
Artvin/TURKEY*

[topraksp@artvin.edu.tr](mailto:topraksp@artvin.edu.tr)

**Abstract:**In this presentation we introduce an extended discontinuous Galerkin (XDG) method. Our XDG scheme is based on the Babuska-Zlamal approach and we apply it to a class of prototype elliptic boundary value problems that have solutions consisting of smooth functions perturbed by a set of high frequency modes which occupy a narrow frequency band. The XDG scheme we study is enriched by trigonometric functions that cover the range of these perturbations. A theoretical error analysis is provided that shows the method converges and gives specifics on its accuracy. These error estimates are provided in terms of the degree of the polynomials used in the approximation and the largest high frequency.

**Keywords:** Discontinuous Galerkin (DG), Babushka-Zlamal DG scheme, High Frequency, Extended Discontinuous Galerkin.

### References:

- [1] [BZ] I. Babuska and M. Zlamal, Nonconforming elements in the finite element method with penalty, SIAM J. Num. Anal., 10 (1973).
- [2] [BS] S.C. Brenner and L.R. Scott, The Mathematical Theory of Finite Element Methods, Springer-Verlag (1994). V. Berinde, "On the approximation of fixed points of weak contractive mappings", Carpathian J. Math, 19(2003), 7-22.
- [3] [CQ] S.U. Chirputkar and D. Qian, Coupled Atomistic/Continuum Simulation based on an Extended Space-Time Finite Element Method, CMES, 850 (2008), 1-18.
- [4] [H] R. Heinzle, Method of Babuska-Zlamal, Lecture Notes at <http://www.ricam.oeaw.ac.at/>.
- [5] [T] S. Toprakseven, Theoretical Error Analysis and Computations with XDG, Dissertation at University of Cincinnati (2014).

## ON A $C^*$ - MODULE NORMED SPACE AND ITS TOPOLOGICAL PROPERTIES

SUPAMA, Atok ZULIJANTO, Imam SOLEKHUDIN, SUMARDI

*Department of Mathematics, Gadjah Mada University,  
Yogyakarta/INDONESIA  
[supama@ugm.ac.id](mailto:supama@ugm.ac.id)  
[atokzulijanto@yahoo.com](mailto:atokzulijanto@yahoo.com)  
[imams@ugm.ac.id](mailto:imams@ugm.ac.id)  
[mardimath@ugm.ac.id](mailto:mardimath@ugm.ac.id)*

**Abstract:** One knows that Hilbert spaces have important roles in many area, such as statistics, quantum mechanics, etc. In 1953, Irving Kaplansky generalized the notion of Hilbert spaces. He introduced  $C^*$ -module Hilbert spaces by defining an inner product like function on a left module, which take values in a  $C^*$ -algebra.

In this work, inspired by the Kaplansky's, we construct a notion of a  $C^*$ -module normed space. Further, we observe some topological properties of the space as well.

**Keywords:**  $C^*$ -algebra, left-module, positive element, lattice.

### References:

- [1] Bourbaki, N., "Integration I", Springer-Verlag (2004)
- [2] Budayana, I.N., "Fixed Point Theorems in Partial Cone Metric Spaces", M.Sc thesis, GadjahMada University, Yogyakarta, Indonesia (2015).
- [3] Chi-Keung Ng., "Regular normed bimodules", <http://arxiv.org/abs/math/0609159v1>, (2006).
- [4] Cornford, D., "Geographic Information Systems", Computer Science, Aston University Birmingham B4 7ET, (2005) <http://www.cs.aston.ac.uk/>.
- [5] Dennery, P. and Krzywicki, A., "Mathematics for Physicists", Courier Dover Publications, (1996).
- [6] Dudley, R.M., "Real analysis and probability", The Wadsworth and Brooks/Cole Mathematics Series, Pacific Grove, CA, (1989).
- [7] Guo, T.X. and Zhu, H.L., "A Characterization of Continuous Module Homomorphisms on Random Semi-Normed Modules and Its Applications", Acta Mathematica Sinica, 19 (1) (2003), 201--208.

## NUMERICAL SOLUTIONS OF SINGULARLY PERTURBED TURNING POINT PROBLEMS EXHIBITING AN INTERIOR LAYER VIA MAGNUS SERIES EXPANSION METHOD

Sure KÖME, Aytekin ERYILMAZ

*Department of Mathematics, NevşehirHacıBektaşVeliUniversity,  
Nevşehir/TURKEY*

[surekome@gmail.com](mailto:surekome@gmail.com), [eryilmazaytekin@gmail.com](mailto:eryilmazaytekin@gmail.com)

**Abstract:** In this presentation, we present the numerical solutions of singularly perturbed turning point problems exhibiting an interior layer, which is near the turning point, by means of the Magnus series expansion method. The method is applied to three different turning point problems with different orders and then numerical results are illustrated with figures in detail. Finally, we show that the higher order method is more powerful than the lower order one for solving singularly perturbed turning point problems exhibiting an interior layer by comparing the numerical results.

**Keywords:** Magnus Series Expansion Method, Singular Perturbation, Turning Point.

### References:

- [1] C. M. Bender, S. A. Orszag, "Advanced Mathematical Methods for Scientists and Engineers", McGraw-Hill, New York, (1978).
- [2] W. Magnus, "On the exponential solution of differential equations for a linear operator", *Comm. Pure and Appl. Math.*, 7(1954), 639-673.
- [3] A. Iserles, H. Munthe-Kaas, S. Norsett, A. Zanna, "Lie-group methods", *Acta Numerica*, 9(2000), 215-365.
- [4] A. Iserles, S. P. Norsett, "On the solution of linear differential equations in Lie groups", *Phil. Trans. R. Soc. A*, 357(1999), 983-1019.

## ON GENERALIZATION ABSOLUTE RIESZ SUMMABILITY FACTORS OF FOURIER SERIES

Hikmet Seyhan ÖZARSLAN, Şebnem YILDIZ

<sup>1</sup>Department of Mathematics, Erciyes University,  
Kayseri/TURKEY

[seyhan@erciyes.edu.tr](mailto:seyhan@erciyes.edu.tr)

<sup>2</sup>Department of Mathematics, Ahi Evran University, Kırşehir/TURKEY

[sebnemyildiz@ahievran.edu.tr](mailto:sebnemyildiz@ahievran.edu.tr)

**Abstract:** In this presentation, we define two general theorem on  $|A, p_n|_k$  summability factors of Fourier series by using matrix transformation undersuitable conditions. By using this theorem, we obtain some new results concerning other important summability methods.

**Keywords:** Summability factors, Absolute matrix summability, Fourier series, Hölder inequality, Minkowski inequality.

### References:

- [1] G. H. Hardy, "Divergent Series", Oxford Univ. Press, Oxford (1949).
- [2] H. Bor, "On two summability methods", Math. Proc. Cambridge Philos Soc. 97 (1985), 147-149.
- [3] H. Bor, "Local property of  $|\overline{N}, p_n|_k$  summability of factored Fourier series", Bull. Inst. Math. Acad. Sinica, 17 (1989), 165-170.
- [4] H. Bor, "Multipliers for  $|\overline{N}, p_n|_k$  summability of Fourier series", Bull. Inst. Math. Acad. Sinica, 17 (1989), 285-290.
- [5] H. Bor, "On the local property  $|\overline{N}, p_n|_k$  summability of factored Fourier series", J. Math. Anal. Appl., 163 (1992), 220-226.
- [6] H. Bor, "On local property of  $|\overline{N}, p_n; \delta|_k$  summability of factored Fourier series", J. Math. Anal. Appl., 179 (1993), 646-649.
- [7] H. Bor, "On the local property of factored Fourier series", Z. Anal. Adwend. 16 (1997), 769-773.

### Acknowledges.

This work supported by the Ahi Evran University Scientific Research Projects Coordination Unit. Project Number: FEF.E2.16.025.



## SPECTRAL SINGULARITIES OF IMPULSIVE DISCRETE DIRAC OPERATORS

Şerifenur CEBESoy, Elgiz BAIRAMOV, Şeyda SOLMAZ

*Department of Mathematics, Ankara University,  
Ankara/TURKEY*

[s.cebesoy@hotmail.com](mailto:s.cebesoy@hotmail.com), [bairamov@science.ankara.edu.tr](mailto:bairamov@science.ankara.edu.tr),  
[seydasolmaz@hotmail.com.tr](mailto:seydasolmaz@hotmail.com.tr)

**Abstract:** In this presentation, we consider the operator  $L$  generated in  $L_2(\mathbb{Z}, C^2)$  by the following Discrete Dirac equation for  $\forall n \in \mathbb{Z}\{-1,0,1\}$  için

$$\begin{aligned}y_{n+1}^{(2)} - y_n^{(2)} &= \lambda y_n^{(1)} \\ -y_n^{(1)} + y_{n-1}^{(1)} &= \lambda y_n^{(2)}\end{aligned}$$

with impulsive condition

$$\begin{pmatrix} y_1^{(1)} \\ y_1^{(2)} \end{pmatrix} = \begin{pmatrix} a & b \\ c & d \end{pmatrix} \begin{pmatrix} y_{-1}^{(1)} \\ y_{-1}^{(2)} \end{pmatrix}$$

where  $a, b, c, d$  are complex numbers. We investigate eigenvalues and spectral singularities of  $L$  depending on the choice of the constants  $a, b, c, d$  and generalize the results obtained in [1-2] to the discrete Dirac operator  $L$ . Note that, the spectral theory of  $L$  without impulsive conditions was investigated in detail in [3-4].

**Keywords:** Discrete Dirac equation, Discrete Dirac operator, spectral singularities, eigenvalues, interaction point.

### References:

- [1] A. Mostafazadeh, H. Mehri-Dehnavi, "Spectral singularities, biorthonormal systems and a two-parameter family of complex point interactions", *J. Phys. A: Math. Theory*, 42 (2009), 125303 (27 pp).
- [2] A. Mostafazadeh, "Spectral singularities of a general point interaction", *J. Phys. A: Math. Theory*, 44 (2011), 375302 (9 pp).
- [3] E. Bairamov, A. O.Çelebi, "Spectrum and spectral expansion for the non-selfadjoint discrete Dirac operators", *Quart. J. Math. Oxford Ser. (2)* 50 (1999), no. 200, 371--384.
- [4] M. Adivar, E. Bairamov, "Spectral properties of non-selfadjoint difference operators.", *J. Math. Anal. Appl.* 261 (2001), no. 2, 461--478.

## FIXED POINT RESULTS FOR BERINDE-TYPE ALMOST CONTRACTIONS ON $G_p$ -METRIC SPACES

Şeyma ÇEVİK<sup>1</sup>, Hasan FURKAN<sup>2</sup>

<sup>1</sup>*Department of Mathematics, KahramanmaraşSütçü İmam University,  
Kahramanmaraş/TURKEY  
[seymacevik263@gmail.com](mailto:seymacevik263@gmail.com)*

<sup>2</sup>*Department of Mathematics, KahramanmaraşSütçü İmam  
University, Kahramanmaraş/TURKEY  
[hasanfurkan@hotmail.com](mailto:hasanfurkan@hotmail.com)*

**Abstract:** In this paper, we define the concepts of  $(\delta, L)$ -almost contraction,  $(\varphi, L)$ -almost contraction and Ćirić-type almost contraction in the sense of Berinde in  $G_p$ -complete  $G_p$ -metric space. Furthermore, we prove the existence of fixed points and common fixed points of mappings satisfying Berinde type contractions stated above and also provide the conditions which are necessary for the uniqueness of fixed points and common fixed points. Consequently, we obtain the generalizations of comparable results in the literature. In addition, we introduce a few examples to ensure the existence of our results.

**Keywords:** Fixed point, common fixed point,  $G_p$ -metric space, Berinde-type almost contractions.

### References:

- [1] M. R. A. Zand, A. D. Nezhad, "A generalization of partial metric spaces", *J. Contemp. Appl. Math.*, 24, 86-93, (2011).
- [2] Aydi H., Karapınar E. and Salimi P., "Some fixed point results in  $G_p$ -metric spaces", *J. Appl. Math.*, 2012, Article ID 891713, 16 pages, doi:10.1155/2012/891713, (2012).
- [3] Lj. Ćirić, S. M. Alsulami, V. Parvaneh, R. Roshan, "Some fixed point results in ordered  $G_p$ -metric spaces", *Fixed Point Theory Appl.* 2013:317, 1-25, (2013).
- [4] V. Berinde, "General constructive fixed point theorems for Ćirić-type almost contractions in metric spaces", *Carpathian J. Math.*, 24, No.2, 10-19, (2008).
- [5] V. Berinde, "Approximating fixed points of weak  $\varphi$ -contractions using the Picard iteration", *Fixed Point Theory*, 131-147, (2003).

## WIJSMAN $I_2$ -INVARIANT CONVERGENCE OF DOUBLE SEQUENCE OF SETS

Şükrü TORTOP<sup>1</sup>, Erdinç DÜNDAR<sup>2</sup>

<sup>1</sup>*Department of Mathematics, AfyonKocatepe University,  
Afyonkarahisar/TURKEY  
[stortop@aku.edu.tr](mailto:stortop@aku.edu.tr)*

<sup>2</sup>*Department of Mathematics, AfyonKocatepe University,  
Afyonkarahisar/TURKEY  
[edundar@aku.edu.tr](mailto:edundar@aku.edu.tr)*

**Abstract:** In this paper, we study the concepts of Wijsman invariant statistical convergence, Wijsman  $I_2$ -invariant convergence ( $I^\sigma_{W_2}$ ), Wijsman  $I^*_2$ -invariant convergence ( $I^{*\sigma}_{W_2}$ ), Wijsman p-strongly invariant convergence ( $[W_2V_\sigma]_p$ ) of double sequence of sets and investigate the relationships among Wijsman invariant convergence,  $[W_2V_\sigma]_p$ ,  $I^\sigma_{W_2}$  and  $I^{*\sigma}_{W_2}$ . Also, we introduce the concepts of  $I^\sigma_{W_2}$ -Cauchy double sequence and  $I^{*\sigma}_{W_2}$ -Cauchy double sequence of sets.

**Keywords:** Invariant, I-convergence, Wijsman convergence, double sequence.

## A PRIORI ESTIMATES OF SOLUTIONS BOUNDARY VALUE PROBLEMS FOR THE HIGHER ORDER ELLIPTIC EQUATIONS IN GENERALIZED MORREY SPACES

Tahir GADJIEV, Shahla GALANDAROVA

*Institute of Mathematics and Mechanics,  
Baku/AZERBAIJAN  
[tgadjiev@mail.az](mailto:tgadjiev@mail.az)*

**Abstract:** A priori estimates are derived for the solutions boundary value problems for the higher order elliptic equations generalized Morrey spaces. This problem on bounded smooth domains is considered. Also one obtains  $L_{p,\lambda} - L_{q,\lambda}$  regularity estimates. On bases this estimates the solvability this problem in generalized Morrey spaces is proved..

## TWO PARAMETRIC (P; Q)-STANCU-BETA OPERATORS AND THEIR APPROXIMATION PROPERTIES

Taqseer KHAN

*Department of Mathematics, Aligarh Muslim University,  
Aligarh/INDIA  
[taqi.khan91@gmail.com](mailto:taqi.khan91@gmail.com)*

**Abstract:** The purpose of this paper is to introduce two parametric (p; q)-analogue of the Stancu-Beta operators. We study approximating properties of these operators using the Korovkin's approximation theorem and also study a direct theorem. We also obtain the Voronovskaja type estimate for these operators. Furthermore, we study the weighted approximation results and pointwise estimate for these operators. Finally, we present statistical approximating results for these operators.

**Keywords:** Two parametric Stancu-Beta operators; Linear positive operators; Korovkin theorem; Lipschitz functions; Modulus of continuity; Voronovskaja estimate; Statistical convergence.

### References:

- [1]. T. Acar, A. Aral, On Pointwise Convergence of q-Bernstein Operators and Their q-Derivatives, *Numer. Funct. Anal. Optim.*, 36 (3) (2015) 287-304.
- [2]. A. Aral, O. Do\_ğru, BleimannButzer and Hahn operators based on q-integers, *J. Inequal. Appl.*, (2007) 1-12. Art. ID 79410.
- [3]. O. Dalmanoglu, Approximation by Kantorovich type q-Bernstein operators, in *Proceedings of the 12th WSEAS International Conference on Applied Mathematics, Cairo, Egypt, (2007) 113-117.*
- [4]. R.A. DeVore, G.G. Lorentz, *Constructive Approximation*, Springer-Verlag, Berlin, 1993.
- [5]. O. Duman, A-statistical convergence of sequences of convolution operators, *Taiwanese J. Math.* 12 (2) (2008) 523-536.
- [6]. H. Fast, Sur la convergence statistique, *Colloq. Math.* 2 (1951) 241-244.

## A COMPARISON OF FINITE-DIFFERENCE METHOD BY FIRST ORDER AND SECOND ORDER CENTRAL DIFFERENTIATION FORMULAS FOR LINEAR ODES UP TO FOURTH DEGREE AND A GENERALIZED CODE

Tefaruk HAKTANIR, Hatice CITAKOGLU, Murat COBANER

*Department of Civil Engineering, Erciyes University, Kayseri/TURKEY*  
[thaktan@erciyes.edu.tr](mailto:thaktan@erciyes.edu.tr), [hcitakoglu@erciyes.edu.tr](mailto:hcitakoglu@erciyes.edu.tr), [mcobaner@erciyes.edu.tr](mailto:mcobaner@erciyes.edu.tr)

**Abstract:** The finite-difference method is applied to two second degree, a third degree, and a fourth degree linear ordinary differential equations (LODEs), whose analytical solutions are available, by using the first order and next the second order central differentiation formulae (FOCDF, SOCDF), with step sizes of  $\Delta x = 0.1, 0.05, 0.02, 0.01$ , separately. Usage of SOCDF is not observed to yield a convincing betterment while necessitating more laborious algebraic manipulations in transferring the LODEs to finite-difference equations. A computer program commonly applicable to any LODE up to the fourth degree is coded, which is to be linked to a sub-program comprising the coefficients of the resultant finite difference equations of the particular problem handled. Both programs use FOCDFs, and the results are improved by the extrapolation-to-the-limit formula, which is observed to yield more accurate results than the case using SOCDF with the same  $\Delta x$ .

**Keywords:** boundary-value-problem type of linear ordinary differential equations

### References:

- [1] Chapra S C and Canale R P (1988) Numerical Methods in Engineering. Second Edition, McGraw-Hill, Inc., New York, NY, 10016, USA.
- [2] Hoffman J D (2001) Numerical Methods for Engineers and Scientists. Second Edition, Marcel Dekker, Inc, 270 Madison Avenue, New York, NY, 10016, USA.
- [3] Kiusalaas J (2005) Numerical Methods in Engineering with Matlab. Cambridge University Press, The Edinburgh Building, Cambridge CB2, 2RU, UK.

## MATHEMATICAL ANALYSIS OF LENGYEL-EPSTEIN MODEL BY FRACTIONAL-ORDER DIFFERENTIAL EQUATIONS SYSTEMS

Teslima DAŞBAŞI<sup>1</sup>, BahatdinDAŞBAŞI<sup>2</sup>

*1Department of Chemical and Chemical Processing Technologies, Cumhuriyet  
University, Sivas/TURKEY*

[teslimadasbasi@hotmail.com](mailto:teslimadasbasi@hotmail.com)

*2Department of Computer Technologies, Cumhuriyet University, Sivas/TURKEY*

[dasbasi\\_bahatdin@hotmail.com](mailto:dasbasi_bahatdin@hotmail.com)

**Abstract:** The examined model in this study is fractional-order form of the dimensionless Lengyel-Epstein model being the oscillating chemical reactions. In this sense, it is obtained the following system of two fractional-order differential equation:

$$\begin{aligned} D^\alpha x(t) &= F(x, y) = a - x - 4 \frac{xy}{1+x^2} \\ D^\alpha y(t) &= G(x, y) = bx \left( 1 - \frac{y}{1+x^2} \right) \end{aligned} \quad (1)$$

where  $\alpha \in (0,1]$ . It is founded the positive equilibrium point. In addition that, the stability analysis of equilibrium point of model (1) is made. Results of this analysis are supported via numerical simulations drawn by datas obtained from literature.

**Keywords:** Fractional-order differential equation system, mathematical model, stability analysis, equilibrium points, oscillating chemical reactions.

### References:

- [1] LinglongDua and Mingxin Wang, "Hopf bifurcation analysis in the 1-D Lengyel–Epstein reaction–diffusion model," *Journal of Mathematical Analysis and Applications*, vol. 366, no. 2(2010), 473-485.
- [2] E. Ahmed, A.M.A. El-Sayed, and H.A.A. El-Saka, "On some Routh–Hurwitz conditions for fractional order differential equations and their applications in Lorenz, Rössler, Chua and Chen systems," *Phys. Lett. A*, vol. 358, 2006.

## GLOBAL EXISTENCE AND BOUNDEDNESS OF SOLUTIONS FOR A TYPE OF NONLINEAR INTEGRO DIFFERENTIAL EQUATIONS OF THIRD ORDER

Timur AYHAN

*Department of Primary School-Mathematics  
Faculty of Education Siirt University, Siirt/Turkey  
[tayhan002@gmail.com](mailto:tayhan002@gmail.com)*

**Abstract:** In this article, a kind of nonlinear integro-differential equations of third order is dealt. The global existence and boundedness of solutions are discussed. In the proof of the main theorem, the second (direct) method of Lyapunov is used by constructing an appropriate Lyapunov function. The result obtained in this paper contains and enlarges some well known results on the third order nonlinear differential equations with delay in the literature. We also give an example to show the impressiveness of the method utilized.

**Keywords:** Lyapunov functional, integro-differential equation, global existence

### References:

- [1] C. Tunç, "Boundedness of solutions of a third order nonlinear differential equation", *J. Inequal. Pure Appl. Math.* 6(1), (2005), 1-6.
- [2] J. O. C. Ezeilo, "A boundedness theorem for a certain third order differential equations", *Proc. London Math. Soc.* 13(3), (1963), 99-124.
- [3] M. Remili, L. D. Oudjedi, "Stability and boundedness of the solutions of non-autonomous third order differential equations with delay", *Acta Univ. Palack. Olomuc. Fac. Rerum. Natur. Math.* 53(2), (2014), 139-147.
- [4] T. Hara, "On the uniform ultimate boundedness of solutions of certain third order differential equations", *J. Math. Anal. Appl.* 80(2), (1981), 533-544.

**A NEW RESULT ON THE CONTINUABILITY AND  
BOUNDEDNESS OF SOLUTIONS TO A CLASS OF  
VECTOR DIFFERENTIAL EQUATIONS OF THIRD ORDER  
WITH DELAY**

Timur AYHAN

*Department of Primary School-Mathematics  
Faculty of Education Siirt University, Siirt/Turkey  
[tayhan002@gmail.com](mailto:tayhan002@gmail.com)*

**Abstract:** In this paper, we use Lyapunov's second method, by constructing an appropriate Lyapunov functional, sufficient conditions which warrant the continuability and boundedness of all solutions to a kind of nonlinear vector differential equations of third order with constant retarded argument are established. Also, we give an example to illustrate the theoretical analysis in this study and to check the impressiveness of the method employed.

**Keywords:** Lyapunov functional, continuability, boundedness, third order.

**References:**

- [1] A. M. Lyapunov, "Stability of Motion", Academic Press, London, (1966).
- [2] C. Tunç, S. A. Mohammed, "On the qualitative properties of differential equations of third order with retarded argument", *Proyecciones* 33(3), 325–347, (2014).
- [3] N. N. Krasovskii, "Stability of Motion. Applications of Lyapunov's Second Method to Differential Systems and Equations with Delay", Stanford, Calif.: Stanford University Press, (1963).
- [4] V. Kolmanovskii, A. Myshkis, "Introduction to the Theory and Applications of Functional Differential Equations", Kluwer Academic Publishers, Dordrecht, (1999).



## AN INVERSE NODAL PROBLEM TO CONSTRUCT COULOMB POTENTIAL FOR $p$ -LAPLACIAN STURM- LIOUVILLE EQUATION WITH POLYNOMIALLY BOUNDARY CONDITIONS

Tuba GULSEN

*Department of Mathematics, Firat University  
Elazığ/TURKEY  
[tubagulsen87@hotmail.com](mailto:tubagulsen87@hotmail.com)*

**Abstract:** In this study, we solve an inverse nodal problem for  $p$ -Laplacian Sturm-Liouville equation with coulomb potential when boundary condition polynomially dependent on spectral parameter. Then, we obtain asymptotic expansion of eigenvalues and nodal parameters by using modified Prüfer substitution. Finally, we construct coulomb potential by nodal lengths.

**Keywords:** Inverse Nodal Problem, Prüfer Substitution, Coulomb Potential

### References:

- [1] J. R. McLaughlin, "Inverse spectral theory using nodal points as data-a uniqueness result", J. Differential Equations, 73, 354-362 (1988).
- [2] C. K. Law, W. C. Lian and W. C. Wang, "Inverse nodal problem and the Ambarzumyan problem for the  $p$ -Laplacian", Proc. Roy. Soc. Edinburgh Sect. A Math., 139(6), 1261-1273 (2009).
- [3] W. C. Wang, "Direct and inverse problems for one dimensional  $p$ -Laplacian operators", National Sun Yat-sen University, PhD Thesis, (2010).
- [4] N. Topsakal and R. Amirov, "Inverse problem for Sturm-Liouville operators with coulomb potential which have discontinuity conditions inside an interval", Math. Phys. Anal. Geom., (13), 29-46 (2010).

## SOME GENERAL RESULTS FOR THE AVERAGE LOWER 2-DOMINATION NUMBER OF GRAPHS

Tufan TURACI

*Department of Mathematics, Karabük University,  
Karabük/TURKEY*

[tufanturaci@karabuk.edu.tr](mailto:tufanturaci@karabuk.edu.tr)

**Abstract:** In a communication network, the vulnerability measures the resistance of the network to disruption of operation after the failure of certain stations or communication links. The average lower 2-domination number is newly defined for the graph vulnerability.

In this presentation, the abovementioned new parameter is defined and examined. Then, upper and lower bounds are determined and exact formulas are found for the average lower 2-domination number of any graph  $G$ . Finally, some results are obtained for the average lower 2-domination number of join graph.

**Keywords:** Graph vulnerability; Connectivity; Network design and communication; Domination number; Average lower 2-domination number.

### References:

- [1] A. Aytaç and T. Turacı, "Vertex Vulnerability Parameter of Gear Graphs", *International Journal of Foundations of Computer Science*, 22:5(2011), 1187–1195.
- [2] M. Blidia, M. Chellali and F. Maffray, "On Average Lower Independence and Domination Number in Graphs", *Discrete Math.*, 295(2005), 1-11.
- [3] M.A. Henning, "Trees with Equal Average Domination and Independent Domination Numbers", *Ars Combinatoria*, 71(2004), 305-318.
- [4] T. Turacı, "The Concept of Vulnerability in graphs and Average Lower 2-domination Number", 28.th National Mathematics Conference, September 7-9, 2015, Antalya/TURKEY.
- [5] T. W. Haynes, S. T. Hedetniemi and P. J. Slater, "Fundamentals of Domination in Graphs", *Advanced Topic*, Marcel Dekker, Inc, New York, 1998.
- [6] V. Aytaç, "Average Lower Domination Number in Graphs", *Comptes Rendus de L'academie Bulgare des Sciences*, 65:12(2012), 1665-1674.

## A NEW EFFECTIVE METHOD TO SOLVE NONLINEAR PARTIAL DIFFERENTIAL EQUATIONS: THE UNIFIED METHOD

Şamil AKÇAĞIL<sup>1</sup>, Tuğba AYDEMİR<sup>2</sup>

And Ömer Faruk GÖZÜKIZIL<sup>3</sup>

<sup>1</sup>*The Faculty of Economics and Administrative Sciences, BilecikŞeyhEdebali  
University,  
Bilecik/TURKEY*

[samilakcagil@hotmail.com](mailto:samilakcagil@hotmail.com)

<sup>2</sup>*Institute of Natural Sciences, SakaryaUniversity,  
Sakarya/TURKEY*

[tgb.aydemir@gmail.com](mailto:tgb.aydemir@gmail.com)

<sup>3</sup>*Department of Mathematics, SakaryaUniversity,  
Sakarya /TURKEY*

[farukg@sakarya.edu.tr](mailto:farukg@sakarya.edu.tr)

**Abstract:** In this paper, we construct and present a new effective method called the unified method for solving nonlinear partial differential equations (NPDEs). Compared to other methods, the significant contribution of the unified method is firstly to unify the family of tanh function methods and the family of (G'/G) expansion methods. Secondly, it gives many more solutions for NPDEs direct, concise and simple manner than the total of these two families. Also, the unified method gives these abundant solutions without using tedious and complex algorithm on computer programs. Afterwards, we demonstrate the effectiveness of the unified tanh method by seeking more exact solutions of the Lonngrenwave equation.

**Keywords:** The tanh function method; The extended tanh function method; The modified extended tanh function method; The complex tanh function method; (G'/G) expansion method; The new approach of generalized (G'/G) expansionmethod; The (G'/G,1/G) expansion method; Nonlinear partial differential equations; Travelling wave solution; The unified method; The LonngrenWave Equation.

### References:

- [1] W. Malfliet, Solitary wave solutions of nonlinear wave equations, Am. J. Phys. 60 (7) (1992) 650--654.

## THE MULTIDIMENSIONAL REVERSE HARDY-TYPE INEQUALITIES FOR SUPREMAL OPERATOR

Rza MUSTAFAYEV<sup>1</sup>, Tuğçe ÜNVER<sup>2</sup>

<sup>1</sup>Department of Mathematics, Kirikkale University,  
Kirikkale/TURKEY

[rzamustafayev@gmail.com](mailto:rzamustafayev@gmail.com)

<sup>2</sup>Department of Mathematics, Kirikkale University,  
Kirikkale/TURKEY

[tugceunver@gmail.com](mailto:tugceunver@gmail.com)

**Abstract:** In this presentation, we give the characterization of the inequalities

$$\|gw\|_{p,\mathbb{R}^n} \leq C \left\| v(t) \|g\|_{\infty, {}^cB(0,t)} \right\|_{q,(0,\infty)}$$

and

$$\|gw\|_{p,\mathbb{R}^n} \leq C \left\| v(t) \|g\|_{\infty, B(0,t)} \right\|_{q,(0,\infty)}$$

for all non-negative measurable functions on  $\mathbb{R}^n$  when  $0 < p, q \leq \infty$ . Here  $w$  and  $v$  are weight function on  $\mathbb{R}^n$  and  $(0, \infty)$ , respectively,  $B(0, t)$  is the ball in  $\mathbb{R}^n$  centered at the origin of radius  $t$  and  ${}^cB(0, t) := \mathbb{R}^n \setminus B(0, t)$ .

**Keywords:** Hardy Inequality, supremal operator, discretization.

### References:

- [1] W.D. Evans, A. Gogatishvili, and B. Opic, "The reverse Hardy inequality with measures", *Math. Inequal. Appl.* **11** (2008), no. 1, 43–74.
- [2] A. Gogatishvili, R.Ch. Mustafayev, "The multidimensional reverse Hardy inequalities", *Math. Inequal. Appl.* **15** (2012), no. 1, 1–14.
- [3] R.Ch. Mustafayev, T. Ünver, "Reverse Hardy-type inequalities for supremal operators with measures", *Math. Inequal. Appl.* **18** (2015), no. 4, 1295–1311.
- [4] W. Rudin, "Principles of mathematical analysis" Third edition. International Series in Pure and Applied Mathematics. McGraw-Hill Book Co., New York-Auckland-Düsseldorf, 1976. x+342 pp. 26-02.

## ON STATISTICAL CONVERGENCE WITH RESPECT TO THE GEOMETRIC MEAN AND ITS APPLICATIONS TO APPROXIMATION THEOREMS

Uğur KADAK<sup>1</sup>, Feyzi BAŞAR<sup>2</sup>

<sup>1</sup>*Department of Mathematics, Bozok University,  
Yozgat/TURKEY*

[ugurkadak@gmail.com](mailto:ugurkadak@gmail.com)

<sup>2</sup>*Department of Mathematics, Fatih University,  
İstanbul/TURKEY*

[feyzibasari@gmail.com](mailto:feyzibasari@gmail.com)

**Abstract:** In the present paper, we extend the notions of statistical convergence and statistical summability in the sense of Geometric calculus. In first, we introduce geometric statistically convergence and statistically geometric summability with respect to the geometric density. Later, we define weighted versions of both above notions. Based on the definition of geometric linearity, we prove a Korovkin type approximation theorem and give an example via Bernstein positive linear operator. Furthermore, we estimate the rate of convergence in terms of modulus of continuity in geometric sense. Finally, we examine some Voronovskaja type results connected with geometric Taylor expansion.

**Keywords:**

Geometric statistically convergence, statistically geometric summability, Korovkin and Voronovskaja type approximation theorems, geometric modulus of continuity, rates of convergence.

## NECESSARY AND SUFFICIENT CONDITIONS FOR FIRSTORDER DIFFERENTIAL OPERATORS TO BE ASSOCIATED WITH A GENERALIZED CAUCHY-RIEMANN OPERATOR IN CLIFFORD ANALYSIS

Uğur YÜKSEL

Department of Mathematics, Atılım University,  
Ankara/TURKEY

[ugur.yuksel@atilim.edu.tr](mailto:ugur.yuksel@atilim.edu.tr)

**Abstract:** In this paper we consider initial value problems of type

$$\partial_t u = F(t, x, u, \partial_{x_i} u) := \sum_{i=0}^n A^{(i)}(t, x) \partial_{x_i} u + B(t, x)u + C(t, x)$$
$$u(0, x) = u_0(x)$$

in the space of generalized monogenic functions  $u(t, x)$  in the sense of Clifford Analysis satisfying the differential equation

$$D_\lambda u := Du + \lambda u = 0,$$

where  $t \in [0, T]$  is the time variable  $x = (x_0, x_1, \dots)$  runs in a bounded and simply connected domain in  $\mathbb{R}^n$ ,  $\lambda$  is a real number, and  $D$  is the Cauchy-Riemann operator of Clifford analysis. We prove necessary and sufficient conditions on the coefficients of the operator  $F$  under which  $F$  is associated with the generalized Cauchy-Riemann operator  $D_\lambda$ , i.e.  $F$  transforms the set of all solutions of the differential equation  $D_\lambda = 0$  into solutions of the same equation for fixedly chosen  $t$ . This criterion makes it possible to construct operators  $F$  for which the initial value problem is uniquely solvable for an arbitrary initial generalized monogenic function  $u_0$  by the method of associated spaces constructed by W. Tutschke [5] and the solution is also generalized monogenic for each  $t$ .

### References:

- [1] U. Y. Abbas, U. Yüksel, Necessary and sufficient conditions for first order differential operators to be associated with a disturbed Dirac operator in Quaternionic Analysis. *Adv. Appl. Clifford Algebras* 25 (2015), 1--12.
- [2] Y. Bolívar, C. Vanegas, Initial value problems in Clifford-type analysis. *Complex Variables and Elliptic Equations*, 58, (2013), 557-569.

## INVERSE NUMERICAL RADIUS INEQUALITY FOR REPRODUCING KERNEL HILBERT SPACE OPERATORS

Ulaş YAMANCI<sup>1</sup>, Mehmet GÜRDAL<sup>2</sup>

<sup>1,2</sup>*Department of Mathematics, Süleyman Demirel University,  
Isparta/TURKEY*

[ulasyamanci@sdu.edu.tr](mailto:ulasyamanci@sdu.edu.tr), [gurdalmehmet@sdu.edu.tr](mailto:gurdalmehmet@sdu.edu.tr)

**Abstract:** A basic inequality for numerical radius is the power inequality stating that  $w(A^n) \leq w^n(A)$ , ( $n = 1, 2, \dots$ ). This inequality is well known in the literature. But, the inverse inequality  $w^n(A) \leq C w(A^n)$  for any  $n > 0$  with some constant  $C$  are not well studied in the literature. Also, the analog inequality for the Berezin number of operators on the Reproducing Kernel Hilbert Space is not investigated in general. So, in this paper, we give new some inverse inequalities for numerical radius and Berezin number of some operators..

**Keywords:** Numerical radius, Hilbert-type inequality, Berezin number, positive operator.

**Acknowledgement:** This work is supported by TÜBA through Young Scientist Award Program (TÜBA-GEBİP/2015)

### References:

- [1] N. Aronzajn, "Theory of reproducing kernels", Trans. Amer. Math. Soc., 68(1950), 337-404.
- [2] M.T. Karaev, "Berezin symbol and invertibility of operators on the functional Hilbert spaces", J. Funct. Anal., 238(2006), 181-192.
- [3] M.T. Karaev, M. Gürdal, U. Yamancı, "Some results related with Berezin symbols and Toeplitz operators", Math. Inequal. Appl., 17(3)(2014), 1031-1045.
- [4] M. Kian, "Hardy-Hilbert type inequalities for Hilbert space operators", Ann. Funct. Anal., 3(2)(2012), 128-134.
- [5] S. Saitoh, "Theory of reproducing kernels and its applications", Pitman Research Notes in Mathematics Series V., 189, 1988.

## SECOND-ORDER BOUNDARY VALUE PROBLEM ON A HALF-LINE

Ummahan AKCAN<sup>1</sup>, Erbil ÇETİN<sup>2</sup>

<sup>1</sup>*Department of Mathematics, Faculty of Science, Anadolu University, 26470, Eskişehir/TURKEY*

[ummahanakcan@anadolu.edu.tr](mailto:ummahanakcan@anadolu.edu.tr)

<sup>2</sup>*Department of Mathematics, Ege University, Bornova, İzmir/TURKEY*

[erbil.cetin@ege.edu.tr](mailto:erbil.cetin@ege.edu.tr)

**Abstract:** In this presentation, we deal with second-order three-point boundary value problem with integral boundary condition on a half-line. By using fixed point theorems, we give sufficient conditions for the existence solutions of the problem. Also, an example which supports our result is indicated.

**Keywords:** Infinite interval problems, Schauder's fixed point theorem, Integral boundary conditions.

### References:

- [1] J. Zu, "Existence and Uniqueness of Periodic Solution for Nonlinear Second-Order Ordinary Differential Equations" *Bound. Value Probl.*, Volume 2011, doi:10.1155/2011/192156.
- [2] H. Lian, W. Ge, "Solvability for second-order three-point boundary value problems on a half line," *Appl. Math. Lett.*, 19 (2006) 1000-1006
- [3] U. Akcan, N.A. Hamal, "Existence of concave symmetric positive solutions for a three-point boundary value problems, *Adv. Differ. Equ.* 2014.
- [4] I. Fonseca, W. Gangbo, "Degree Theory in Analysis and Applications", *Oxford Lecture Series in Mathematics and its Applications 2*, Oxford University Press, 1995.



## PARABOLIC OBLIQUE DERIVATIVE PROBLEM WITH DISCONTINUOUS COEFFICIENTS IN GENERALIZED WEIGHTED MORREY SPACES

Vagif S. GULIYEV<sup>1,2</sup>, M. N. OMAROVA<sup>3</sup>

<sup>1</sup>*Department of Mathematics, Ahi Evran University,  
Kirsehir/TURKEY*

<sup>2</sup>*Institute of Mathematics and Mechanics,  
Baku/AZERBAIJAN  
[yagif@guliyev.com](mailto:yagif@guliyev.com)*

<sup>3</sup>*Baku State University,  
Baku/AZERBAIJAN*

[mehribanomarova@yahoo.com](mailto:mehribanomarova@yahoo.com)

**Abstract:** In this report it is proved that global weighted Morrey-type regularity of the solution of the regular oblique derivative problem for linear uniformly parabolic operators with VMO coefficients. Also authors show that if the right-hand side of the parabolic equation belongs to certain generalized weighted Morrey space  $M^{p,\varphi}(Q, \omega)$ , then the strong solution belongs to the generalized weighted Sobolev-Morrey space  $W_{2,1}^{p,\varphi}(Q, \omega)$  (see [1,2]).

The research of V. Guliyev and M. Omarova was partially supported by the grant of Presidium of Azerbaijan National Academy of Science 2015.

### References:

- [1] V. S. Guliyev, M. N. Omarova, Parabolic oblique derivative problem with discontinuous coefficients in generalized weighted Morrey spaces, *Open Mathematics*, 14 (2016), 49-61.
- [2] V.S. Guliyev, M. N. Omarova, Corrigendum to : Parabolic oblique derivative problem with discontinuous coefficients in generalized weighted Morrey spaces, *Open Mathematics*, 14 (2016), 283-285.

## FIXED POINT THEOREMS FOR MAPPINGS (E.A)- PROPERTY IN PARTIAL METRIC SPACE

Vildan ÖZTÜRK<sup>1</sup>, Duran TÜRKOĞLU<sup>2</sup>

1. Faculty Of Education, ArtvinÇoruh University, Artvin, Turkey İstanbul/TURKEY  
[vildan\\_ozturk@hotmail.com](mailto:vildan_ozturk@hotmail.com)

2. Faculty Of Science, Gazi University, Ankara, Turkey.  
[dturkoglu@gazi.edu.tr](mailto:dturkoglu@gazi.edu.tr)

**Abstract:** In consideration of the concept of integral type (Branciari type) contractive condition and (E.A)-property, we proved fixed point theorems for two pairs of mappings satisfying (E.A)-property under (psi,fi)-contractions of integral type in partial metric spaces.

## RIESZ POTENTIAL IN GENERALIZED MORREY SPACES ON THE HEISENBERG GROUP

Y.PELİN MAMMADOV<sup>1</sup>, A. EROĞLU<sup>2</sup>,

<sup>1</sup>Nakhchivan Teacher-Training Institute, Nakhchivan AZ 7003, Azerbaijan  
[yagubmammadov@yahoo.com](mailto:yagubmammadov@yahoo.com)

<sup>2</sup>Department of Mathematics, Nigde University,  
Nigde/TURKEY  
[aeroglu@nigde.edu.tr](mailto:aeroglu@nigde.edu.tr)

**Abstract:** In this report, it is proved that Riesz potential operator on the Heisenberg group  $\mathbb{H}$  is bounded on generalized Morrey spaces  $M_{p,\varphi}(\mathbb{H})$  (see [1]). The boundedness conditions are formulated in terms of Zygmund type integral inequalities. Based on the properties of the fundamental solution of the sub-Laplacian on  $\mathbb{H}$ , were proved two Sobolev-Stein embedding theorems for generalized Morrey and Besov-Morrey spaces.

### References:

- [1] V.S.Guliyev, A. Eroglu, Y.Y.Mammadov, Riesz potential on the Heisenberg group and generalized Morrey spaces, Journal of Mathematical Sciences, Vol.189, No. 3, 2013, 365-382.

## ON EXISTENCE AND CONVERGENCE THEOREMS FOR A NEW GENERAL NONLINEAR MAPPING ON CAT(0) SPACES

Vatan KARAKAYA<sup>1</sup>, Emirhan HACIOGLU<sup>2</sup>, Yunus ATALAN<sup>2</sup>

<sup>1</sup>*Department of Mathematical Engineering, Yıldız Technical University,  
İstanbul/TURKEY*

[vkaya@yahoo.com](mailto:vkaya@yahoo.com)

<sup>1</sup>*Department of Mathematics, Yıldız Technical University,  
İstanbul/TURKEY*

[haciogluemirhan@gmail.com](mailto:haciogluemirhan@gmail.com), [yunus\\_atalan@hotmail.com](mailto:yunus_atalan@hotmail.com)

**Abstract:** In this presentation, we introduce a new nonlinear hybrid mapping which is more general than 2-generalized hybrid mappings on CAT(0) spaces. Then we prove existence and convergence theorems for class. Our results is generalization of corresponding results in literature.

**Keywords:** Three step iteration, strong convergence, rate of convergence, data dependence integral equation.

### References:

- [1] Takahashi, W., Wong, N. C., & Yao, J. C. "Fixed point theorems for three new nonlinear mappings in Banach spaces". *Journal of Nonlinear and Convex Analysis*, 13(2012), 363-382..
- [2] Phuengrattana, Withun, and SuthepSuantai. "Existence and convergence theorems for generalized hybrid mappings in uniformly convex metric spaces." *Indian Journal of Pure and Applied Mathematics* 45, no. 1 (2014): 121-136..

## SOME THEOREMS ABOUT STATISTICAL CONVERGENCE ON TIME SCALES

Yavuz ALTIN

*Department of Mathematics, FiratUniversity,  
Elazığ/TURKEY  
[yaltin23@yahoo.com](mailto:yaltin23@yahoo.com)*

**Abstract:** In this study we introduce statistical convergent sequence spaces on an arbitrary time scale and examine some inclusion relations among them.

**Keywords:** Statistical Convergence, Time scales.

### References:

- [1] D. Borwein, "Linear functionals connected with strong Cesàro summability", *Journal of the London Mathematical Society*, 40 (1965), 628-634.
- [2] R. Çolak, "On  $\lambda$  – statistical convergence", Conference on summability and applications, commerce University, may 12-13, (2011), Istanbul, Turkey.
- [3] M.S. Seyyidoglu, M. and N. Ö.Tan, "A note on statistical convergence on time scale", *Journal of Inequalities and Applications*, (2012) , 219, 8 pp.
- [4] C. Turan, and O. Duman, "Statistical convergence on timescales and its characterizations", *Advances in applied mathematics and approximation theory*, 57-71, Springer Proc. Math. Stat., 41, Springer, New York, (2013).
- [5] M. Mursaleen, "  $\lambda$  – statistical convergence", *Mathematica Slovaca*, 50 (2000), no.1, 111-115.
- [6] M. Bohner, and A. Peterson, A, "Dynamic equations on time scales, an introduction with applications ", Birkhauser, Boston, 2001.
- [7] H. Fast, "Sur la convergence statistique", *Colloquium Mathematicum*, 2 (1951), 241–244.

## AUTO-BÄCKLUND TRANSFORMATION FOR SOME NONLINEAR PARTIAL DIFFERENTIAL EQUATION

Ibrahim E. INAN<sup>1</sup>, Yavuz UĞURLU<sup>2</sup>, Hasan BULUT<sup>2</sup>

<sup>1</sup>Firat University, Faculty of Education, Department of Mathematics 23119  
Elazig, Turkey

[ieinan@yahoo.com](mailto:ieinan@yahoo.com)

<sup>2</sup>Firat University, Science Faculty, Department of Mathematics, 23119  
Elazig, Turkey

[matematikci\\_23@yahoo.com.tr](mailto:matematikci_23@yahoo.com.tr), [hbulut@firat.edu.tr](mailto:hbulut@firat.edu.tr)

**Abstract:** In this paper, we apply auto-Bäcklund transformation for Sharma-Tasso-Olver (STO) equation and fourth order equation of the Burgers hierarchy. We obtain solitary wave solutions of these equations. Auto-Bäcklund transformation was developed as a direct and simple method to obtain solutions of nonlinear partial differential equations by Fan.

**Keywords:** Auto-Bäcklund transformation, STO equation, fourth order equation of the Burgers hierarchy, solitary wave solution

### References:

- [1] X.B. Hu, W.X.Ma, "Application of Hirota's bilinear formalism to the Toeplitz lattice-some special soliton-like solutions", *Physics Letters A* 293 (2002), 161.
- [2] Y.Shang, "Bäcklund transformation, Lax pairs and explicit exact solutions for the shallow water waves equation", *Applied Mathematics and Computation* 187 (2007), 1286.
- [3] A.M. Abourabia, M.M. El Horbaty, "On solitary wave solutions for the two dimensional nonlinear modified Kortweg-de Vries-Burger equation, *Chaos, Solitons* 29 (2006), 354.

## A NEW APPROACH TO FRACTIONAL $q$ -DIFFERENCE EQUATIONS AND THE $q$ -LAPLACE TRANSFORM

Yavuz YAZICI<sup>1</sup>, Umut Mutlu ÖZKAN<sup>2</sup>

<sup>1</sup>*Department of Mathematics, Cankiri Karatekin University, Cankiri/TURKEY*  
yavuzyazici@karatekin.edu.tr

<sup>2</sup>*Department of Mathematics, Afyon Kocatepe University,*  
*Afyonkarahisar/TURKEY*  
umut\_ozkan@aku.edu.tr

**Abstract:** In this presentation, we introduce a new form of fractional  $q$ -difference equations derived the fractional  $q, \rho$ -derivative. We also introduce the  $q, \rho$ -Laplace transform and the  $q, \rho$ -convolution to solve new type the fractional  $q$ -difference equations.

**Keywords:** The  $q, \rho$ -Laplace transform, the  $q, \rho$ -convolution, the fractional  $q, \rho$ -integral, the fractional  $q, \rho$ -derivative.

### References:

- [1] Gasper, George and Rahman, M. *Basic hypergeometric series*. (Cambridge university press, 2004).
- [2] Díaz, R. & Teruel, C.  $q, k$ -Generalized Gamma and Beta Functions. *J. Nonlinear Math. Phys.* 12, 118–134 (2005).
- [3] Annaby, M. H. & Mansour, Z. S.  *$q$ -Fractional Calculus and Equations*. 2056, (Springer, 2012).
- [4] Anatoly, A. K. Hadamard-type fractional calculus. *J. Korean Math. Soc.* 38, 1191–1204 (2001).
- [5] Al-salam, W. A. Some fractional  $q$ -integrals and  $q$ -derivatives. *Proc. Edinburgh Math. Soc. (Series 2)* 15, 135–140 (1966).
- [6] Kac, Victor and Cheung, P. *Quantum calculus*. (Springer Science & Business Media, 2002).
- [7] Yazici, Y & Ozkan, U. M.  $q, \rho$ -Fractional Calculus and  $q, \rho$ -Laplace Transform. *Advances in Difference Equations*. (Submitted).
- [8] Katugampola, U. N. New approach to a generalized fractional integral. *Appl. Math. Comput.* 218, 860–865 (2011).
- [9] Sole, A. De & Kac, V. G. On integral representations of  $q$ -gamma and  $q$ -beta functions. *arXiv Prepr. math/0302032* 1–16 (2003).
- [10] JAbdi, W. H. Application of  $q$ -Laplace transform to the solution of certain  $q$ -integral equations. *Rend. del Circ. Mat. di Palermo* 11, 245–257 (1962).

ON THE CONSTRUCTION OF GENERAL SOLUTION OF  
THE EQUATION  $\frac{\partial w(z)}{\partial \phi(z)} - \frac{1}{2} \phi(z)^{-1} \tilde{\lambda} \overline{w(z)} = 0$

Yeşim SAĞLAM ÖZKAN<sup>1</sup>, Sezayi HIZLIYEL<sup>2</sup>

<sup>1</sup>Department of Mathematics, Uludag University,  
Bursa/TURKEY

[ysaglam@uludag.edu.tr](mailto:ysaglam@uludag.edu.tr)

<sup>2</sup>Department of Mathematics, Uludag University,  
Bursa/TURKEY

[hizliyel@uludag.edu.tr](mailto:hizliyel@uludag.edu.tr)

**Abstract:** This essay is an attempt to construct the general solution of  $\frac{\partial w}{\partial \phi} = Aw + B\bar{w}$  type equation which has special choosing of coefficients. Where the unknown  $w(z) = (w_{ij}(z))$  is  $m \times s$  matrix valued function,  $\phi(z)$  is a generating solution for  $Q$ -holomorphic function and  $A = \{a_{ij}(z)\}$  and  $B = \{b_{ij}(z)\}$  are commuting with  $Q$ .

**Keywords:**  $Q$ -holomorphic functions, singular coefficients, generalized analytic functions.

**References:**

- [1] A. Douglis, "A Function theoretic approach to elliptic systems of equations in two variables" *Comm. Pure Appl. Math.* 6(1953), 259-289.
- [2] B.V. Bojarskii, "Theory of generalized analytic vectors (in Russian)", *Ann. Polon. Math.* 17 (1966), 281-320.
- [3] S. Hızıyel, M. Çağlıyan, "Generalized  $Q$ -holomorphic functions", *Complex Var. Theory Appl.* 49 (2004), 427-447.
- [4] S. Hızıyel, M. Çağlıyan, "Pseudo  $Q$ -holomorphic functions", *Complex Var. Theory Appl.* 49 (2004), 941-955.
- [5] S. Hızıyel, "Carleman-Type Theorems for Generalized  $Q$ -Holomorphic Functions", *Journal of Mathematical Analysis and Applications* 412(2014), 816-827.

## CENTRAL FACTORIAL TYPE NUMBERS ASSOCIATED WITH AVERAGING OPERATOR

Yılmaz ŞİMŞEK

*Department of Mathematics, Akdeniz University,*

*Antalya/TURKEY*

[ysimsek@akdeniz.edu.tr](mailto:ysimsek@akdeniz.edu.tr)

**Abstract:** The aim of this paper is to give and investigate the properties of the numbers  $y_1(n, k; \lambda)$  via their generating functions. These numbers are related to the Stirling numbers of the second kind and the other numbers like as combinatorial sums. We use some operators which are related to the translation or shifting operator and averaging operator. We give relationships between these numbers and these operators. Finally, we completed our results by given further comments and remarks.

**Keywords:** Central factorial numbers, Stirling numbers, Shifting operator, Averaging operator, Combinatorial sum, Generating function.

### References:

- [5] M. Bona, Introduction to Enumerative Combinatorics, The McGraw-Hill Companies, Inc. New York, 2007.
- [6] J. Cigler, Fibonacci polynomials and central factorial numbers, preprint.
- [7] G. B. Djordjevic and G. V. Milovanovic, Special classes of polynomials, University of Nis, Faculty of Technology Leskovac, 2014.
- [8] R. Golombek, Aufgabe 1088, *El. Math.* 49 (1994) 126-127.
- [9] Y. Simsek, New families of special numbers for computing negative order Euler numbers, preprint.
- [10] Y. Simsek, Special numbers on analytic functions, *Appl. Math. (Irvine)* 5 (2014), 1091-1098.



## STABILITY OF NONLINEAR VOLTERRA-FREDHOLM INTEGRO DIFFERENTIAL EQUATION: A FIXED POINT APPROACH

Yunus ATALAN<sup>1</sup>, Vatan KARAKAYA<sup>2</sup>

<sup>1</sup>*Department of Mathematics, Yıldız Technical University,  
İstanbul/TURKEY*

[yunus\\_atalan@hotmail.com](mailto:yunus_atalan@hotmail.com)

<sup>2</sup>*Department of Mathematical Engineering, Yıldız Technical University,  
İstanbul/TURKEY*

[vkkaya@yahoo.com](mailto:vkkaya@yahoo.com)

**Abstract:** The aim of this presentation is to establish the Hyers-Ulam stability and the Hyers-Ulam-Rassias stability of the class of nonlinear Volterra Fredholm integro-differential equations via fixed point method in Banach spaces.

**Keywords:** Volterra-Fredholm integro differential equation Hyers-Ulam stability, fixed point method.

### References:

- [1] M. I. Berenguer, D.Gámez, A. L.Linares, "Fixed point techniques and Schauder bases to approximate the solution of the first order nonlinear mixed Fredholm–Volterra integro-differential equation". *Journal of Computational and Applied Mathematics*, (2013)252, 52-61.
- [2] M.Gachpazan, O.Baghani, "Hyers-Ulam stability of Volterra integral equation". *International Journal of Nonlinear Analysis and Applications*, 2010, 1(2), 19-25.
- [3] M. Akkouchi. "Hyers-Ulam-Rassias stability of nonlinear Volterra integral equations via a fixed point approach". *Acta Universitatis Apulensis*, 26(2011), 257-266.

## ON STATISTICAL E-CONVERGENCE OF DOUBLE SEQUENCES

Yurdal SEVER<sup>1</sup>, Özer TALO<sup>2</sup>

<sup>1</sup>*Department of Mathematics, AfyonKocatepe University,  
Afyonkarahisar/TURKEY  
[yurdalsever@hotmail.com](mailto:yurdalsever@hotmail.com)*

<sup>2</sup>*Department of Mathematics, Celal Bayar University,  
Manisa/TURKEY  
[ozertalo@hotmail.com](mailto:ozertalo@hotmail.com)*

**Abstract:** In this paper we have introduced the concepts of statistical e-limit superior and e-limit inferior for real double sequences and proved some fundamental properties of  $st\_e$ -limit superior and inferior. Using the concept of statistical e-convergence for double real sequences, we obtain a Korovkin-type approximation theorem for double sequences of positive linear operators defined on the space of all  $2\pi$ -periodic and real valued continuous functions on the real two-dimensional space. Furthermore, we display an application which shows that our new result is stronger than its classical version.

**Keywords:** Double sequence space, e-convergence, statistical e-convergence, Positive linear operator, Korovkin-type approximation theorem.

## THE VARIATIONAL FORMULATION OF AN INVERSE PROBLEM FOR A PARABOLIC EQUATION

Yusuf KOÇAK

*<sup>1</sup>Department of Mathematics, Ağrı İbrahim Çeçen University,  
İstanbul/TURKEY  
[ykocak27@hotmail.com](mailto:ykocak27@hotmail.com)*

**Abstract:** In this presentation, the variational formulation of an inverse problem for a parabolic equation is considered. The existence and uniqueness of solution of variational problem is proved. The necessary condition for this solution is given.

**Keywords:** Variational problem, Inverse Problem, Parabolic equation

### References:

- [1] Y. Koçak, M.A. Dokuyucu, "On a necessary condition for optimal control of hyperbolic equation", AIP Conf. Proc. 1726, 020085 (2016)
- [2] M.Abbas, T. Nazir, "A new faster iteration process applied to constrained minimization and feasibility problems", Matematicki Vesnik, 66(2014), 223.
- [3] R.Tagiev, "Optimal Coefficient Control in Parabolic Systems", Differential Equations, 2009, Vol. 45, No. 10, pp. 1526–1535.
- [4] Y. Koçak, E. Çelik, N. Y. Aksoy "A note on Optimal Control Problem Governed by Schrödinger Equation", Open Physics. Volume 13, Issue 1, ISSN (Online) 2391-5471.

## COMPACTNESS OF FRACTIONAL MAXIMAL OPERATOR IN WEIGHTED $L^{p(x)}(0, \ell)$ SPACE

Yusuf ZEREN<sup>1</sup>, Lutfi AKIN<sup>2</sup>

<sup>1</sup>*Yildiz Technical University, Science Faculty, Department of Mathematic*

*Email: [yzeren@yildiz.edu.tr](mailto:yzeren@yildiz.edu.tr)*

<sup>2</sup>*Mardin Artuklu University, Faculty of Economics and Administrative Sciences*

*Department of Business Administration*

*Email: [lutfiakın@artuklu.edu.tr](mailto:lutfiakın@artuklu.edu.tr)*

**Abstract:**  $B(x, r) = \{y \in \mathbb{R}^n : |x - y| < r\}$  and  $B(x, r) = B(x, r) \cap \Omega$ ,

$\Omega$  is a non-empty open set in  $\mathbb{R}^n$ ,  $d_\Omega$  denotes the diameter of  $\Omega$

$$\rho_{p(\cdot)}(f) = \int_0^l |f(x)|^{p(x)} dx < \infty \text{ modul function (finite), if there is}$$

$$\text{ess sup}_{x \in (0, l)} p(x) < \infty \text{ then } f \text{ modul is}$$

$$\|f\|_{L^{p(\cdot)}(0, l)} = \inf \left\{ \lambda > 0 : \rho_{p(x)} \left( \frac{f}{\lambda} \right) < \infty \right\}$$

$$w(x)^{p'(x)} \in L^1(B(0, a)), \quad v(x)^{q(x)} \in L^1(a, l); \quad V(x) = \int_x^l v(y)^{q(y)} dy,$$

$$W(x) = \int_0^x w(y)^{p'(y)} dy$$

**Theorem:** Let  $f(x) \geq 0$  measurable functions with  $p^- > 1$ ,  
 $q(0) \geq p(0) > 1$ .

If there are conditions  $\limsup_{t \rightarrow 0} V(t)^{1/q(0)} W(t)^{1/p'(0)} = 0$  and

$\sup_{t \in (0, \infty)} V(t)^{1/q(0)} W(t)^{1/p'(0)} < \infty$ . Then from  $L^{p(\cdot)}(0, l)$  to  $L^{q(\cdot)}(0, l)$

$$M^{a(\cdot)} f(x) = \sup_{r>0} \frac{1}{|B(x, r)|^{1-\frac{a(x)}{n}}} \int_{\bar{B}(x, r)} f(y) dy$$

fractional maximal operator is compact.

## NEW SOLUTIONS OF THE SPACE-TIME FRACTIONAL SHARMA-TASSO-OLVER EQUATION WITH CONFORMABLE DERIVATIVE

Yücel ÇENESİZ<sup>1</sup>, Orkun TAŞBOZAN<sup>2</sup>, Ali KURT<sup>3</sup>, Olaniyi Samuel IYIOLA<sup>4</sup>

<sup>1</sup>*Department of Mathematics, Selçuk University,  
Konya/TURKEY*

[ycenesiz@selcuk.edu.tr](mailto:ycenesiz@selcuk.edu.tr)

<sup>2</sup>*Department of Mathematics, Mustafa Kemal University,  
Hatay/TURKEY*

[otasbozan@mku.edu.tr](mailto:otasbozan@mku.edu.tr)

<sup>3</sup>*Department of Mathematics, Mustafa Kemal University,  
Hatay/TURKEY*

[alikurt@mku.edu.tr](mailto:alikurt@mku.edu.tr)

<sup>4</sup>*Department of Mathematical Sciences, University of Wisconsin-  
Milwaukee Wisconsin, USA*

[osiyiola@uwm.edu](mailto:osiyiola@uwm.edu)

**Abstract:** The main purpose of this article is to find the exact and approximate solutions of conformable space-time fractional Sharma-Tasso-Olver equation using first integral method (FIM) and q-homotopy analysis method (q-HAM) respectively. The obtained exact and numerical solutions are compared with each other. Also, the numerical results obtained by q-HAM are compatible with the exact solutions obtained by FIM; hence, it is clearly seen that these techniques are powerful and efficient in finding approximate and exact solutions for nonlinear conformable fractional PDEs.

**Keywords:** First Integral Method; Sharma-Tasso-Olver Equation; q-Homotopy Analysis Method; Conformable Fractional Derivative.

### References:

- [1] A. Kurt, Y. Cenesiz, O. Tasbozan, On the Solution of Burgers Equation with the New Fractional Derivative, *Open Phys.* 13, 355 (2015).
- [2] O.S. Iyiola, G.O. Ojo, On the analytical solution of Fornberg-Wthitham equation with the new fractional derivative, *Pramana Journal of Physics*, 85, 567-575 (2015).
- [3] T. Abdeljawad, On conformable fractional calculus. *J. Comput. Appl. Math.* 279, 57-66 (2015).

## NONCOMMUTATIVE SPACE AND 2D SCHRÖDINGER EQUATION WITH CENTRAL POTENTIAL

Slimane ZAIM, Hakim GUELMAMENE

*<sup>1</sup>Department of physics , Batna1 University,  
Batna/TURKEY  
[zaim69slimane@yahoo.com](mailto:zaim69slimane@yahoo.com)*

**Abstract:** We obtain exact solutions of the 2D Schrödinger equation with the Singular Even-Power Potential in non-commutative space, using the Power-series expansion method. Hence we can say that the Schrödinger equation in non-commutative space describes to the particles with spin  $(1/2)$  in an external uniform magnetic field. Where the noncommutativity play the role of magnetic field with created the total magnetic moment of particle with spin  $1/2$ , who in turn shifted the spectrum of energy. Such effects are similar to the Zeeman splitting in a commutative space.

**Keywords:** Central potential, Noncommutative Geometry.

### References:

- [1] Shi-. Hai Dong and all, Exact solutions of the Schrödinger equation with Singular Even-Power potential in two dimensions
- [2] L. Witten, Gravitation: An introduction to Current Research. Wiley, New York (1962).
- [3] Shi-. Hai Dong, Exact solutions of the two -dimensional Schrödinger equation with certain potentials, International Journal of Theoretical Physics. Vol.39 ,No.4, (2000).
- [4] Shi-Hai Dong, Zhong-Qi Ma, Giampiero Esposito, Exact solutions of the. Schrödinger equation with Inverse-Power Potential, Found.Phys.Lett. 12 (1999) 465-474.

## DETERMINING THE CENTER OF GRAVITY AND SIMILARITY MEASURES OF SEQUENCE SPACES OF TRIANGULAR FUZZY NUMBERS

Zarife ZARARSIZ

*Department of Mathematics, NevşehirHacıBektaşVeli University,  
Nevşehir/TURKEY*

[zarifezararsiz@nevsehir.edu.tr](mailto:zarifezararsiz@nevsehir.edu.tr)

**Abstract:** In this presentation, firstly, we mention  $(t_1, t_2)$ - type fuzzy numbers and their algebraic operations, shortly. After, we calculate the COG(center of gravity) points of a sequence of  $(t_1, t_2)$ - type triangular fuzzy numbers. Furthermore, we present the methods to measure the degree of similarity between sequences of  $(t_1, t_2)$ - type fuzzy numbers. By this way, we contribute to the fuzzy risk analysis.

**Keywords:** Fuzzy number, COG, similarity measure, fuzzy risk analysis, sequence space.

### References:

- [1] L. A. Zadeh, "Fuzzy sets", Information and Computation, 8(1965), 338-353.
- [2] S.-J. Chen, S.-M. Chen, "Fuzzy risk analysis based on similarity measures of generalized fuzzy numbers, "IEEE Transactionson Fuzzy Systems, 11(2003), 45-56.
- [3] R. Kangari, L. S. Riggs, "Construction risk assessment by linguistics", IEEE Transactions on Engineering Management, 36(1992), 126-131.
- [4] S. -M. Chen, "New methods for subjective mental workload assessment and fuzzy risk analysis", Cybernetics and Systems, 27(1996), 449-472.
- [5] Z. Zararsız, M. Şengönül, "On the gravity of center of sequence of fuzzy numbers", Annals of Fuzzy Mathematics and Informatics, 6(2013), 479-485.

## OBTAINING MATHEMATICAL MODELS OF THE PIEZOELECTRIC SYNTHETIC JET

Zeynep EKİCİOĞLU KÜZECİ<sup>1</sup>, Celal Sami TÜFEKÇİ<sup>2</sup>

<sup>1</sup>*Department of Mechanical Engineering, Ahi Evran University,  
Kırşehir/TURKEY*

*[zeynepkicioglu@gmail.com](mailto:zeynepkicioglu@gmail.com)*

<sup>2</sup>*Undersecretariat for Defence Industries,  
Ankara/TURKEY*

*[celal.tufekci@gmail.com](mailto:celal.tufekci@gmail.com)*

**Abstract:** In this study mathematical models of a piezoelectric driven synthetic jet was obtained via bond graphs technique. Synthetic jets are known as a mechanism that can blow and absorb the fluid through an orifice by movement of the diaphragm. Mathematical expressions, transfer function, state space representation and port-Hamiltonian model of the system were found by the bond graphs representation which is a graphical method and based on the energy flow between the system elements. Different representations of the system were simulated with MATLAB and the results similarity with each other were determined.

**Keywords:** Bond graphs, modeling, synthetic jet, port-Hamiltonian representation.

### References:

- [1] Z. EkicioğluKüzeci., C. S. Tüfekçi , "Sentetik Jetin Toplu Parametrelili Modelinin Bond Grafiği Tekniği Kullanılarak EldeEdilmesi" Otomatik Kontrol Ulusal Toplantısı (2014).
- [2] A. Glezer, M. Amitay, "Synthetic jets", Annual Review of Fluid Mechanics, 34, 1, 503-529, (2002).
- [3] B. Koçer, C.S. Tüfekçi, "Sentetik Jet Sistemlerinin Modellenmesi", Otomatik Kontrol Ulusal Toplantısı (2013).



## LACUNARY $I_\sigma$ -CONVERGENCE

Uğur ULUSU<sup>1</sup>, Fatih NURAY<sup>1</sup>

<sup>1</sup>*Department of Mathematics, AfyonKocatepeUniversity,  
Afyonkarahisar/TURKEY  
[ulusu@aku.edu.tr](mailto:ulusu@aku.edu.tr), [fnuray@aku.edu.tr](mailto:fnuray@aku.edu.tr)*

**Abstract:** In this study, the concept of lacunary invariant uniform density of any subset  $A$  of the set  $\mathbb{N}$  of positive integers is defined. Associate with this, the concept of lacunary  $I$ -invariant convergence for real number sequences is given. Also, we examine relationships between this new type convergence concept and the concepts of lacunary invariant summability, strongly lacunary  $q$ -invariant convergence and lacunary invariant statistical convergence which are studied in this area before. Finally, introducing lacunary  $I^*$ -invariant convergence concept and lacunary  $I$ -invariant Cauchy sequence concepts, we give the relationships among these concepts and relationships with lacunary  $I$ -invariant convergence concept.

**Keywords:** Statistical convergence, lacunary sequence, invariant convergence,  $I$ -convergence,  $I$ -Cauchy sequence.

## EXISTENCE AND NONEXISTENCE FOR NONLINEAR PROBLEM

B. ABDELLAOUI<sup>1</sup>, K. BIROUD<sup>1</sup>, J. DAVILA<sup>2</sup>, AND F. MAHMOUDI<sup>2</sup>

<sup>1</sup>*Departement de Mathématiques, Université Abou Bakr Belkaid, Tlemcen 13000, Algeria.*

[boumediene.abdellaoui@uam.es](mailto:boumediene.abdellaoui@uam.es), [khbiroud@yahoo.fr](mailto:khbiroud@yahoo.fr)

<sup>2</sup>*Departamento de Ingeniería Matemática, CMM, Universidad de Chile, Casilla 170-3 Correo 3, Santiago, CHILE.*

[jdavila@dim.uchile.cl](mailto:jdavila@dim.uchile.cl), [fmahmoudi@dim.uchile.cl](mailto:fmahmoudi@dim.uchile.cl)

**Abstract:** Let  $\phi \subset \mathbb{R}$  be a bounded regular domain of  $\mathbb{R}$ . We consider the following class of elliptic problem

$$\begin{cases} -\Delta u = \frac{u^q}{d^2} & \text{in } \Omega \\ u > 0 & \text{in } \Omega \\ u = 0 & \text{on } \partial\Omega \end{cases}$$

where  $0 < q \leq 2^* - 1$ . We investigate the question of existence and nonexistence of positive solutions depending on the range of the exponent  $q$ .

**Keywords:** Hardy inequality, Nonlinear elliptic problems, singular weight.

## MAXIMUM PRINCIPLE FOR OPTIMAL CONTROL PROBLEM OF FORWARD BACKWARD WITH A JUMP IN THE MEAN-FIELD MODEL

N. CHAOUCHKHOUANE, B. LABED and L. TAMER

*University of Biskra, PO box 145, Biskra, Algeria*  
tamerlazhar@yahoo.fr

**Abstract:** We prove a necessary and sufficient condition for optimal control of controlled forward-backward stochastic differential equation with random jumps in the mean-field type. The coefficients of our system depend on the law of the solution, the control variable is allowed to enter both diffusion and jumps coefficients.

## ON A SOLUTIONS IN $PC(0,b;X)$ OF SOME INTEGRAL EQUATION WITH APPLICATION TO AN IMPULSIVE SEMILINEAR DIFFERENTIAL EQUATION

Leila AITKAKI<sup>1</sup>, Nadjat ABADA<sup>2</sup>

<sup>1</sup>*Department of Mathematic and informatics, ENSC,  
Constantine/Algeria*  
[leilaitkaki@yahoo.fr](mailto:leilaitkaki@yahoo.fr)

<sup>2</sup>*Department of Mathematic and informatics, ENSC,  
Constantine/Algeria*  
[b65abada@yahoo.fr](mailto:b65abada@yahoo.fr)

**Abstract:** This paper is devoted to establishing the existence of solutions of some integral equation with Krasnosel'skij's theorem in the space  $PC(0;b,X)$ . The Hausdorff measure of noncompactness and the Monch's theorem are used. An application to solving a first order semilinear impulsive differential equation with nonlocal conditions is given.

**Keywords:** impulsive differential equations, fixed point theorem, mild solution, measure of noncompactness.

### References:

- [1] S. Ji, G. Li, A unified approach to nonlocal impulsive differential equations with the measure of noncompactness, *Advances in Difference Equations*. (2012), 182. 1-19.
- [2] S. Wen, S. Ji, An existence theorem of impulsive differential equations with non local conditions, *Int. J. Nonlinear Sci.* 14. (2012), 186-192.
- [3] L. Zhu, Q. Dong, G. li, Impulsive differential equations with nonlocal conditions in general Banach spaces, *Advances in Difference Equations*. (2012), 1-12.

## PERSISTENCE AND GLOBAL STABILITY IN A BEDDINGTON-DEANGELIS TYPE THREE SPECIES FOOD CHAIN

W. KHELLAF

*Department of Mathematics, SeddikBenyahia University,  
Jijel/Algeria  
wahiba\_khellaf@yahoo.fr*

**Abstract:** Our investigation concerns the three-dimensional continuous time dynamical system which models a predator-prey food chain. This model is based on the Beddington-DeAngelis-type functional response. Primarily, we study from the viewpoint of permanence (uniform persistence). The Beddington-DeAngelis functional response is similar to the Holling type-II functional response but contains a term describing mutual interference by predators. Also, we establish criteria under which we have boundedness of solutions, existence of an attracting set. Finally, by constructing a proper Lyapunov function, we obtain a sufficient condition for global stability of the positive equilibrium.

**Keywords:** Boundedness, Uniform persistence, Global stability, Lyapunov functional.

### References:

- [1] M. A. Aziz-Alaoui, "Study of a Leslie-Gower-type tritrophic population model," *Chaos, Solitons and Fractals*, vol. 14, no. 8, (2002), 1275-1293.
- [2] H. I. Freedman and S. G. Ruan, "Uniform persistence in functional-differential equations," *Journal of Differential Equations*, vol. 115, no. 1, (1995), 173-192.
- [3] J. K. Hale and P. Waltman, "Persistence in infinite-dimensional systems," *SIAM Journal on Mathematical Analysis*, vol. 20, no. 2, (1989) 388-395.
- [4] P. Y. H. Pang and M. Wang, "Strategy and stationary pattern in a three-species predator-prey model," *Journal of Differential Equations*, vol. 200, no. 2, (2004), 245-273.
- [5] Y. Yang, S. Ruan and D. Xiao, "Global stability of an age-structured virus dynamics model with Beddington-DeAngelis infection function," *Mathematical Biosciences and Engineering*, vol. 12, no. 4, (2015), 859-877.

## POSTER SESSION

### ON THE PARABOLIC EQUATION WITH NONLOCAL CONDITIONS

Abdelhak Berkane and Abdelkrim Zekri

University Frères Mentouri-Constantine, Faculty of Sciences Exact,  
Departement of Mathematics  
Corresponding author: [berkane@usa.com](mailto:berkane@usa.com)

**Abstract:** In this work, we consider a boundary value problem for parabolic equation with integral conditions as boundary conditions and instead of the initial value condition we imposed the nonlocal condition of integral type. We obtain sufficient conditions for the unique solvability of the considered problem in  $L_{\infty}(p)$  ( $1 \leq p < \infty$ ) space.

**Keywords.** Parabolic Equation, Abstract Differential Equation, Semigroup with singularity, Integral condition.

**References:**

- [1] J. R. Cannon, The solution of the heat equation. Subject to the specification of energy, Quart. Appl. Math., 21, 155-160 (1963).
- [2] Yu. T. Sil'chenko, Ordinary differential operator with irregular boundary conditions, Sib. Mat., Zh., 40, No. 1, 183-190 (1999); English transl. in Sib. Math. J., 40 (1999).

### A NONLOCAL SPECTRAL PROBLEM

Abdelkrim Zekri and Abdelhak Berkane

University Frères Mentouri-Constantine,  
Faculty of Sciences Exact,  
Department of Mathematics  
Corresponding author: [zekri6080@gmail.com](mailto:zekri6080@gmail.com)

**Abstract:** We consider a second-order ordinary differential operator with a spectral parameter and homogeneous integral conditions containing the unknown function and its derivative. We obtain an a priori estimate of the solution for sufficiently large values of the parameter. Also we prove the Fredholm solvability of the problem.

**Keywords.** Differential equation, integral condition, Fredholm property, priori estimate.

**References:**

- [1] M. S. Agranovich and M. I. Vishik; Elliptic problems with a parameter and parabolic problems general form, Uspekhi Mat. Sciences. 1964. 19. S.53-161.
- [2] Darovskaya K. A and Skubachevskii A. L; A spectral problem with integral conditions, Proceedings of the Seminar. Petrovskii 2010.

### FIXED POINT THEOREM AND EM ALGORITHM

Ahsene LANANI<sup>1</sup>, Rahima BENCHABI<sup>2</sup>

<sup>1</sup>*Department of Mathematics, FreresMentouri University,  
Constantine/ALGERIA  
[Aalanani1@yahoo.fr](mailto:Aalanani1@yahoo.fr)*

<sup>2</sup>*Department of Mechanical Engineering, FreresMentouri University,  
Constantine/ALGERIA  
[rbenchabi@yahoo.fr](mailto:rbenchabi@yahoo.fr)*

**Abstract:** When we are confronted with solving nonlinear equations which do not admit explicit solutions, we must use approximate methods based on iterative processes or algorithms. One of the best known iterative methods is the fixed point theorem, often applied in analysis or algebra. In our case, we will apply this method in a stochastic context. By means of this application, we show the relationship between this method and the EM algorithm, which is an iterative process, often applied in statistics.

**Keywords:** Fixed point, EM algorithm, linear model, nonlinear equation.

**References:**

- [1] R.P. Agarwal, M. Meehan, D.O'Regan, "Fixed Point Theory and Applications", Cambridge University Press, 2001.
- [2] J. Dugundji, A. Granas, "Fixed Point Theory", Springer-Verlag, 2003.
- [3] W.A. Kirk, M.A. Khamisi, "An Introduction to Metric Spaces and Fixed Point Theory", John Wiley, New York, 2001.
- [4] W.A. Kirk, S. Brailey, "Handbook of Metric Fixed Point Theory", Springer-Verlag, 2001.
- [5] A.P. Dempster, N.M. Laird, D.B. Rubin, "Maximum likelihood with incomplete data via the E-M algorithm", *Journal of the Royal Statistical Society*, 39(1977), 1-38.
- [6] N.M. Laird, J.H. Ware, "Random effects models for longitudinal data", *Biometrics*, 38(1982), 963-974.
- [7] J.L. Foulley, F. Jaffrézic, C.R. Granié, "EM-REML estimation of covariance parameters in gaussian mixed models for longitudinal data analysis", *Genetics Selection Evolution*, 32(2000), 129-141.

## A NEW MODIFIED SCHEME FOR LINEAR SHALLOW-WATER EQUATIONS

Aicha BOUSSAHA

*Department of Mathematics, National Superior School  
of Mines and Metallurgy, Annaba, Algeria*  
[boussahaaicha@yahoo.fr](mailto:boussahaaicha@yahoo.fr)

**Abstract:** In this presentation, we propose a modified scheme [1] for simulating irregular wave trains (IWTs) propagation dispersive of tsunami with suitable initial and boundary conditions by applying the alternating direction implicit (ADI) method. The convergence, stability and consistency criteria of the scheme have been studied. We introduce a weakly dissipative terms into improved linear Boussinesq equations (ILBqs) that permits the mathematical tool to simulating a transoceanic propagation dispersive of tsunami in both ocean and laboratory experimental. The new numerical dispersion of the proposed model is manipulated to replace the physical dispersion of (ILBqs) by controlling dispersion-correction parameters. The new model developed in this study is applied to propagation of Heraklion tsunami scenario1 (HTS1) of the 365 AD earthquake. The resulting scheme is efficient and practical to implement. Furthermore, a comparison between the present results with another existing numerical method has been reported and we found that they are in a good agreement.

**Keywords:**

Improved Linear Boussinesq equations; Numerical dispersion-correction parameter; ADI scheme; Dissipation effects; Tsunamis

**References:**

- [1] AichaBoussaha, AbdelhamidLaouar, AllaouaGuerziz, Hossam .Hassan, A new modified scheme for linear shallow-water equations with distant propagation of irregular wave trains tsunami dispersion type for inviscid and weakly viscous fluids, Global Journal Pure and Applied Mathematics., ISSN 0973-1768 Volume 10, Number 6 (2014), pp. 793-815.

## ELECTRO-VISCOELASTIC ANTIPLAN CONTACT PROBLEM WITH POWER FRICTION LAW

Allaoua BOUDJEDOUR and Mohamed DALAH

*Department of Mathematics,*

*Faculty of Sciences*

*University Mentouri Constantine, Algeria*

[haboudjedour@yahoo.fr](mailto:haboudjedour@yahoo.fr)

**Abstract:** In this paper we present an antiplane contact problem where the material is considered electro-viscoelastic and the friction is modeling by the power friction law. First, we derive the mathematical model, and we try to construct the variational formulation. Then we establish the existence of a unique weak solution to the model.

**Keywords:** Contact problem, electro-viscoelastic material, variational formulation, power friction law.

### References:

- [1] Rabinowicz E. (1965): Friction and Wear of Materials. — New York: Wiley.
- [2] Horgan C.O. (1995): Anti-plane shear deformation in linear and nonlinear solid mechanics. — SIAM Rev., Vol. 37, No. 1, pp. 53–81.

## HIGH ORDER BOUNDARY VALUE PROBLEMS AT RESONANCE ON AN UNBOUNDED INTERVAL

Assia FRIOUI

**Abstract:** The aim of this paper is the solvability of a class of higher order differential equations with initial conditions and an integral boundary condition on the half line. Using coincidence degree theory by Mawhin and constructing suitable operators, we prove the existence of solutions for the posed resonance boundary value problems.

## THE FRACTIONAL-ORDER MATHEMATICAL MODELING OF BACTERIAL RESISTANCE AGAINST MULTIPLE ANTIBIOTICS IN CASE OF LOCAL BACTERIAL INFECTION

Bahatdin DAŞBAŞI<sup>1</sup>, Emre Hayri BARAZ<sup>2</sup>

<sup>1</sup>Department of Computer Technologies, Cumhuriyet University, Sivas/TURKEY  
[dasbasi\\_bahatdin@hotmail.com](mailto:dasbasi_bahatdin@hotmail.com)

<sup>2</sup>Department of Banking and Insurance, Cumhuriyet University, Sivas/TURKEY  
[emrebaraz@gmail.com](mailto:emrebaraz@gmail.com)

**Abstract:** The proposed local bacterial infection model in this study is fractional-order form of model suggested in [1]. In this respect, the population sizes of sensitive and resistant bacteria to multiple antibiotics at time  $t$  is denoted by  $S$  and  $R$ , respectively. In addition that, the concentration of the  $i$ -th antibiotic,  $i = 1, 2, \dots, n$  is showed by  $C_i(t)$ . Therefore, it is obtained the following system of  $(n + 2)$  fractional-order differential equation:

$$\begin{aligned} D^\alpha S(t) &= \beta_s S \left(1 - \frac{S + R}{K}\right) - S \sum_{i=1}^n (\bar{q}_i + \bar{\alpha}_i) C_i - \mu_s S \\ D^\alpha R(t) &= \beta_r R \left(1 - \frac{S + R}{K}\right) - S \sum_{i=1}^n \bar{q}_i C_i - \mu_r R \\ D^\alpha C_i(t) &= \Lambda_i - \mu_i C_i, \quad i = 1, 2, \dots, n \end{aligned} \quad (1)$$

where  $\alpha \in (0, 1]$ . The parameters used in the model (1) are as follows: it is presumed that bacteria follow a logistic growth with carrying capacity  $K$ . The parameter  $\beta_s$  and  $\beta_r$  are the birth rate of susceptible and resistant bacteria, respectively. The sensitive and resistant bacteria to multiple antibiotics have per capita natural death rates  $\mu_s$  and  $\mu_r$ , respectively. During the administration of the  $i$ -th antibiotic, a number of resistant bacteria to it can be showed up due to mutations of exposed sensitive bacteria to such antibiotic, it is modeled this situation by the term  $\bar{q}_i C_i S$  where  $\bar{q}_i$  is the mutation rate of sensitive bacteria due to exposure to  $i$ -th antibiotic. Sensitive bacteria also die due to the action of the antibiotics, and it is assumed that this situation in model is by the term  $\bar{\alpha}_i C_i S$ , where  $\bar{\alpha}_i$  is the death rate of sensitive bacteria due to exposure to  $i$ -th antibiotic...



## CHELYSHKOV COLLOCATION APPROACH FOR A MODEL DESCRIBING BIOLOGICAL SPECIES LIVING TOGETHER

Cem OĞUZ<sup>1,2</sup>, Mehmet SEZER<sup>2</sup>

<sup>1</sup>*Department of Mathematics, Ahi Evran University,  
Kırşehir/TURKEY*

[cem.oguz@ahievran.edu.tr](mailto:cem.oguz@ahievran.edu.tr)

<sup>2</sup>*Department of Mathematics, Celal Bayar University,  
Manisa/TURKEY*

[mehmet.sezer@cbu.edu.tr](mailto:mehmet.sezer@cbu.edu.tr)

**Abstract:** In this presentation, a numerical technique called Chelyshkov collocation method has been developed to solve a system of two nonlinear integro-differential equations which arises in biological model problems. This technique is essentially based on the truncated Chelyshkov series and its matrix representations together with collocation points. Also, to demonstrate the validity and applicability of technique, several test problems are given and the results are compared with the results of some existing methods in literature.

**Keywords:** System of nonlinear integro-differential equations, Chelyshkov polynomials and series, Biological species, Collocation points.

### References:

- [1] Y.Khan, H.Vázquez-Leal, Q. Wu, "An efficient iterated method for mathematical biology model", *Neural Computing and Applications*, 23(2013), 677–682.
- [2] E. Babolian, J. Biazar, "Solving the problem of biological species living together by Adomian decomposition method", *Applied Mathematics and Computation*, 129(2002), 339–343.
- [3] F. Shakeri, M. Dehghan, "Solution of a model describing biological species living together using the variational iteration method", *Mathematical and Computer Modelling*, 48(2008), 685–699.
- [4] S. Yousefi, "Numerical solution of a model describing biological species living together by using Legendre multiwavelet method", *International Journal of Nonlinear Science*, 11(1)(2011), 109–113.

## EXISTENCE OF SOLUTIONS FOR $P(X)$ -SOLITONS TYPE EQUATIONS IN SEVERAL SPACE DIMENSIONS

Dellal ABDELKADER<sup>1</sup>, Henderson JOHNNY<sup>2</sup>, Ouahab ABDELGHANI<sup>3</sup>

<sup>1</sup>*Department of Mathematics / Ecole Normale Supérieure–Kouba,  
Alger / Algeria  
[adellal@yahoo.fr](mailto:adellal@yahoo.fr)*

<sup>2</sup>*Department of Mathematics / Baylor University USA  
Baylor / USA  
[Johnny\\_Henderson@baylor.edu](mailto:Johnny_Henderson@baylor.edu)*

<sup>3</sup>*Laboratory of Mathematics / Univ Sidi Bel Abbes, Algeria  
Sidi Bel Abbes / Algeria  
[Agh\\_ouahab@yahoo.fr](mailto:Agh_ouahab@yahoo.fr)*

**Abstract:** In this presentation, we study a class of Lorentz invariant nonlinear field equations in several space dimensions. The main purpose is to obtain soliton-like solutions with variable exponent. The fields are characterized by a topological invariant, we call the charge. We prove the existence of a static solution which minimizes the energy among the configurations with nontrivial charge.

**Keywords:** Soliton, variational calculus, variable exponents and splitting lemma.

### References:

- [1] A. Dellal, J. Henderson, A. Ouahab, Existence of solutions for  $p(x)$ -Soliton type equations in Several Space Dimensions, Panamer. Math. J , Vol. 25(2015), No.4, pp. 35 – 56.
- [2] V.BENCI; D'AVENIA P; FORTUNATO D. AND PISANI L; Solitons in several space dimensions: Derrick's problem and infinitely many solutions, Arch. Ration. Mech. Anal. 154 (2000), 297–324.
- [3] L. Diening, P. Harjulehto, P. Hästö & M. Ruzicka, Lebesgue and Sobolev spaces with variable exponents, Lecture Notes in Mathematics, vol. 2017, Springer-Verlag, Heidelberg, 2011.

## THE EXISTENCE OF SOLUTIONS FOR A FRACTIONAL-ORDER BOUNDARY VALUE PROBLEM

Dondu OZ<sup>1</sup>, Ilkay KARACA<sup>2</sup>

<sup>1</sup>*Department of Mathematics, Ege University,  
İzmir/TURKEY  
[donduayhan@gmail.com](mailto:donduayhan@gmail.com)*

<sup>2</sup>*Department of Mathematics, Ege University,  
İzmir/TURKEY  
[ilkay.karaca@ege.edu.tr](mailto:ilkay.karaca@ege.edu.tr)*

**Abstract:** In this study, we are investigated the existence of solutions for a fractional-order boundary value problem by using some fixed point theorem on the cone. An example is also given to illustrate the main result.

**Keywords:** Fractional-order, fixed point theorem, boundary value problem.

### References:

- [1] R. P. Agarwal, D. O' Regan, M. Meehan, "Fixed point theory and applications", Cambridge University Press, (2004).
- [2] M. Dalir, M. Bashaur, "Applications of fractional calculus", *Mathematical Sciences*, Vol. 4(2010), 1021-1032.
- [3] A.A. Kilbas, H.M. Srivastava, J.J. Trujillo, "Theory and applications of fractional differential equations", *North-Holland Mathematics Studies*, 204(1999), 69-79p.
- [4] I. Podlubny, "Fractional differential equations", Academic Press (1999).
- [5] S. Liang and J. Zhang, "Existence of three positive solutions of m-point boundary value problems for some nonlinear fractional differential equations on an infinite interval", *Computers and Mathematics with Applications* (2011), 3343-3354p.
- [6] P.S.V. Nataraj, "Fractional calculus and fractional differential equations with SCILAB", *SGGS IE and T* (2010), Nanded, April 23-25.
- [7] M. Rehman and R.A. Khan, "Existence and uniqueness of solutions for multi-point boundary value problems for fractional differential equations", *Applied Mathematics Letters*, 23(2010), 1038-1044 pp.

## PROPERTIES OF MINIMIZING CURVES FOR GEOMETRIC OPTIMAL CONTROL PROBLEMS

Driai Nedjoud

University of Setif 1, Algeria

[ndriai@yahoo.fr](mailto:ndriai@yahoo.fr)

**Abstract:** The optimal control theory is a very important part of the optimization problem solving optimal control problems. In this paper we give a geometric approach to a problem of optimal control, where it uses the basic concepts of calculus of variations, such as the Euler-Lagrange equation as a necessary condition for optimality, the principle maximum of Pontriaguine (PMP), which gives an analytical aspect to the optimal control problem and allows us to study some property functions that defines the criterion to minimize the regularity of solutions (minima or maxima). One other very important aspect is the geometric aspect that used to find the geodesics (surveying), their natures, their numbers requires a geometric background as fields, vector, vector spaces, eligible curve... So in may define an optimal control problem governed by EDO geometrically by giving some conditions.

**Keywords.**

optimal control, the principle of maximum Pontriaguine, calculus of variations.

## A NEW APPROACH OF THE CUTTING PLANE ALGORITHM USING INTERIOR POINT METHOD

El Amir DJEFFAL

*Department of Mathematics, University of Batna 2,*

*Batna, ALGERIA*

[djeffal\\_elamir@yahoo.fr](mailto:djeffal_elamir@yahoo.fr)

**Abstract:** This paper deals with the computation of cutting plane algorithm using interior point method, with a special application to the solution of convex differentiable programming problems. The interior point method is closely related to the classical method of path following, but the cuts are generated from different, more central, points in order to achieve deeper cuts and thereby accelerate convergence. The method is quite general in purpose as it can be applied to a large class of convex differentiable and nondifferentiable optimization problems.

**Keywords:** Convex optimization, Cutting plane algorithm, Interior point method, Path following algorithm.

### References:

- [1] E.W. Cheney and A.A. "Goldstein, Newton's method of convex programming and Tchebycheff approximation", Numer. Math. 1 (1959) 253-268.
- [2] J.E. Kelley, "The cutting plane method for solving convex programs", J. Sot. Industrial Appl. Math. 8 (1960) 703-712.
- [3] El. A. Djeflal, L. Djeflal, F. Benoumelaz, Finding a strict feasible dual solution of a convex optimization problem. Afrika Matematika (springer), Volume 27, Issue 1, pp 13-21, 2016.

## ON THE GENERALIZATION OF THE GRAPH-DIRECTED ITERATED FUNCTION SYSTEMS

Yunus ÖZDEMİR<sup>1</sup>, Fatma Diğdem YILDIRIM<sup>2</sup>

<sup>1</sup>*Department of Mathematics, Anadolu University, Eskişehir, TURKEY*  
[yunuso@anadolu.edu.tr](mailto:yunuso@anadolu.edu.tr)

<sup>2</sup>*Department of Mathematics, Anadolu University, Eskişehir, TURKEY*  
[fdyildirim@anadolu.edu.tr](mailto:fdyildirim@anadolu.edu.tr)

**Abstract:** In this presentation, we first introduce classical (hyperbolic) iterated function systems (IFS), countable iterated function systems (CIFS) and graph-directed iterated function systems (GIFS). Then we define the notion of graph-directed countable iterated function system (GCIFS) as a generalization of CIFS to the graph-directed case in the sense of Secelean (see [4,5]). We also give some novel examples as an attractor of some GCIFS.

**Keywords:** Iterated function systems (IFS), countable IFS, graph-directed IFS.

### References:

- [1] M.F. Barnsley, "Fractals everywhere", Academic Press, 1988.
- [2] G. Edgar, "Measure, Topology and Fractal Geometry", Springer, New York, 2008.
- [3] J. Hutchinson, "Fractals and Self Similarity", Indiana Univ. J. Math., 30(1981), 713–747.
- [4] N.A. Secelean, "Countable Iterated Function Systems", Far East Journal of Dynamical Systems, Pushpa Publishing House, 3(2)(2001), 49–167.
- [5] N.A. Secelean, "Countable Iterated Function System", Lambert Academic Publishing, 2013.

## APPROXIMATION OF THE UNILATERAL CONTACT PROBLEM BY THE FINITE ELEMENT METHOD

Frekh TAALLAH

Department of Mathematics, Badji Mokhtar University,  
Annaba/ALGERIA  
*frekh2003@yahoo.fr*

**Abstract:** Several problems in mechanic, physics, control and those dealing with contacts lead to study of systems of variational inequalities. In this study we considered a deformed elastic solid with a unilateral contact of a rigid body. This model has been studied by Lions, J.L. and G. Stampacchia [8]. In this paper, we studied the existence, uniqueness and continuity of the deformation of this solid with respect to the data.

**Keywords:** Contact, variational inequalities, finite element methods.

### References:

- [1] Bernadou, M. and P.G. Ciarlet, 1994. Existence theorems for two-dimensional linear shell theories. *J. Elasticity*, 34: 111-113.
- [2] Bernardi, C., Y. Maday and F. Rapetti, 2004. *Discrétisations variationnelles de problèmes aux limites elliptiques*. Collection "Mathématiques et Applications"45, Springer-Verlag, ISBN: 3540213694, pp. 310.
- [3] Brezis, H., 1983. *Analyse fonctionnelle*, Collection Mathématiques Appliquées pour la Maîtrise.
- [4] Brezis, H. and G. Stampacchia, 1968. Sur la régularité de la solution d'inéquations elliptiques. *Bull. Soc. Math. France* (96): 153-180.
- [5] Ciarlet, P.G., 1978. *The Finite Element Method for Elliptic Problems*. North-Holland, Amsterdam, New-York, Oxford, ISBN 0444850287, pp. 530.
- [6] Lions, J.L. and G. Stampacchia, 2005. Variational inequalities. *Comm. Pure Appl. Math* 20, pp. 493-519.

## SOME SPECIAL CURVES AND MANNHEIM CURVES IN THREE DIMENSIONAL EUCLIDEAN SPACE

Funda KAYMAZ<sup>1</sup>, Ferdağ KAHRAMAN AKSOYAK<sup>2</sup>

<sup>1</sup>*Department of Mathematics, Ahi Evran University,*

*Kırşehir/TURKEY*

[f\\_kaymaz@outlook.com](mailto:f_kaymaz@outlook.com)

<sup>2</sup>*Department of Mathematical Education, Ahi Evran University, Kırşehir/TURKEY*

[ferda.kahraman@yahoo.com](mailto:ferda.kahraman@yahoo.com)

**Abstract:** In this paper we investigate some special curves which have Mannheim curves and Mannheim partner curves and obtain some characterizations about them.

**Keywords:** Mannheim curves, Mannheimpartner curves, curvature, torsion

### References:

- [1] Blum R., A Remarkable Class of Mannheim-Curves, *Canad. Math. Bull.*, Vol. 9(2), 223-228, 1966.
- [2] Liu H.Wang F. Mannheim partner curves in 3-space, *J. Geom.* 88, 120-126 (2008)
- [3] Mannheim A.; *Paris C. R.*, 86, 1254-1256, 1878.



## LAMB SHIFT IN HYDROGEN LIKE ATOM INDUCED FROM NON COMMUTATIVE QUANTUM SPACE TIME

Hakim GUELMAMENE

*Department of physics, Batna 1 University, ALGERIA*

[hakphy@yahoo.com](mailto:hakphy@yahoo.com)

**Abstract:** In In this work we present an important contribution to the non-commutative approach to the hydrogen atom to deal with lamb shift corrections. This can be done by studying the Klein-Gordon equation in a non-commutative space-time as applied to the Hydrogen atom to extract the energy levels, by considering the second-order corrections in the non commutativity parameter and by comparing with the result of the current experimental results on the Lamb shift of the 2P level to extract a bound on the parameter of non-commutativity. Phenomenologically we show that the non-commutativity effects induce lamb shift corrections.

**Keywords:** Klein-Gordon equation, non-commutative space, quantum Hydrogen atom.

### References:

- [1] S. Doplicher, K. Fredenhagen and J.E. Roberts, Phys.Lett. B331, 39(1994).
- [2] S. Doplicher, K. Fredenhagen and J.E. Roberts, Commun. Math. Phys. 172, 187 (1995).
- [3] S. Zaim, A. Boudine, N. Mebarki, M. Moumni, Rom. Journ. Phys., Vol. 53, Nos. 3-4, P. 445-462 (2008).
- [4] N. Mebarki, S. Zaim, L Khodja and H Aissaoui Phys. Scripta 78 045101(2008).
- [5] A. Stern Phys. Rev. Lett. 100 061601 (2008).

## MODELING AND CONTROL FOR NONLINEAR SYSTEM

Hachemi GLAOUI

*Faculté des Sciences et technologies  
Université de Béchar. BP 417 Béchar, 08000, Algerie.  
glaouih@yahoo.fr*

**Abstract:** Continuous processes in the plastics, textile paper and other industries, require several drives working in synchronism. The aim of this paper is to control speed of the winding system, and to maintain a constant mechanical tension between the rollers of the system. Several controllers are considered, including sliding-mode control (SMC) single input/single output (SISO) and SMC multi input/multi output (MIMO) and Proportional-integral (PI/MIMO). Since the PI control method can be applied easily and is widely known, it has an important place in control applications. But this method is insensitive to parameter changes. The advantage of an SMC is its robustness and ability to handle the non-linear behaviour of the system. The main contribution of this paper consists of designing MIMO sliding mode control law of a distributed parameter based on the original model for which the control variables are coupled. The performances of the control law are illustrated by means of simulations and compared to previous results obtained by SISO and (PI-MIMO) control laws.

**Keywords:** component; Winding system, induction machine Proportional-integral (PI), sliding mode control

### References:

- [1] Christian Thiffault Pierre Sicard Alain Bouscayrol TENSION CONTROL LOOP USING A LINEAR ACTUATOR BASED ON THE ENERGETIC MACROSCOPIC REPRESENTATION CCECE 2004-CCGEI 2004, Niagara Falls, May/mai 2004
- [2] S. Charlemagne, A. Bouscayrol, Slama-Belkhodja, J.P. Hautier, "Flatness based control of non-linear textile multimachine process", in Proc. of EPE'03, CD-ROM, Toulouse (France), September 2003.
- [3] Adlane Benlatreche Dominique Knittel "State Feedback Control with Full or Partial Integral Action for Large Scale Winding Systems" Industry Applications Conference, 2005. Vol. 2 page(s): 973- 978 Oct 2005

## EXISTENCE OF POSITIVE SOLUTIONS FOR SOME SYSTEMS OF SINGULAR SECOND-ORDER DIFFERENTIAL EQUATIONS

Karima MEBARKI<sup>1</sup>, Smail DJEBALI<sup>2</sup>

<sup>1</sup>*Department of Mathematics, Bejaia University,  
Béjaia/ALGERIA*

[mebarqi\\_karima@hotmail.fr](mailto:mebarqi_karima@hotmail.fr)

<sup>2</sup>*Department of Mathematics, Ecole Normale Supérieure, Algiers/ALGERIA*  
[djebali@hotmail.com](mailto:djebali@hotmail.com)

**Abstract:** In this work, we are concerned with the existence and the multiplicity of nontrivial positive solutions for a boundary value problem of a second-order differential equations system subject to an integral boundary condition and posed on the positive half-line. The positive nonlinearities depend on the solution and their derivatives and may have space singularities. New existence results of single and multiple solutions are obtained by means of the fixed point index theory on special cones in some weighted Banach spaces. Examples with numerical computations are included to illustrate the obtained existence theorems. This work surveys and generalizes previous works.

**Keywords:**

Second-order differential equations, systems, positive solutions, fixed point theory.

**References:**

- [1] R. P. Agarwal, D. O'regan, "A coupled system of boundary value problems", *Appl. Anal.*, 69 (1998), 381-385.
- [2] S. Djebali, K. Mebarqi, "Existence results for a class of Bvps on the positive half-line", *Comm. Appl. Nonlin. Anal.*, 14(2) (2007), 13-31.
- [3] S. Djebali, K. Mebarqi, "On the singular generalized Fisher-like equation with derivative depending nonlinearity", *Appl. Math. Comput.*, 205 (2008), 336-351.
- [4] A.M. Fink and J.A. Gatica, "Positive solutions of second order system of boundary value problems", *J. Math. Anal. Appl.*, 180 (1993) 93-108.

## ON INVARIANT WIDE BAND NOISE FILTER

Kanda ABUASSBA

*Department of Mathematics, Eastern Mediterranean University,  
Cyprus/TURKEY*

[kinda.joudeh@gmail.com](mailto:kinda.joudeh@gmail.com)

**Abstract:** Kalman filtering is one of the most essential results of filtering theory. Originally it was set as a method for estimating linear systems disturbed by white noise process. Later on it was proved that the real noises are not exactly white, they are wide band. The noticeable characteristic of wide band noises is that they are observed only by autocovariance functions, which means that infinitely many distinct wide band noises may have the same autocovariance function. In this presentation we introduce an invariant result of linear filtering when the signal and observations are disturbed by independent wide band noise and white noise, respectively. The important feature of this result is that it depends on the autocovariance function and free of the relaxing function.

**Keywords:** Kalman filtering, white noise, wide band noise.

### References:

- [5] Kalman R.E., A new approach to linear filtering and prediction problems, Transactions ASME, Ser. D (J. Basic Engineering), Vol. 82, 1960, pp. 35-45.
- [6] Kalman R.E. and Busy R.S., New results in linear filtering and prediction theory, Transactions (1961), 59-108.
- [7] . Fleming W.M. and Rishel R.W., Deterministic and Stochastic Optimal Control, Springer-Verlag, 1975, 222 p.
- [8] Bashirov A.E., Problem 2.1. On error of estimation and minimum of cost for wide band noise driven systems, in: Eds: V.D. Blondel and A. Megretski, Unsolved problems in mathematical systems and control theory, Princeton University Press, 2004, pp. 67-73.

## ANALYSE AND STUDY OF ANTIPLANE ELECTRO-VISCOELASTIC CONTACT PROBLEM

Hacene Chaouche SOUMEYA<sup>1</sup>, Mohamed DALAH<sup>1</sup> and Allaoua BOUDJEDOUR<sup>1</sup>

*<sup>1</sup>Department of Mathematics, Faculty of Sciences,  
Mentouri University Constantine,  
Constantine / Algeria  
[dalah.mohamed@yahoo.fr](mailto:dalah.mohamed@yahoo.fr)*

**Abstract:** In this work we assume that the material is electro-elastic and the friction is modeled with Tresca's law and the foundation is assumed to be electrically conductive. First we derive the well posedness mathematical model. In the second step, we give the classical variational formulation of the model which is given by a system coupling an evolutionary variational equality for the displacement field and a time-dependent variational equation for the potential field. Then we prove the existence of a unique weak solution to the model by using the Banach fixed-point Theorem.

### References:

- [1] W. Han and M. Sofonea. Quasistatic Contact Problems in Viscoelasticity and Viscoplasticity. Studies in Advanced Mathematics, Americal Mathematical Society, Providence, RI-International Press, Somerville, MA, 2002.
- [2] M. Dalah. Analyse of a Electro-Viscoelastic Antiplane Contact Problem With Slip-Dependent Friction. Electronic Journal of Differential Equations. N°. 118, 1-15, (2009)

## ON FINITE ELEMENT APPROXIMATION IN THE $L^{\infty}$ - NORM OF SYSTEM OF PARABOLIC QUASI- VARIATIONAL INEQUALITIES RELATED TO STOCHASTIC CONTROL PROBLEMS

Mohamed El Amine BENCHEIK LE HOCINE

<sup>1</sup>*Department of Mathematics, Tamanrasset University Center,  
Tamanrasset/ALGERIA  
[kawlamine@gmail.com](mailto:kawlamine@gmail.com)*

**Abstract:** This paper deals with the numerical analysis of system of parabolic quasi variational inequalities related to stochastic control problems. An optimal  $L^{\infty}$ -convergence of a piecewise linear finite element method is established using the concept of subsolution and discrete regularity.

**Keywords:** Parabolic quasi variational inequalities, Hamilton-Jacobi-Bellman equation, finite element methods, subsolutions method,  $L^{\infty}$ -asymptotic behavior.

### References:

- [6] M. Boulbrachene, M. Haiour, B. Chentouf, On a noncoercive system of quasi-variational inequalities related to stochastic , Journal of Inequalities in Pure and Applied Mathematics. 3(2002), 1-14.
- [7] Messaoud Boulbrachene, On the finite element approximation of the impulse control quasivariational inequality, Mathematical Models , Methods and Application, (2015), 107-126.
- [8] M. A. Bencheikh Le Hocine, M. Haiour, Algorithmic approach for the asymptotic behavior of a system of parabolic quasi variational inequalities , Applied Mathematics Sciences, 7(2013), 909 - 921.
- [9] Mohamed Amine Bencheikh Le Hocine, Salah Boulaaras, Mohamed Haiour, An optimal  $L^{\infty}$ -error estimate for an approximation of a parabolic variational inequality, Numerical Functional Analysis and Optimization, 37(2016), 1-18.V.
- [10] Salah Boulaaras, Mohamed Amine Bencheikh le Hocine, Mohamed Haiour, The finite element approximation in a system of parabolic quasi-variational inequalities related to management of energy production with mixed boundary condition, Computational Mathematics and Modeling, 25 (2014), 530-543.
- [11] J. Nitsche,  $L^{\infty}$ -convergence of finite element approximations, In Mathematical Aspects of Finite Element Methods, Lect. Notes Math., 606(1977), 261-274.

## THE EFFECT OF ALLEE FACTOR ON STABILITY IN A NONLINEAR DISCRETE-TIME POPULATION MODEL INVOLVING DELAY

Özlem AK GÜMÜŞ

<sup>1</sup>*Department of Mathematics, Adiyaman University,  
Adiyaman/TURKEY  
[akgumus@adiyaman.edu.tr](mailto:akgumus@adiyaman.edu.tr)*

**Abstract:** In this study, I will present the effect of Allee factor on the local stability of equilibrium point of the discrete-time population model involving delay generated for  $k=1$  in [1] with a different approach. The results demonstrate that the Allee effect either reduces the local stability of equilibrium point of the population dynamic model or increases.

**Keywords:** Allee effect, Discrete-time models, Local stability

### References:

- [1] J. R. Graef, C. Quian, "Global stability in a nonlinear difference equation, *Journal of Difference Equations and Applications* 5(1999), 251-270.
- [2] H. Merdan, O. Ak Gumus, Stability analysis of a general discrete-time population model involving delay and Allee effects, *Applied Mathematics and Computation* 219(2012), 1821-1832.
- [3] O. Ak Gumus, H. Kose, On the stability of delay population dynamics related with Allee effects, *Mathematical and Computational Applications* 17(2012), 56-67.
- [4] O. Ak Gumus, H. Kose, Allee effect on a new delay population model and stability analysis, *Journal of Pure and Applied Mathematics: Advances and Applications* 7(2012), 21-31.
- [5] W. C. Allee, *Animal Aggregations: A Study in General Sociology*, University of Chicago Press, Chicago, (1931).

## OPTIMAL CLAIM BEHAVIOUR FOR VEHICLE DAMAGE INSURANCES

S.SEGNI

<sup>1</sup>*Department of Mathematics, University of Guelma,  
Box 401, 24000 Guelma/Algeria  
[segnianis@gmail.com](mailto:segnianis@gmail.com)*

**Abstract:** In this paper we analyse the optimal claim behavior of a risk sensitive of a risk sensitive policy holder having a vehicle damage insurance.

It is proved that the optimal decision is of the form : to claim for damages only if its amount exceeds a certain limit. Moreover, we also derive the optimal stopping rule to terminate the insurance. Finally, some computational results are presented.

**Keywords:** Bonus-malus systems; Automobile insurance; Markov decision processes.

### References:

- [1] V. Bijsoort, "Optimal claim behavior for insurances on hull and appurtenances mappings", Erasmus University, Rotterdam.
- [2] Howard, R and J.Matheson "Risk-sensitive Markov decision processes.Stochastic Modelling and Analysis : A Computational Approach. Wiley, New York.

## VOLTERRA INTEGRO-DIFFERENTIAL EQUATIONS OF CONVOLUTION TYPE

Sami SEGNI

*Department of Mathematics, Guelma University, Guelma, Algeria.*

**Abstract:**In this poster, the operational matrices of piecewise constant orthogonal functions on the interval  $[0,1)$  are used to solve Volterra integro-differential equations of convolution type without solving any system. Begin we obtain Laplace transform of the problem and then we find numerical inversion of Laplace transform by operational matrices. Examples are given to illustrate our results.

**Keywords:**Volterra integro-differential equation; Piecewise constant orthogonal functions; Laplace transforms; Inversion of Laplace transform.



## THE WEAK SOLUTION OF ANTIPLANE ELECTRO-VISCOELASTIC CONTACT PROBLEM WITH REGULARIZED FRICTION LAW

Hacene Chaouche SOUMEYA and Mohamed DALAH

*Department of Mathematics,  
Faculty of Exact Sciences  
University Mentouri Constantine, Algeria*  
[samara\\_avenir@yahoo.fr](mailto:samara_avenir@yahoo.fr)  
[dalah.mohamed@yahoo.fr](mailto:dalah.mohamed@yahoo.fr)

**Abstract:** In this work we study the weak solution of the antiplane electro-viscoelastic problem with regularized friction law. In addition to the mathematical interest in the convergence result when the viscosity is very small, this is of importance from an electro-mechanical point of view, as it indicates that the case of elasticity with friction may be considered as a limit case of visco-elasticity with friction.

**Keywords:** Contact problem, antiplane, friction, formulation variationnelle, electro-visco-elasticity.

### References:

- [1] M. Sofonea, M. Dalah, Antiplane Frictional Contact of ElectroViscoelastic Cylinders, *Electronic Journal of Differential Equations*, Vol. 2007(2007), No. 161, pp. 114.
- [2] N. Strömberg, *Continuum Thermodynamics of Contact, friction and wear*, These de Ph.D, Linköping.

## NEW EXACT SOLUTIONS OF NONLINEAR PARTIAL DIFFERENTIAL EQUATIONS USING TRIAL EQUATION METHOD

Riadh HEDLI, Abdelouahab KADEM

*Department of Mathematics, Ferhat ABBES University  
Setif/ALGERIA*

[riadh\\_al19@yahoo.fr](mailto:riadh_al19@yahoo.fr), [abdelouahabk@yahoo.fr](mailto:abdelouahabk@yahoo.fr)

**Abstract:** Nonlinear partial differential equations have a significant role in several scientific and engineering fields. These equations appear in solid state physics, fluid mechanics, chemical kinetics, plasma physics, population models, nonlinear optics, and many others. Many mathematicians and physicists work in the field using a variety of powerful methods to study nonlinear phenomena, such as the inverse scattering method, the Bäcklund transformation method, the Darboux transformation, Hirota's bilinear transformation, the homogeneous balance method, the tanh method, sine-cosine method, the exp-function method, the G'/G-expansion method, and so on. These methods derived many solutions to most nonlinear evolution equations. Recently, Professor Liu proposed a powerful method called trial equation method for finding exact solutions to nonlinear differential equations. By using his method, the nonlinear differential equation is reduced to an ordinary differential equation under the travelling wave transformation. Then, the ODE is reduced to the elementary integral form. Finally, the complete discrimination system for polynomial is used to solve the corresponding integrals. We can obtain the classification of all single travelling wave solutions to the equation. This idea is competent to solve divers types of nonlinear differential equations. The trial equation method and complete discrimination system for polynomial give a lot of new solutions to many nonlinear differential equations that are presented in this paper.

**Keywords:** The Nonlinear Partial Differential Equation, Complete Discrimination System for Polynomial, Trial Equation Method, Exact solution.

### References:

- [1] C. S. Liu, "Trial Equation Method to Nonlinear Evolution Equations with Rank Inhomogeneous: Mathematical Discussions and Its Applications," *Communications in Theoretical Physics*, Vol. 45, No. 2, 2006, 219-223.
- [2] C. S. Liu, "Using Trial Equation Method to Solve the Exact Solutions for two kinds of KdV Equations with Variable Coefficients," *Acta Physica Sinica*, Vol. 54, No. 10, 2005, p. 4506.

## A STUDY OF THE APPLICATION OF CHAOS TO THE GLOBAL OPTIMIZATION

Tayeb HAMAIZIA

*Department of Mathematics, Faculty of Sciences Exacts, University Constantine 1  
Algeria.*

[h2tayeb@gmail.com](mailto:h2tayeb@gmail.com)

**Abstract:** In this communication we undertake a performance analysis for a new class of evolutionary algorithms called chaos optimization algorithm (COA), recently proposed by Caponetto and al. [1], [2], [3], It was originally proposed to solve nonlinear optimization problems with bounded variables. Different chaotic mapping have been considered, combined with several working strategy. In this work, a chaotic strategy is proposed based on a new two-dimensional discrete chaotic attractor. Experiments results showed that the proposed algorithm can achieve good performance.

**Keywords:** Chaos; Chaos optimization; discrete map ; Global optimization.

### References:

- [1] T. Hamaizia, R. Lozi, An improved chaotic optimization algorithm using a new global locally averaged strategy, *Journal of Nonlinear Systems and Applications* 3 (2) (2012) 58-63.
- [2] L. S. Coelho, Tuning of PID controller for an automatic regulator voltage system using chaotic optimization approach, *Chaos, Solitons and Fractals*, 39, 2009, 1504-1514.
- [3] B. Li, W.S. Jiang, Chaos optimization method and its application, *Journal of Control Theory and*

## DETERMINATION OF SOME NON LINEAR GROWTH CURVES WITH THE SUM OF SQUARE REDUCTION TEST FOR TURKEYS REARING IN FREE RANGE SYSTEM

Ufuk KARADAVUT<sup>1</sup>, Atilla TAŞKIN<sup>2</sup>, Mehmet Emin YAZICI<sup>3</sup>

<sup>1</sup>*Department of Biometry and Genetic, Ahi Evran University, Kırşehir/TURKEY*  
[ukaradavut@ahievran.edu.tr](mailto:ukaradavut@ahievran.edu.tr)

<sup>2</sup>*Department of Animal Science, Ahi Evran University, Kırşehir/TURKEY*  
[ataskin@ahievran.edu.tr](mailto:ataskin@ahievran.edu.tr)

<sup>3</sup>*Department of Animal Science, Science Institute, Kırşehir/TURKEY*  
[emn\\_0602@hotmail.com](mailto:emn_0602@hotmail.com)

**Abstract:** In this study was aimed to determine non linear growth curves of live weight of turkey breed British United Turkeys (BUT) Big 6 in rearing free range system. For this, turkeys were grown for 8-20 weeks. Live weights were modeled with fitting Generalized Logistic, Logistic and Gompertz growth curves. Coefficient of Determination ( $R^2$ ), residual sum of square (RSS) and mean square error (MSE) were used as comparison criteria. As results, growth curve fitting revealed that Generalized Logistic (0,951) and Logistic models (0,953) provided similar  $R^2$ , but they had lower than RSS (953,247 and 954,122) and MSE values (12,36 and 13,25) according to Gompertz model. Gompertz model showed in high RSS (1026,2) and MSE (26,35) values both for sex and low value of  $R^2$ (0,912). According to the sum of square reduction test, female have the highest live weight potential (5208 g), as male have the smaller (4502 g).

**Key Words:** Growth Curves, Free Range System, Modeling, Turkeys

### References:

- [1] Draper, N.R. and H. Smith, 1998. Applied Regression Analysis. John Wiley and Sons, New York
- [2] Karadavut, U. and S.A. Kayış, 2006. A growth curve application to compare weights of five wheat varieties. J. Agric. Fac. University Selçuk, 40: 107–110.
- [3] Karadavut, U., S.A. Kayış, Ç. Palta and O.Okur, 2008. A Growth Curve Application to Compare Plant Heights and Dry Weights of Some Wheat Varieties. American-Eurasian J. Agric. Environ. Sci., 3: 888– 892.

## LOCAL CONDITIONS FOR THE EXISTENCE OF CYCLES

Zineb BENMEZIANE

*Université des sciences et de la technologie Houari Boumediene  
Faculté de Mathématiques , Département de Recherche Opérationnelle  
Bp 32 ElAlia, Algiers (Algeria)  
[zbenmeziane@yahoo.fr](mailto:zbenmeziane@yahoo.fr)*

**Abstract:** In this presentation, we deal with the existence of cycles in a particular extension of claw-free-graphs namely the quasi-claw-free graphs. A graph  $G$  is quasi-claw-free if for any two vertices  $x$  and  $y$  with distance 2 there exist a vertex  $u \in N(x) \cap N(y)$  such that  $N(u) \subseteq N[x] \cup N[y]$ .

In this paper, we are interested in local conditions on graphs such as triangularly connected graphs. A graph  $G$  is triangularly connected if for every pair of edges  $e_1, e_2 \in E(G)$ ,  $G$  has a sequence of triangles  $T_1, T_2, \dots, T_l$  such that  $e_1 \in T_1, e_2 \in T_l$  and  $E(T_i) \cap E(T_{i+1}) \neq \emptyset$  for  $1 \leq i \leq l-1$ .

We prove that every triangularly connected quasi-claw-free graph is almost fully cycle extendable. Therefore, Ainouche's conjecture is once again solved.

**Keywords:** Cycles, Hamiltonicity, connected, claws.

### References:

- [1] A.Ainouche, Quasi claw free graphs. Discrete Math.179(1998).
- [2] M. X.Qu and H.Lin, Quasilocally Connected, Almost Locally Connected, or Triangularly connected graphs. Discrete Geometry, Combinatorics(2007).
- [3] E.X.Y.Qu and J.Wang, Vertex pancyclicity in quasi –claw-free graphs. Discrete Math.309(2009).

## MAPPINGS BETWEEN C\*- ALGEBRAS THAT PRESERVE THE SPECTRUM

Hakan AVCI<sup>1</sup>, Nilay SAGER<sup>2</sup>

<sup>1</sup>, Department of Mathematics, Ondokuz Mayıs University,  
Samsun/TURKEY

[hakanav@omu.edu.tr](mailto:hakanav@omu.edu.tr)

<sup>2</sup>, Department of Mathematics, Ondokuz Mayıs University, Samsun/TURKEY

[nilay.sager@omu.edu.tr](mailto:nilay.sager@omu.edu.tr)

**Abstract:** In this study, we show that a  $*$  - homomorphism  $\varphi : A \rightarrow B$  between unital commutative  $C^*$ - algebras  $A$  and  $B$  which verify  $r_B(\varphi(x)) = r_A(x)$  for any  $x \in A_+$  satisfies the property to preserve spectrum and hence adjoint mapping  $\varphi^* : \Delta(B) \rightarrow \Delta(A)$  is surjective, that is,  $\varphi^*$  maps maximal ideal space of  $B$  to maximal ideal space of  $A$ .

**Keywords:**  $C^*$ - algebra, Gelfand transform, maximal ideal, spectrum, complex homomorphism, topological divisor of zero.

### References:

- [1] J.B.Conway, "A Course in Functional Analysis(Second Edition)", Springer - Verlag, New York (1990).
- [2] J.Dixmier, "C\*- Algebras", Elsevier North - Holland Publishing Company, New York (1977).
- [3] E.Kaniuth, ". A Course in Commutative Banach Algebras", Springer - Verlag, New York (2009).
- [4] G.J.Murphy, "C\* - Algebras and Operator Theory", Academic Press, San Diego (1990).
- [5] W.Rudin, "Functional Analysis(Second Edition)", Academic Press, San Diego (1991).
- [6] N.Sager,H.Avcı, "Some Spectrum Properties in C\*- Algebras", Turkish Journal of Science & Technology, 10(2015), 27-30.
- [7] N.Sager, "Some Spectrum Properties in C\*- Algebras", Master' s thesis, Ondokuz Mayıs University, Samsun (2015).

## EXISTENCE OF MINIMAL AND MAXIMAL SOLUTIONS FOR A SECOND ORDER QUASILINEAR DYNAMIC EQUATION WITH INTEGRAL BOUNDARY CONDITIONS

Mohammed DERHAB<sup>1</sup>, Mohamed NEHARI<sup>2</sup>

<sup>1</sup>*University Abou-BekrBelkaidTlemcen, Department of Mathematics  
Tlemcen, Algeria  
[derhab@yahoo.fr](mailto:derhab@yahoo.fr)*

<sup>2</sup> *Dynamic Systems and Applications Laboratory  
Preparatory School of Economy  
Tlemcen, Algeria  
[Nehari\\_72@yahoo.fr](mailto:Nehari_72@yahoo.fr)*

**Abstract:** This work is concerned with the construction of the minimal and maximal solutions for a second order quasilinear dynamic equation with integral boundary conditions, where the nonlinearity is a continuous function. We also give an example to illustrate our results.

**Keywords:** Integral boundary conditions, upper and lower solutions, monotone iterative technique, time scale, p-Laplacian.

## INDEX

### A

A. BENRABAH .....	40
A. BOULAOUAD .....	34
A. EROGLU .....	22, 48, 306
A. H. ADOUM .....	218
A. N. MAMMADOVA .....	64
A. Neşe DERNEK .....	129, 271
A. Turan GÜRKANLI .....	242
A.E. ABDULLAYEVA .....	35
Abbes RABHI .....	36
Abdelaziz AZEB AHMED .....	69
Abdelhak Berkane .....	324
Abdelkader BENALİ .....	38
Abdelkrim Zekri .....	324
Abdelmalek KOUADRI .....	171
Abdelmejid BAYAD .....	37
Abdelouahab KADEM .....	346
Abderrazek CHAOUI .....	39
Abdul Rahim KHAN .....	30
Abdulcabbar SÖNMEZ .....	208
Abdulhamit KUCUKASLAN .....	39
Abdulkadir DOGAN .....	41, 42
Abdulkadir KARAKAŞ .....	43
Abdullah KABLAN .....	76
Abdullah ÖZBEKLER .....	44
Abdullah YENER .....	45
Abdullatif YALÇIN .....	51
Adrian PETRUŞEL .....	28
Aftab ALAM .....	46
Ahmet DAŞDEMİR .....	47
Ahmet Hamdi AVSAR .....	49
Ahmet Ocak AKDEMİR .....	50, 51
Ahmet Sinan CEVIK .....	163
Ahmet ŞAHİNER .....	127, 226
Ahsene LANANI .....	325
Ahu ERCAN .....	52
Aicha BOUSSAHA .....	326
Akhlad IQBAL .....	48
Akshaya DEVI .....	53
Alexander E. LABOVSKY .....	87
Ali AKBULUT .....	53
Ali FARAJZADEH .....	31, 68
Ali Hakan TOR .....	54
Ali KARAİSA .....	55, 56
Ali KURT .....	317
Allaoua BOUDJEDOUR .....	327, 341
Alper EKİNCİ .....	50
Alper KORKMAZ .....	240
Aly R. SEADAWY .....	57
Anwar JA'AFAR .....	58
Arezki KHELOUFI .....	59

Arife Aysun KARAASLAN .....	60
Arshed A. AHMAD .....	206
Asif YOKUŞ .....	61, 89
Assia FRIOUI .....	327
Atilla TAŞKIN .....	348
Atok ZULIJANTO .....	286
Ayhan ESİ .....	279
Ayhan ŞERBETÇİ .....	62
Aykut Ahmet AYGÜNEŞ .....	63
Aynur ŞAHİN .....	65
Aysun SOYSAL .....	66
Aysun YURTTAS .....	163
Ayşe Betül KOÇ .....	67
Aytekin ERYILMAZ .....	287
Azadeh HOSSEINPOUR .....	68

### B

B. ABDELLAOUI .....	22, 321
B. LABED .....	322
B. MEROUANI .....	34
Badreddine MANSOURI .....	70
Bağdagül KARTAL .....	72
Bahaettin CENGİZ .....	73
Bahatdin DAŞBAŞ .....	328
Bahatdin DAŞBAŞI .....	294
Banu AYTAR GÜNTÜRK .....	73
Bapurao DHAGE .....	280
Bariş ÇELİK .....	74
Baver OKUTMUŞTUR .....	75
Bayram BALA .....	76
Benabdderrahmane BENYATTOU .....	77
Bilal ALTAY .....	189, 250
Bilal ÇAVDAR .....	56
Birol GÜNDÜZ .....	230
Boubaker-Khaled SADALLAH <sup>2</sup> .....	59
Boukerrioua KHALED .....	78
Boussetila NADJIB .....	77
Burak DİKİCİ .....	253
Burak KURT .....	79
Bülent DEMİR .....	80
Bülent YILMAZ .....	244
Bünyamin AYDIN .....	81, 82
Büşra BALKAŞ .....	137

### C

Cafer AYDIN .....	186
Cahit KÖME .....	83
Canan Akkoyunlu .....	216
Canay AYKOL YÜCE .....	84
Celal Sami TÜFEKÇİ .....	320



Cem OĞUZ.....	329
Cemil TUNC.....	100
Chiheb TARIK.....	85
Cihan ÜNAL.....	85
Coşkun YAKAR.....	164

### Ç

Çiğdem A. BEKTAŞ.....	281
-----------------------	-----

### D

Dellal ABDELKADER.....	330
Derya SEKMAN.....	86
Dilek ERKMEN.....	87
Djabrane YAHIA.....	88
Doğan KAYA.....	89
Dondu OZ.....	331
Driai Nedjoua.....	332
Duran TÜRKOĞLU.....	217, 306

### E

Eberhard MALKOWSKY.....	111
Ebrahim ZAMANI.....	138
Ecem ACAR.....	90
Egemen HALICI.....	91
El Amir DJEFFAL.....	333
Elgiz BAIRAMOV.....	289
Elif DEMİRCİ.....	92
Elimhan MAHMUDOV.....	128, 276
Ellaggoune FATEH.....	118
Emel KARACA.....	233
Emirhan HACIOGLU.....	93, 307
Emrah Evren KARA.....	94, 188
Emrah YILDIRIM.....	95
Emrah YILMAZ.....	96, 97
Emre TAŞ.....	98
EmreHayri BARAZ.....	328
Erbil ÇETİN.....	99, 304
Erdal KORKMAZ.....	100
Erdal UNLUYOL.....	101
Erdiç DÜNDAR.....	82, 102, 203, 222, 278, 291
Erhan GÜLER.....	102, 103, 235, 273
Erhan SET.....	50, 74, 202
Erkan BOSTANCI.....	91
Ertan İBIKLI.....	277
Esra GÜLLE.....	103
Esra KAMBER.....	104
Esra YOLACAN.....	146
Etibar S. PANAKHOV.....	52
Ezgi ERDOĞAN.....	105, 271

### F

F. Ayça ÇETİNKAYA.....	106
F. MAHMOUDI.....	22, 321
F. REBBANI.....	40
Fadime DİRİK.....	245
Fadime GÖKÇE.....	107
Fahreddin ABDULLAYEV.....	108, 243
Faik GÜRSOY.....	109, 110, 168, 212
Faruk ÖZGER.....	111
Faruk POLAT.....	112
Fatih DERİNGÖZ.....	112
Fatih NURAY.....	102, 222, 321
Fatih SIRIN.....	113
Fatih TAŞÇI.....	117
Fatima BOUDAUD.....	283
Fatma Diğdem YILDIRIM.....	334
Fatma ÖZTÜRK ÇELİKER.....	114
Fayyaz ROUZKARD.....	115
Fella BERRİMİ.....	116
Ferdağ KAHRAMAN AKSOYAK.....	336
Ferhat ŞAH.....	117
Fernane KHAIREDDINE.....	118
Feyzi BAŞAR.....	301
Frekh TAALLAH.....	335
Fridoun MORADLOU.....	119, 266
Fuad KİTTANEH.....	157
Fuat USTA.....	120, 121
Fulya YÖRÜK DEREN.....	122
Funda KAYMAZ.....	336

### G

G. Canan HAZAR.....	123
G. ZAMANI ESKANDANIAND.....	124
Gabil ADILOV.....	152
Gabil M. AMIRALİYEV.....	125, 151, 209, 228
Galip OTURANC.....	272
Gradimir V. MILOVANOVIĆ.....	27
Gulsah OZDEMİR.....	126
Gumrah UYSAL.....	277
Gülden KAPUSUZ.....	127
Gülnare ABDULLAYEV.....	108
Gülseren ÇİÇEK.....	128
Gülşen MENSİMLİ.....	129

### H

Hacene Chaouche SOUMEY.....	345
Hacene Chaouche SOUMEYA.....	341
Hacer Bilgin ELLİDOKUZUOĞLU.....	130, 131
Hacer ŞENGÜL.....	132, 133
Hachemi GLAOUİ.....	338
Hafiz FUKHAR-UD-DİN.....	30
Hafize GÜMÜŞ.....	134

Hakan AVCI.....	350
Hakan PEKEL.....	135
Hakim GUELMAMENE.....	318, 337
Halil EROL.....	136
Halit SAYGILI.....	141
Hamdullah ŞEVLİ.....	137
Hamid VAEZI.....	138
Hamza GUEBBAI.....	139
Hamza MENKEN.....	238
Harun POLAT.....	140, 254
Hasan AKIN.....	117, 141, 210
Hasan BULUT.....	309
Hasan FURKAN.....	187, 189, 290
Hatice ARMUTCU.....	142
Hatice CITAKOGLU.....	293
Hatice YALDIZ.....	143
Henderson JOHNNY.....	330
Hikmet Çağlar.....	216
Hikmet KEMALOĞLU.....	191
Hikmet KOYUNBAKAN.....	96
Hikmet Seyhan ÖZARSLAN.....	72, 288
Hilal BAYINDIR.....	144
Hong-Kun XU.....	26
Houari FETTOUCH.....	145
Hukmi KIZILTUNC.....	146
Huseyin CAKALLI.....	147, 148
Huseyin KAPLAN.....	148
Hüseyin AKSAN.....	149
Hüseyin BUDAK.....	265
Hüseyin KOÇ.....	150

**I**

İbrahim E. INAN.....	273, 309
İlhame AMIRALI.....	125, 151
İlkay KARACA.....	331
İmen HASSAIRI.....	159
İrem KUCUKOGLU.....	153
İsa YILDIRIM.....	213
İsmail Naci CANGUL.....	163, 257
İzhar UDDIN.....	154

**İ**

İbrahim ÇANAK.....	155
İbrahim ERDAL.....	156
İbrahim Halil GÜMÜŞ.....	157
İbrahim ŞANLIBABA.....	158
İdris DAĞ.....	240
İlker GENÇTÜRK.....	160, 169
İlknur YESİLCE.....	152
İmdat İŞCAN.....	269
İnayet DERİN.....	161
İnci EGE.....	95
İsmail AYDIN.....	85, 162
İsmet ARSLAN.....	164

İsmet YILDIZ.....	232
-------------------	-----

**J**

J. DAVILA.....	22, 321
Jan EKSTEEN.....	33
Janpou NEE.....	165
Javid ALI.....	166
Javid IQBAL.....	167
Jeremy LEVESLEY.....	120

**K**

K. BIROUD.....	22, 321
Kadri DOĞAN.....	110, 167, 168
Kanda ABUASSBA.....	340
Kerboua MOURAD.....	168
Kerim KOCA.....	160, 169
Khanlar R. MAMEDOV.....	106, 227
Khier BENMAHAMMED.....	116
Kübra ERDEM BİÇER.....	170

**L**

L. TAMER.....	322
L. AITKAKI.....	212
Lakhdar CHITER.....	171
Lamia HARKAT.....	282
Lamia J.M. AI-MASHHADANI.....	206
Leila AITKAKI.....	322
Lutfi AKIN.....	172, 316

**M**

M. Abdussamed MALDAR.....	173, 196
M. AliSARIGÖL.....	123
M. G.HAJIBAYOV.....	48
M. IMDAD.....	166
M. N. OMAROVA.....	305
M. RAEISI.....	124
M. SENE.....	218
M. Zeki SARIKAYA.....	143, 264, 265
Mahmut İŞİK.....	174
Mahmut KARAKUŞ.....	175, 176
Mahmut UÇMAN.....	136
Makbule KAPLAN.....	177
Manaf MANAFOV.....	76, 178
Mansur İSGENDEROĞLU.....	200
Martin At. STANEV.....	179
Martin MAGID.....	102
Maya ALTINOK.....	180
Md AHMADULLAH.....	181
Md. AHMADULLAH.....	166
Mediha ÖRKÇÜ.....	239
Mehmet Ali BALCI.....	182

Mehmet Ali SARIGÖL.....	107
Mehmet Emin YAZICI.....	348
Mehmet Fatih KARAASLAN.....	183, 201
Mehmet GÜMÜŞ.....	184
Mehmet GÜRDAL.....	303
Mehmet KÜÇÜKASLAN.....	180
Mehmet SEZER.....	170, 329
Mehmet ŞENGÖNÜL.....	274
Mehmet ŞENOL.....	185, 275
Melek Kübra AYHAN.....	186
Meltem KAYA.....	187
Merve AVCI-ARDIÇ.....	51
Merve İLKHAN.....	94, 188
Merve TEMİZER ERSOY.....	189
Meryem ÖZBUNAR.....	190
Mesut COŞKUN.....	191
Metin BAŞARIR.....	65, 94
Mikail ET.....	133, 192, 199
Mohamad JAWAD.....	58
Mohamed BERBICHE.....	193
Mohamed Dalah.....	324
Mohamed DALAH.....	327, 341, 345
Mohamed El Amine BENCHEIK LE HOCINE.....	342
Mohamed HAIOUR.....	197
Mohamed HELLAL.....	198
Mohamed NEHARI.....	351
Mohammad IMDAD.....	46, 181
Mohammad KNEFATI.....	195
Mohammad MURSALEEN.....	25
Mohammed BEGGAS.....	197
Mohammed DERHAB.....	351
Mohammed S. MECHEE.....	194
Moncef DZIRI.....	198
Mouffak BENCHOHRA.....	198
Muge TOGAN.....	163
Muhammad Adil KHAN.....	199
Muhammed ÇINAR.....	199
Muhammed ÇİÇEK.....	164, 200
Muhammet KURULAY.....	201
Muharrem TOMAR.....	202
Mukaddes ARSLAN.....	203
Murat BEŞENK.....	71
Murat CANCAN.....	205
Murat COBANER.....	293
Murat KİRİŞÇİ.....	204
Murat SARI.....	206
Musa BAŞBÜK.....	207
Mustafa AGGUL.....	203
Mustafa ALKAN.....	207
Mustafa AYDIN.....	169
Mustafa Cemil BİŞGİN.....	208
Mustafa Ç. KORKMAZ.....	229
Mustafa KUDU.....	209
Mustapha CHEGGAG.....	231
Mutlay DOGAN.....	210
Müfit ŞAN.....	211
Müzeyyen ERTÜRK.....	110, 212

## N

N. BOUSSETILA.....	40
N. CHAOUCHKHOUEANE.....	322
N. DJITTE.....	218
N.ABADA.....	212
Nadir TRABELSI.....	284
Nadjet ABADA.....	322
Nazli KARACA.....	213
Nazneen KHAN.....	214
Necip ŞİMŞEK.....	215
Neslihan Fatma Er.....	216
Neslihan ZORLU.....	232
Nesrin MANAV.....	217
Nezrin GADIROVA.....	213
Nihal YOKUS.....	219, 221
Nihat AKGÜNEŞ.....	220
Nilay SAGER.....	350
Nimet COSKUN.....	219, 221
Nimet PANCAROĞLU AKIN.....	222
Nour El Houda BOUZARA.....	86, 222
Noureddine BENRABIA.....	223
Nurcan GÜCÜYENEN.....	224
Nurgül OKUR BEKAR.....	225
Nuri ÖZALP.....	241
Nurullah YILMAZ.....	127, 226
Nüket AYKUT HAMAL.....	122

## O

O. DIOP.....	218
Olaniyi Samuel IYIOLA.....	317
Olgun CABRİ.....	227
Omar HİRZALLAH.....	157
Omer YAPMAN.....	228
Orhan Mazlum YAZAR.....	229
Orkun TAŞBOZAN.....	317
Osman ALAGÖZ.....	230
Osman Raşit IŞIK.....	80, 190
Ouahab ABDELGHANI.....	330
Ould Melha KHELLAF.....	231
Oya MERT.....	232
Ozer TALO.....	251

## Ö

Ömer AKGÜLLER.....	182, 233
Ömer Faruk GÖZÜKIZIL.....	299
Ömer KİŞİ.....	103, 235, 273
Özer TALO.....	235, 314
Özge ÇOLAKOĞLU HAVARE.....	238
Özge DALMANOĞLU.....	239
Özlem AK GÜMÜŞ.....	236, 237, 343
Özlem ERSOY HEPSON.....	240
Özlem ÖZTÜRK MIZRAK.....	241

Öznur KULAK ..... 242

**P**

P.VEERAMANI ..... 31  
 Pelin ÖZKARTEPE ..... 243  
 Pembe İPEK ..... 244  
 Pınar OKÇU ..... 245

**Q**

Qamrul Hasan ANSARI ..... 29

**R**

R. A. BANDALIYEV ..... 255  
 R.P.AGARWAL ..... 25  
 RaadM. KADUM ..... 194  
 Rabah DEBBAR ..... 246  
 Rabah LABBAS ..... 231  
 Rahima BENCHABI ..... 325  
 Rahmoune ABITA ..... 77  
 Rais AHMAD ..... 167  
 Ramazan AKGÜN ..... 248  
 Ramazan ÇETİNTAŞ ..... 249  
 Ramazan KAMA ..... 250  
 Ravi P.AGARWAL ..... 99  
 Reha YAPALI ..... 251  
 Remzi TUNTAS ..... 252, 253  
 Rıdvan Cem DEMİRKOL ..... 254  
 Riadh HEDLI ..... 346  
 Richard F. PATTERSON ..... 65  
 Roumaissa BENMARAI ..... 262  
 Rqeeb GUBRAN ..... 181  
 Rza MUSTAFAYEV ..... 300

**S**

S. G.HASANOV ..... 255  
 S.SEGNI ..... 344  
 Saada HAMOUDA ..... 256  
 Sadık DELEN ..... 257  
 Said BELOUL ..... 258  
 Said MAZOUZI ..... 259  
 Sait SAN ..... 260  
 Salah BADRAOUI ..... 261  
 Salah DJEZZAR ..... 262  
 Salem NAFIRI ..... 263  
 Salih AYTAR ..... 263  
 Samet ERDEN ..... 264, 265  
 Sami SEGNI ..... 139, 344  
 Sana DRISS ..... 266  
 Sattar ALIZADEH ..... 266  
 Sebaheddin ŞEVGIN ..... 267  
 Seda KARATEKE ..... 268

Selahattin MADEN ..... 269, 270  
 Selcan KOCABAŞ ..... 271  
 Selma ALTUNDAĞ ..... 104  
 Selman UĞUZ ..... 90  
 Sema Gülbahar ..... 61  
 Sema SERVİ ..... 272  
 Semra SARAÇOĞLU ÇELİK ..... 103, 235, 273  
 Serbay DURAN ..... 273  
 Sercan TURHAN ..... 269  
 Serkan DEMİRİZ ..... 130, 131  
 Sevda ATPINAR ..... 274, 275  
 Sevilay DEMİR ..... 276  
 Sevilay KIRCI SERENBAY ..... 277  
 Sevim YEGÜL ..... 278  
 Sezayi HIZLIYEL ..... 311  
 Sezgin AKBULUT ..... 230  
 Shahla GALANDAROVA ..... 291  
 Shahrbanoo KBARPOOR ..... 96  
 Sibel PAŞALI ATMACA ..... 233  
 Sibel YASEMİN GÖLBOL ..... 279  
 Sidheshwar BELLALE ..... 280  
 Sinan ERCAN ..... 281  
 Slimane ZAIM ..... 318  
 Smail DJEBALI ..... 339  
 Smail KELAIAlA ..... 282  
 SOLEKHUDIN ..... 286  
 Somyot PLUBTIENG ..... 68  
 Sonia RADJEF ..... 283  
 Souad AZRA ..... 284  
 Soumen SHAW ..... 284  
 Stephan HEYNS ..... 33  
 Stéphane MAINGOT ..... 231  
 Suayip TOPRAKSEVEN ..... 285  
 SUMARDI ..... 286  
 SUPAMA ..... 286  
 Sure KÖME ..... 287

**Ş**

Şamil AKÇAĞIL ..... 299  
 Şebnem YILDIZ ..... 288  
 Şerifenur CEBESoy ..... 289  
 Şeyda SOLMAZ ..... 289  
 Şeyhmus YARDIMCI ..... 156  
 Şeyma ÇETİN ..... 234  
 Şeyma ÇEVİK ..... 290  
 Şükrü TORTOP ..... 291

**T**

Tahir GADJIEV ..... 291  
 Taqseer KHAN ..... 292  
 Tayeb HAMAIZIA ..... 347  
 Tedjani HADJ AMMAR ..... 69  
 Tefaruk HAKTANIR ..... 293  
 Teslima DAŞBAŞI ..... 294

Timur AYHAN .....	295, 296
Tuba GULSEN .....	97, 297
Tufan TURACI .....	149, 298
Tuğba AYDEMİR .....	299
Tuğba ŞENLİK ÇERDİK .....	122
Tuğçe ÜNVER .....	300
Tuncay KÖR .....	71
Tülin COŞKUN .....	268

**U**

Ufuk KARADAVUT .....	348
Uğur DEĞER .....	144, 279
Uğur KADAK .....	301
Uğur ULUSU .....	82, 102, 103, 321
Uğur YÜKSEL .....	302
Ulaş YAMANCI .....	303
Ummahan AKCAN .....	304
Umut Mutlu ÖZKAN .....	310

**Ü**

Ümit TOTUR .....	155
------------------	-----

**V**

V.BERİNDE .....	28
Vagif S. GULİYEV .....	32, 142, 305
Vatan KARAKAYA .....	60, 66, 86, 93, 105, 110, 168, 173, 195, 196, 212, 222, 313
Vildan ÖZTÜRK .....	306

**W**

W. KHELLAF .....	323
------------------	-----

**Y**

Y. Y.MAMMADOV .....	306
Y.PELİN .....	306
Yakup HAMEŞ .....	161
Yasin YAZLIK .....	83, 207
Yavuz ALTIN .....	308
Yavuz ALTIN .....	43
Yavuz UĞURLU .....	273, 309
Yavuz YAZICI .....	310
Yeşim SAĞLAM ÖZKAN .....	311
Yıldırım KESKİN .....	272
Yılmaz ALTUN .....	167
Yılmaz SIMSEK .....	37, 126, 153
Yunus ATALAN .....	307, 313
Yunus Emre YILDIRIR .....	49, 249
Yunus ÖZDEMİR .....	334
Yurdal SEVER .....	314
Yusuf KOÇAK .....	315
Yusuf YAYLI .....	102
Yusuf ZEREN .....	113, 142, 172, 234, 316
Yücel ÇENESİZ .....	317
Yüksel SOYKAN .....	184

**Z**

Zameddin. İSMAİLOV .....	244
Zarife ZARARSIZ .....	319
Zehan KESİLMİŞ .....	136
Zeynab JOUYMANDI .....	119
Zeynep EKİCİOĞLU KÜZECİ .....	320
Zhamile ASKEROVA .....	215
Zineb BENMEZIANE .....	349
Zohra Sabrina DELHOUM .....	283
Zuhair NASHED .....	26

ICAA'16

2<sup>nd</sup> INTERNATIONAL CONFERENCE  
ON ANALYSIS AND ITS APPLICATIONS



July 12-15, 2016 Kırşehir / TURKEY

ISBN



ICAA'16

2<sup>nd</sup> INTERNATIONAL CONFERENCE ON ANALYSIS AND ITS APPLICATIONS

JULY 12-15, 2016 KIRŞEHİR/TURKEY

# CERTIFICATE

This is to certify that

**Erhan GÜLER**

has presented an oral presentation entitled

**ROTATIONAL HYPERSURFACE IN 4-SPACE**

during the 2<sup>nd</sup> International Conference on Analysis and its Applications, held on  
July 12-15, 2016 at Ahi Evran University, Kirşehir-TURKEY



**Prof. Dr. Vatan KARAKAYA**

On behalf of Organizing Committee

Chairman

Rector Of Ahi Evran University